


الإطارات (Systems) Frames

نسألكم الدعاء

IF you download the Free **APP. RC Structures**  on your smart phone or tablet, you will be able to play illustrative movies For any paragraph that has a QR code icon 

إذا حملت تطبيق **RC Structures**  على تليفونك المحمول او اللوح السطحي ستستطيع أن تشغل أفلام شرح للمقاطع التي تحتوى على رمز 

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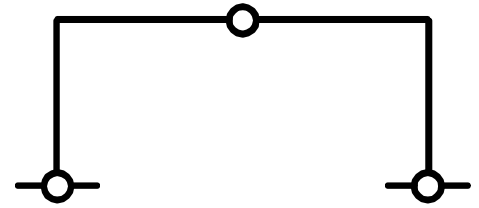
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Types of Frames.



توجد أنواع عديدة من ال **Frames** سدرس أشهرها و هي :

Ⓐ **3 Hinged Frame.**



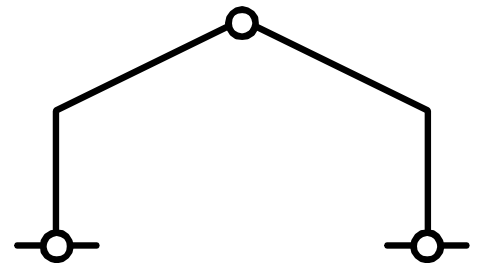
Ⓑ **2 Hinged Frame.**



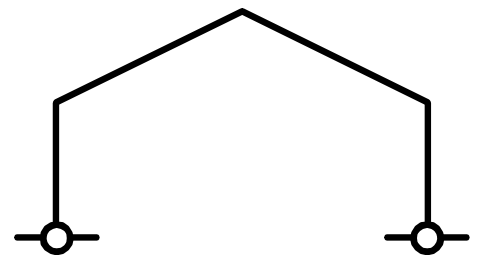
Ⓒ **Fixed Frame.**



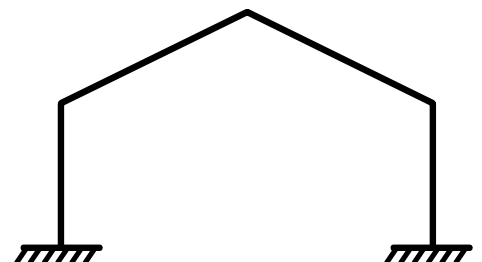
Ⓓ **3 Hinged Inclined Frame.**



Ⓔ **2 Hinged Inclined Frame.**

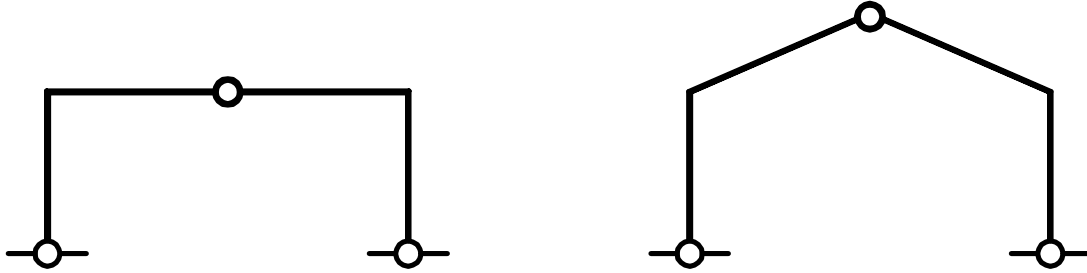


Ⓕ **Fixed Inclined Frame.**

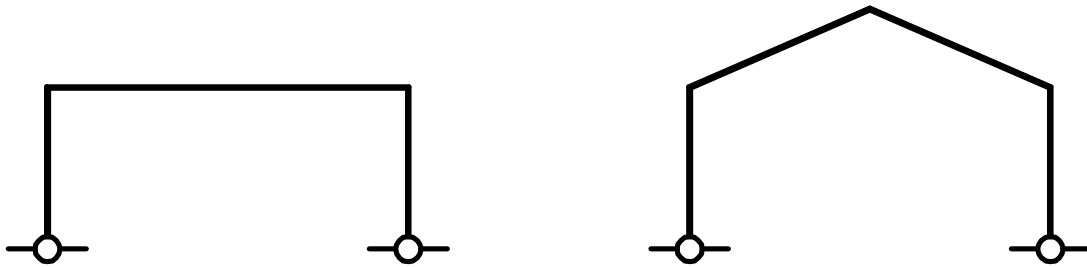


كلما زاد عدد درجات ال *Indeterminacy* لل *system* كلما قلت قيمه ال *moment* و بالتالى يكون ال *system* أرخص .

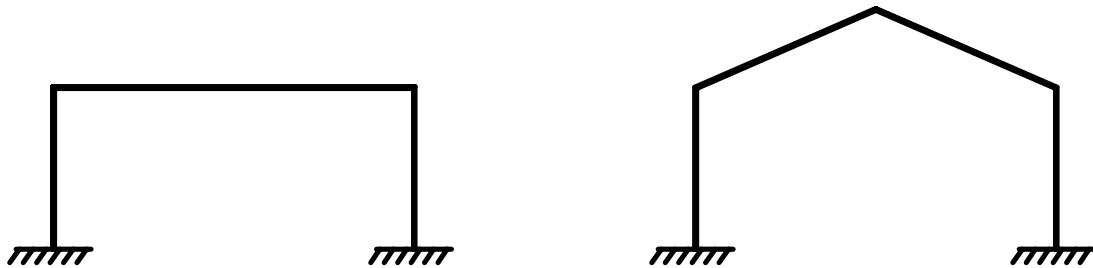
3 Hinged Frame. Detreminate



2 Hinged Frame. Once Statically Indetreminate



Fixed Frame. Twice Statically Indetreminate لانه *symmetric*

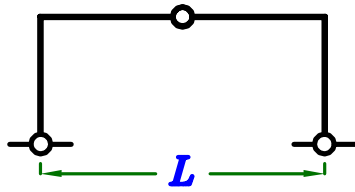


∴ Fixed Frame أرخص من 2 Hinged Frame أرخص من 3 Hinged Frame

Span of Frames.

كلما كان لا **system** عدد درجات **Indeterminacy** أكبر
كلما أستطعنا أن نزيد من **span** ال **system**

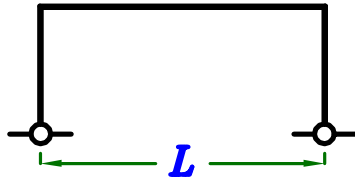
3 Hinged Frame.



$$L = (12 \rightarrow 15) m$$

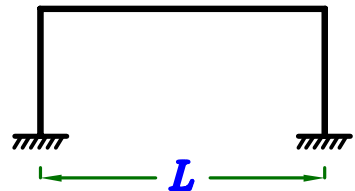
و تصل الى $24 m$ في حالة التربة الضعيفه

2 Hinged Frame.



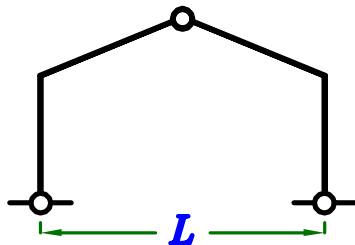
$$L = (12 \rightarrow 22) m$$

Fixed Frame.



$$L = (12 \rightarrow 24) m$$

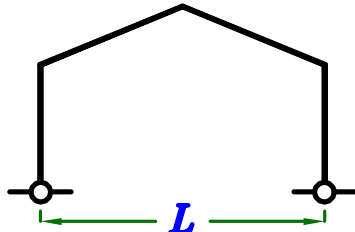
Inclined 3 Hinged Frame.



$$L = (12 \rightarrow 15) m$$

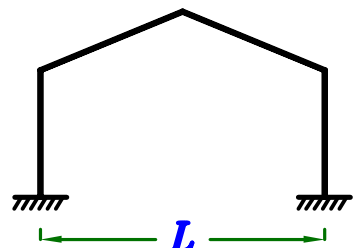
و تصل الى $24 m$ في حالة التربة الضعيفه

Inclined 2 Hinged Frame.



$$L = (12 \rightarrow 22) m$$

Inclined Fixed Frame.

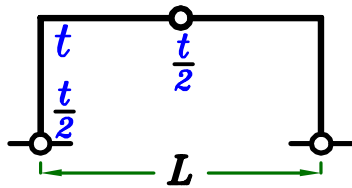


$$L = (12 \rightarrow 24) m$$

Depth of Frames.

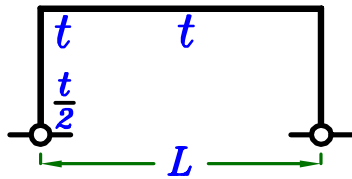
كلما كان لا **system** عدد درجات **Indeterminacy** أكبر
كلما أستطعنا أن نقلل من تخانة ال **system**

3 Hinged Frame.



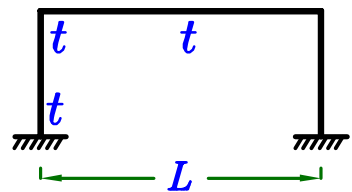
$$t \approx \frac{L}{10}$$

2 Hinged Frame.



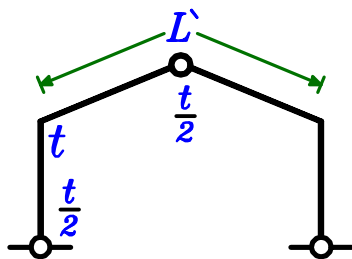
$$t \approx \frac{L}{12 \rightarrow 14}$$

Fixed Frame.



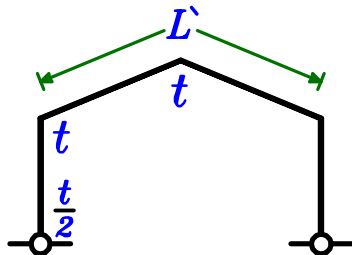
$$t \approx \frac{L}{14 \rightarrow 16}$$

3 Hinged Inclined Frame.



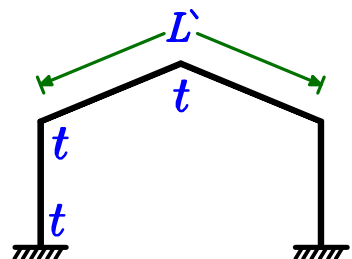
$$t \approx \frac{L'}{10}$$

2 Hinged Inclined Frame.



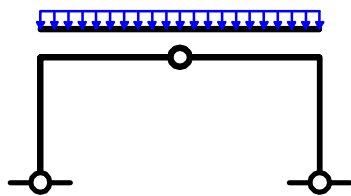
$$t \approx \frac{L'}{12 \rightarrow 14}$$

Fixed Inclined Frame.

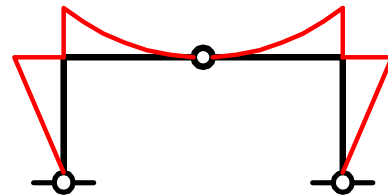
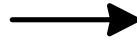


$$t \approx \frac{L'}{14 \rightarrow 16}$$

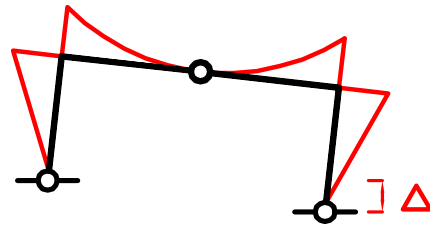
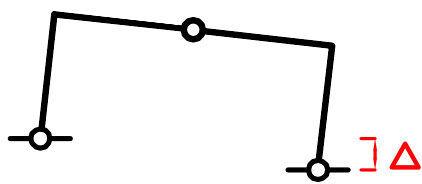
لكن كلما كانت التربة أضعف أى متوقع حدوث **Differential Settlement** أكبر كلما كان من الأفضل أن نختار **system** عدد درجات ال **Indeterminacy** له أقل .
لانه لو كان **determinate system** و حدث له هبوط لعمود واحد فقط اتجاه ال **moment** لن يتغير و بالتالى يكون الحديد الموضوع مناسب فلا يحدث انهيار ال **system** .



3 Hinged Frame.
Determinate

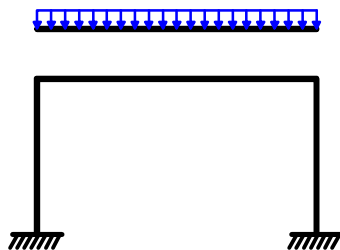


شكل و اتجاه ال **moment** للاحمال الرأسية
الموضوع على اساسه التسليح

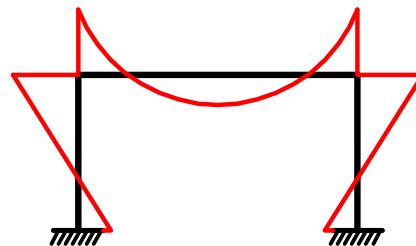


اتجاه ال **moment** لم يتغير
اى نفس مكان التسليح الموضوع

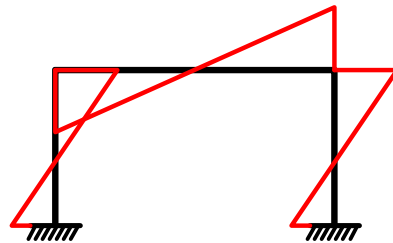
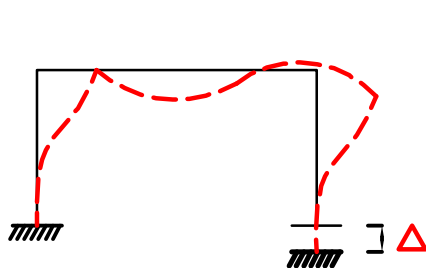
لكن لو **indeterminate system** و كان عدد درجات ال **Indeterminacy** كبير عند حدوث هبوط لعمود واحد فقط يتغير اتجاه ال **moment** عن اتجاه الحديد الاصلى و بالتالى من الممكن ان يؤدى الى انهيار ال **system** .



Fixed Frame.
Twice Statically Indeterminate



شكل و اتجاه ال **moment** للاحمال الرأسية
الموضوع على اساسه التسليح



اتجاه ال **moment** تغير اى لن يكون نفس مكان التسليح الاصلى
من الممكن ان يؤدى الى انهيار ال **system**

لذا اذا كانت التربة ضعيفه يجب استخدام **determinate system حتى لو كان أعلى .**

Choosing Type of Frame.

1 – Type of Soil. Weak Soil. (Clay)

Span (12 → 24) m

use **3 Hinged Frame**

2 – Type of Soil. No Soil data. (or sand)

Span (12 → 22) m

use **2 Hinged Frame**

3 – Type of Soil. No Soil data. (or sand)

Span (22 → 24) m

use **Fixed Frame**

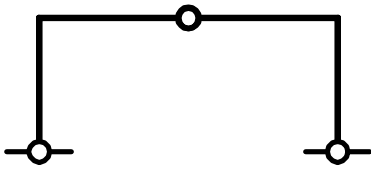
4 – Type of Soil. Hard Soil (Rock or condensed sand)

Span (12 → 24) m

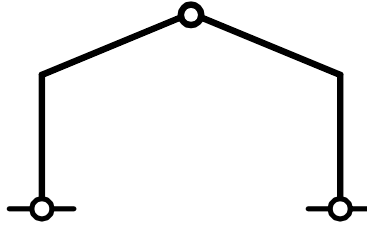
use **Fixed Frame**

Analysis Methods of Frames.

3 Hinged Frame.



3 Hinged Inclined Frame.



→ **Determinate.**

2 Hinged Frame.



Once Statically Indet.

Fixed Frame.



No Sway

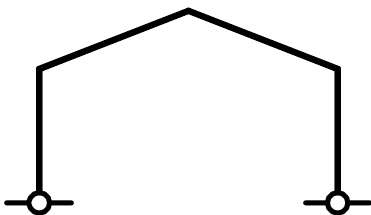
الاسفل

→ **Moment Distribution**

Twice Statically Indet.

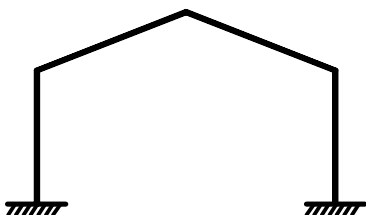
لانه symmetric

2 Hinged Inclined Frame.



Once Statically Indet.

Fixed Inclined Frame.



Twice Statically Indet.

لانه symmetric

Sway

الاسفل

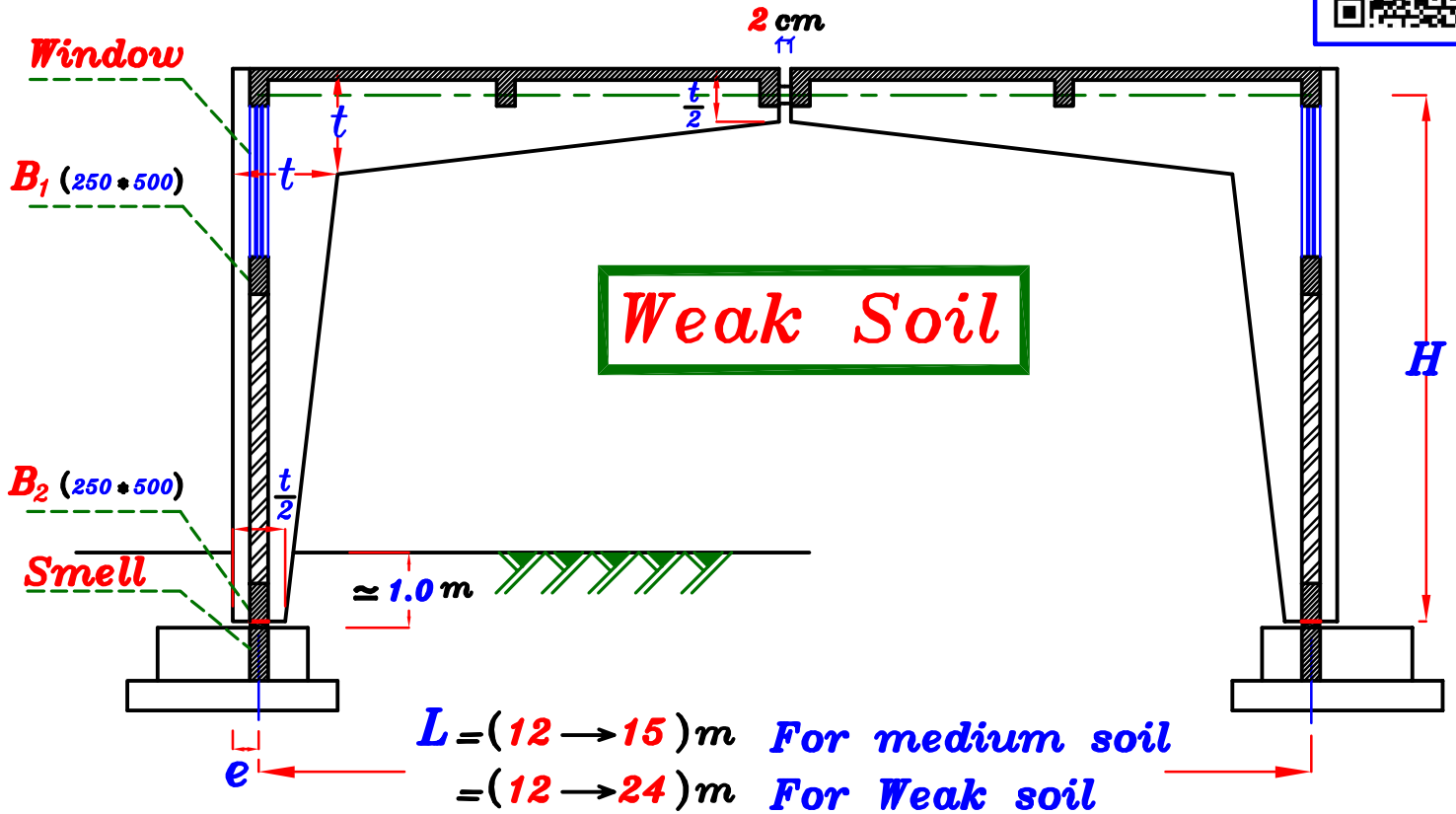
→ **Virtual Work**

Sway

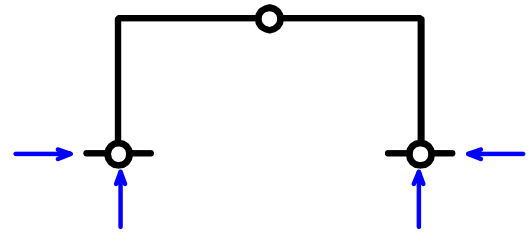
الاسفل

→ **Approximate Method.**

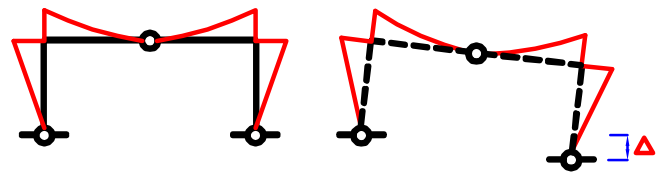
Three Hinged Frame.



– Statical System



The 3 hinged Frame is Statically Determinate structure
So, It is better For WEAK soil.



– Concrete Dimensions.

* **Span (L) = (12 → 15) m For medium soil**
= (12 → 24) m For Weak soil

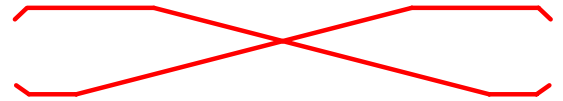
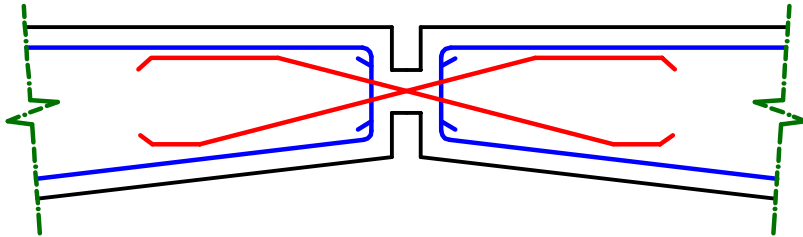
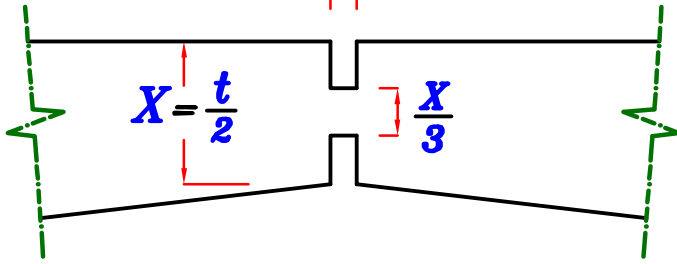
* **$t \approx \frac{L}{10}$**

* **$b = 0.30 \text{ m}$** } **الأكبر**
Spacing
20

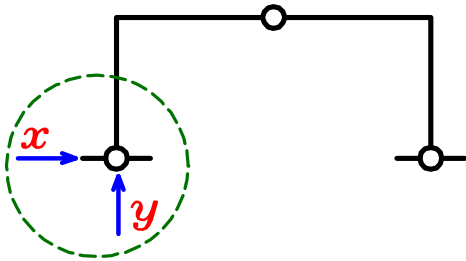
- يوجد فاصل بين ال **Two Frames**

عباره عن **Hinge**

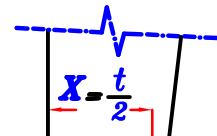
2 cm



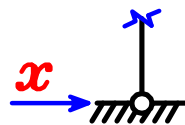
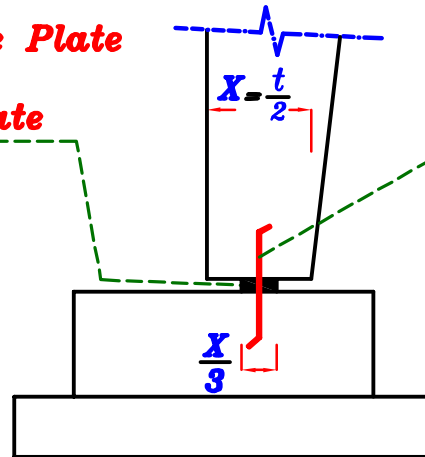
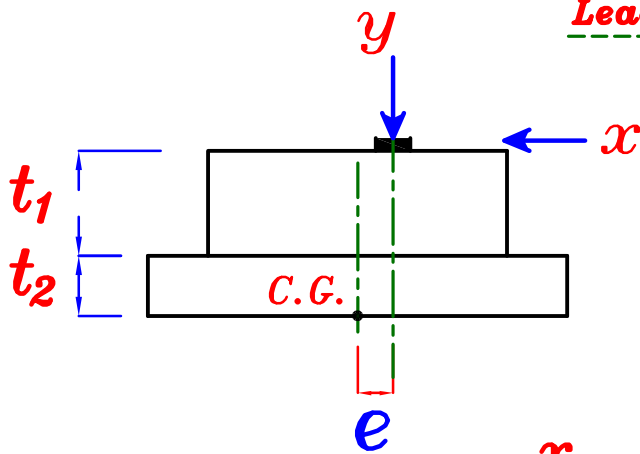
- القواعد عباره عن **Real Hinge**



Neoprene Plate
OR
Lead Plate



أسيخ حديد
لمنع الحركة الافقيه

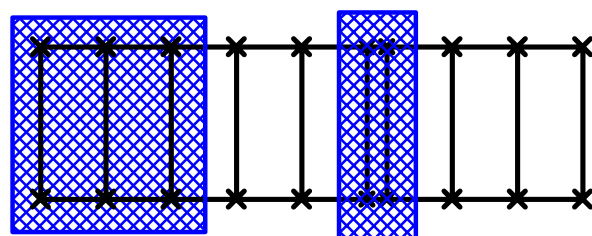
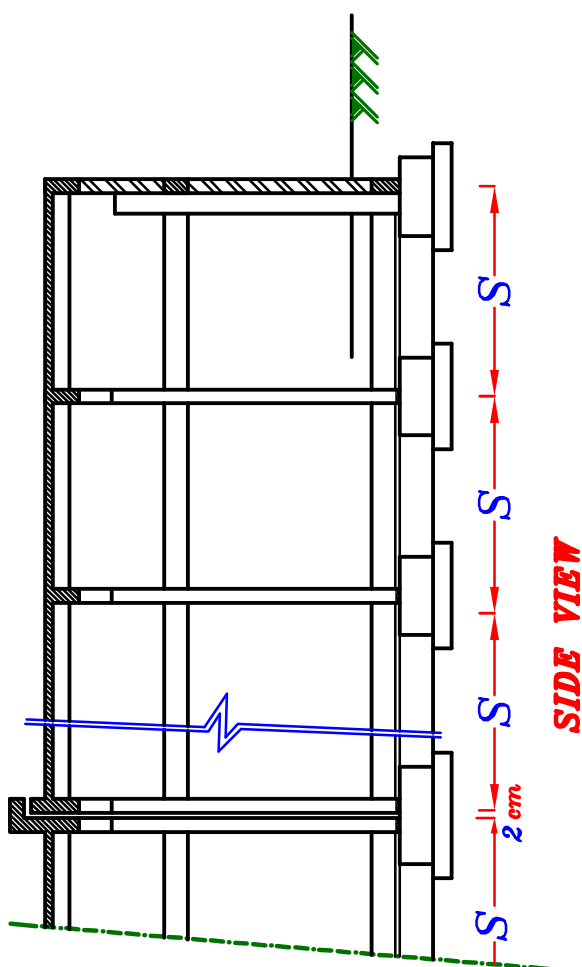
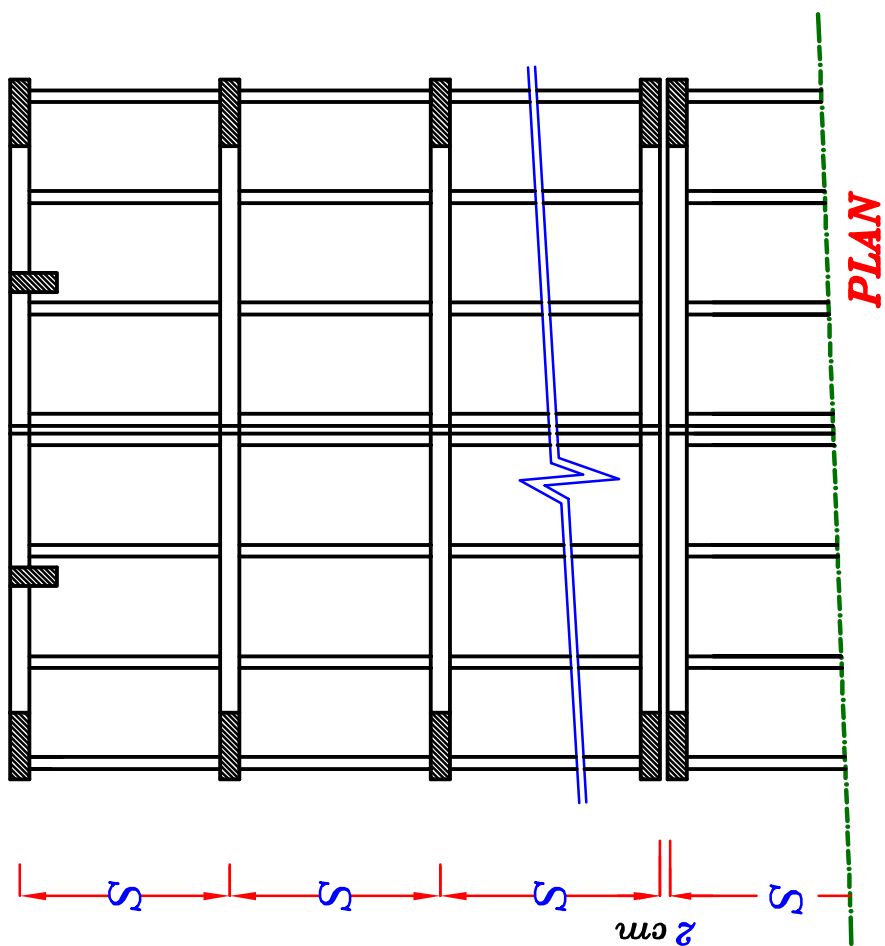
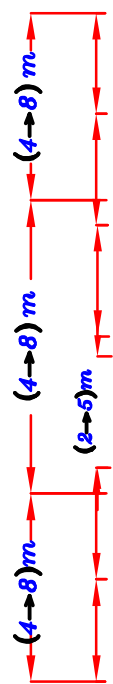
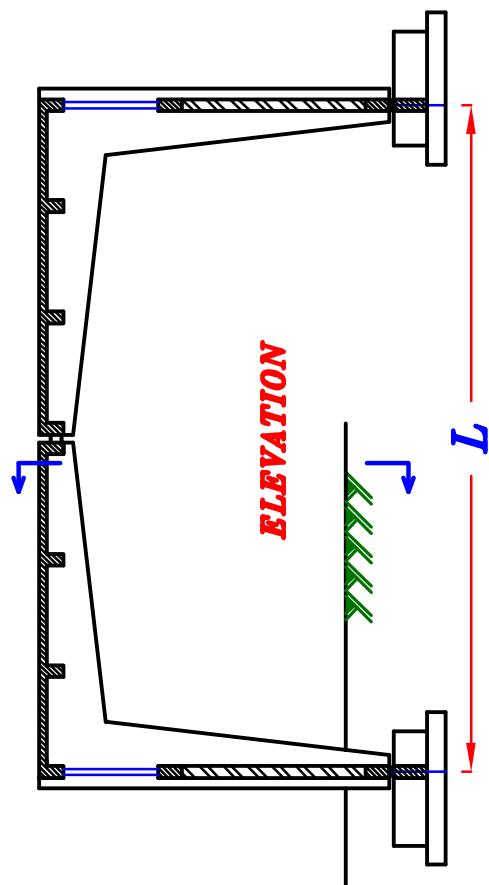


ترحل القواعد عكس إتجاه ال **(X)**

أى ترحل القواعد للخارج مسافه **(e)** لعمل **uniform stress** على التربه

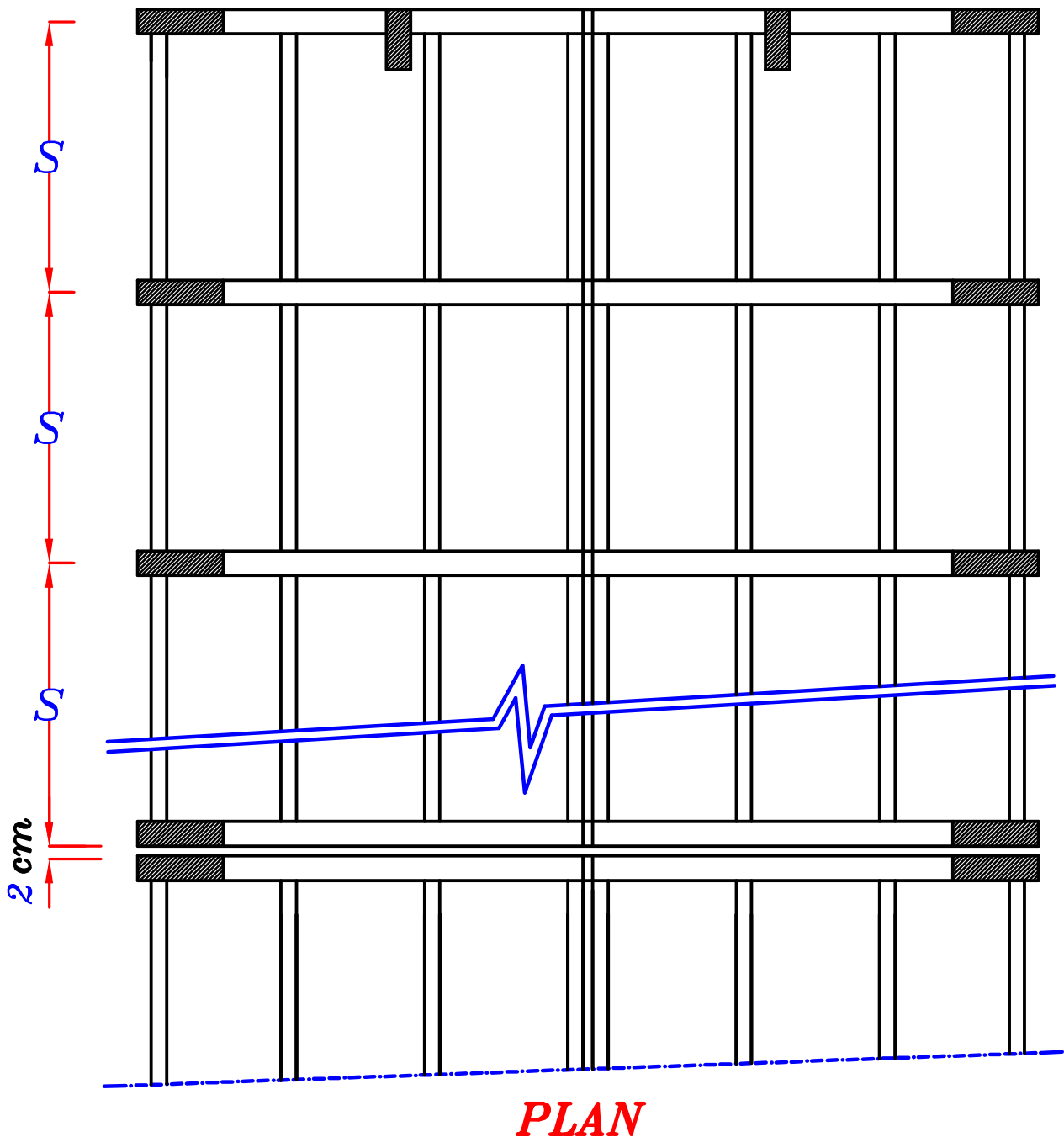
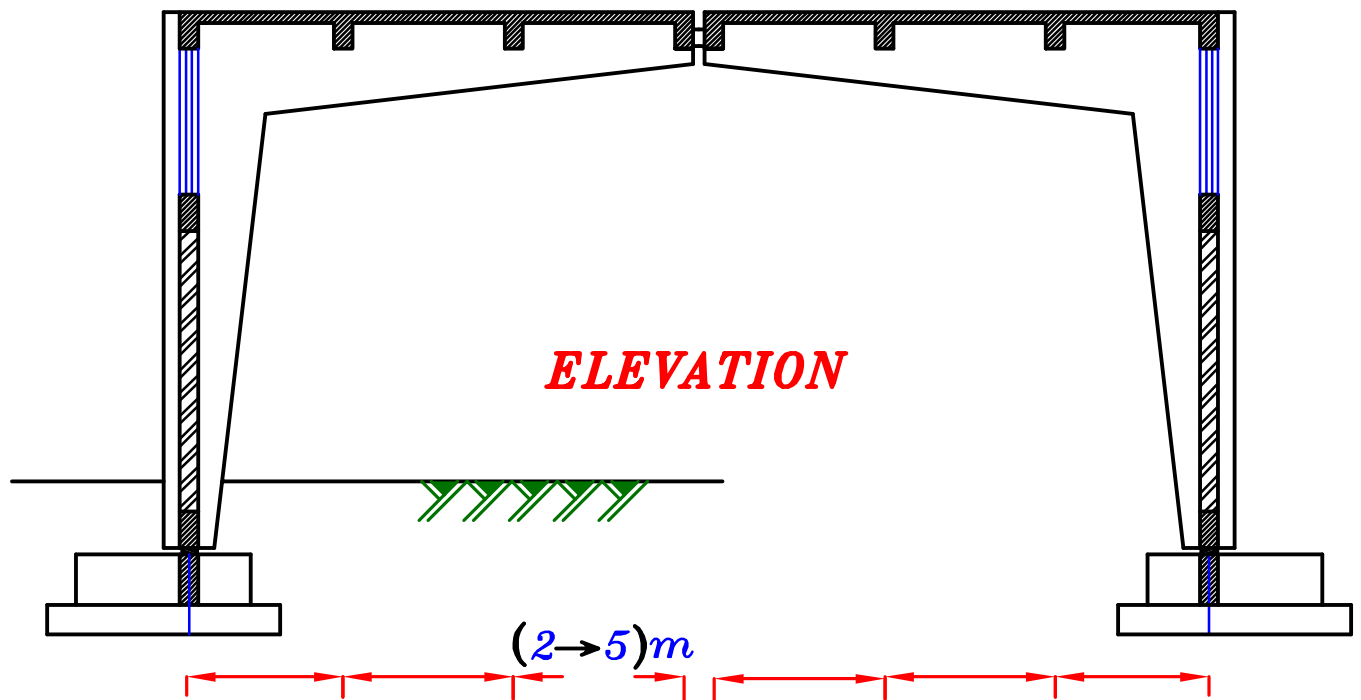
$$\therefore \sum M_{C.G.} = \text{Zero} \quad \therefore x(t_1 + t_2) - y(e) = \text{Zero}$$

$$\therefore e = \frac{x(t_1 + t_2)}{y} \approx (0.25 \rightarrow 0.50) m$$



KEY PLAN

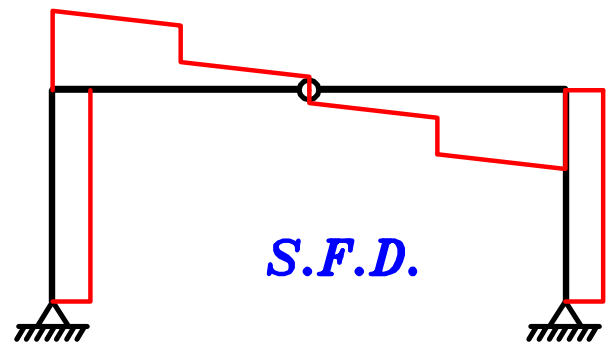
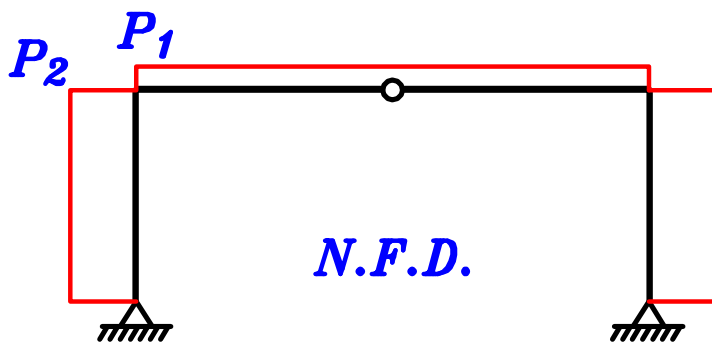
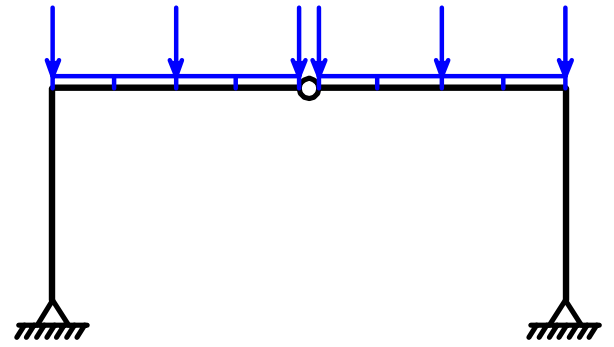
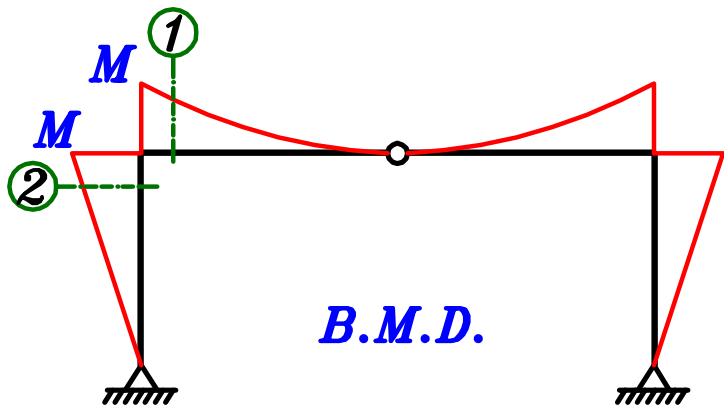
1:200 → **1:400**



Steps of Design.

خطوات المسألة .

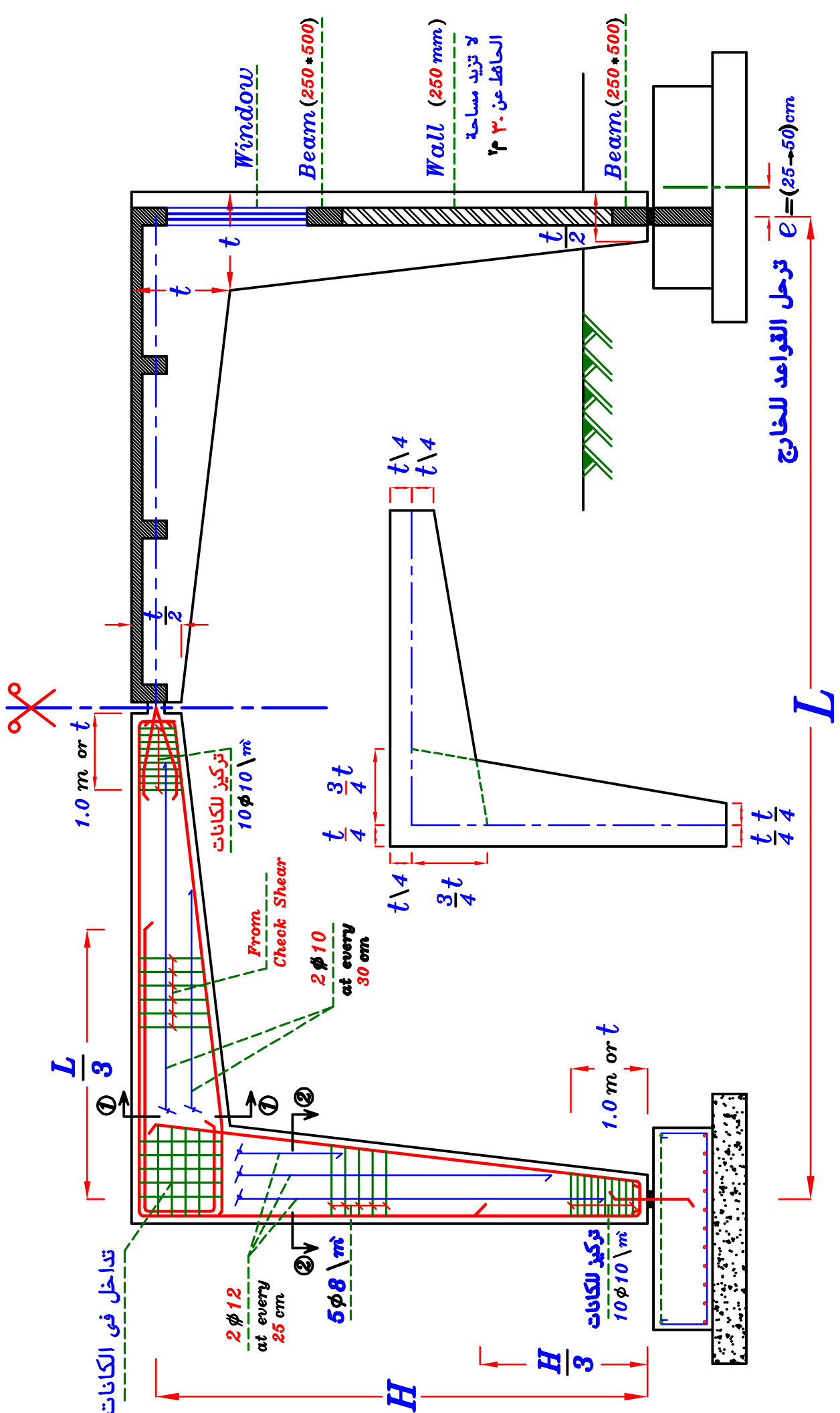
- ١- اختيار ال *system*
- ٢- رسم *Dim. concrete* في ال *elevation & Plan*
- ٣- رسم تسليح البلاطة على نفس ال *Plan*
- ٤- عمل *Load distribution* للبلاطات و حساب الاحمال على ال *System*
- ٥- حل ال *System* و رسم *B.M.D. & N.F.D.*
- ٦- تصميم مقاطعات ال *System* على *M, P*
- ٧- رسم تسليح ال *System* في ال *elevation & cross-sec.*

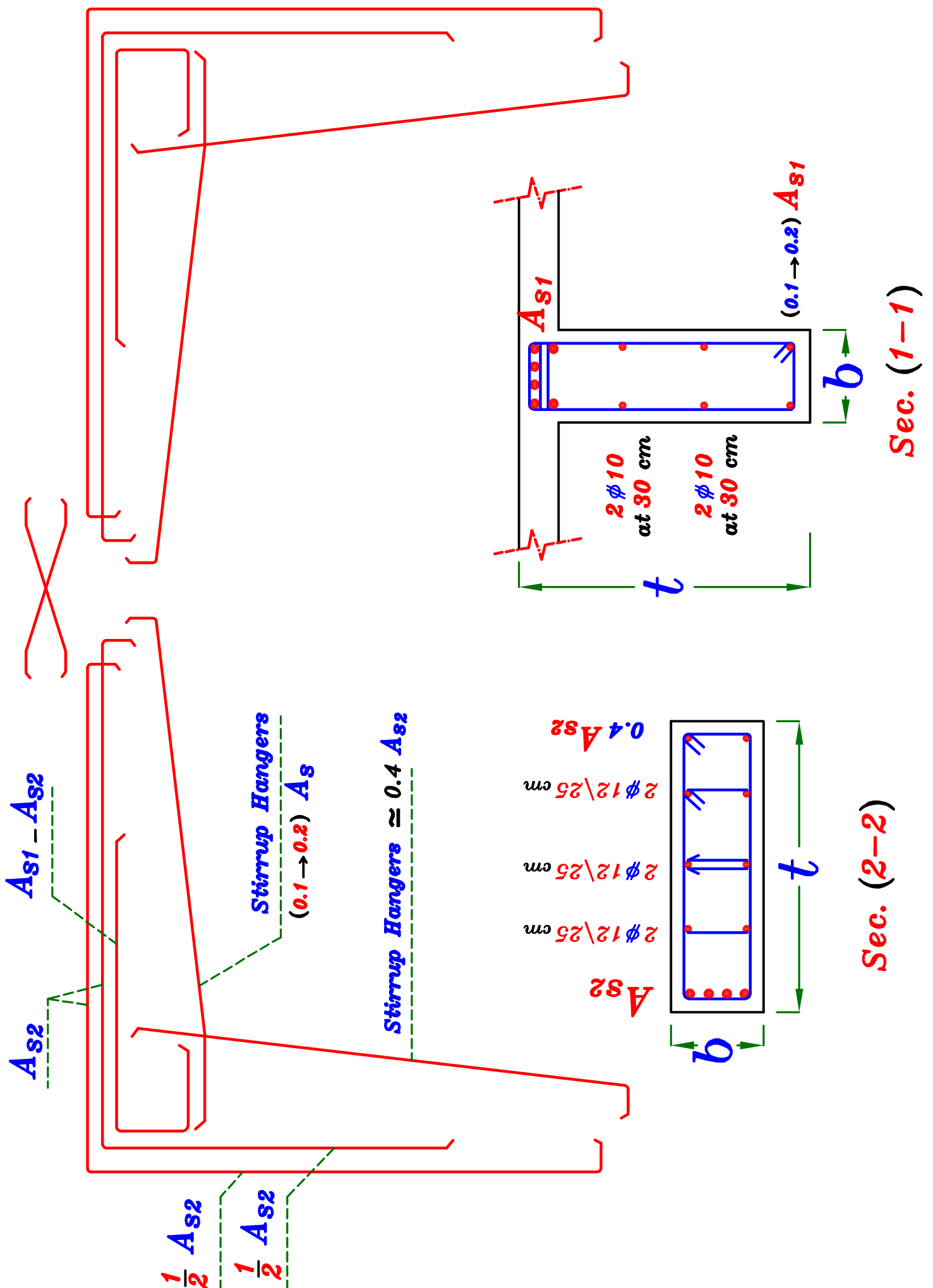


Design:

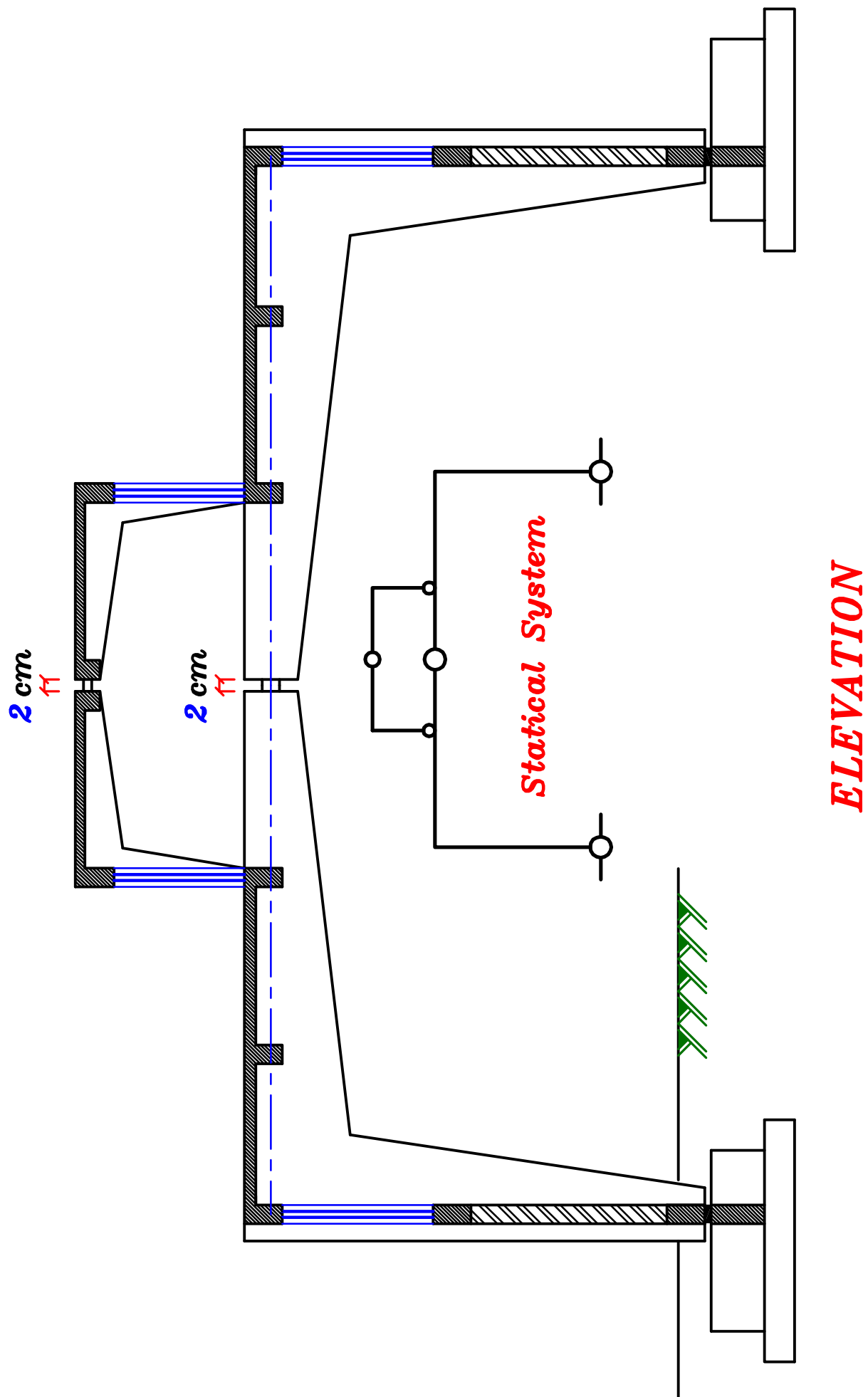
Sec. ① on $M, P_1 \rightarrow$ Get A_{s1}
Sec. ② on $M, P_2 \rightarrow$ Get A_{s2} } Note: $A_{s1} > A_{s2}$

RFT. of the Frame.

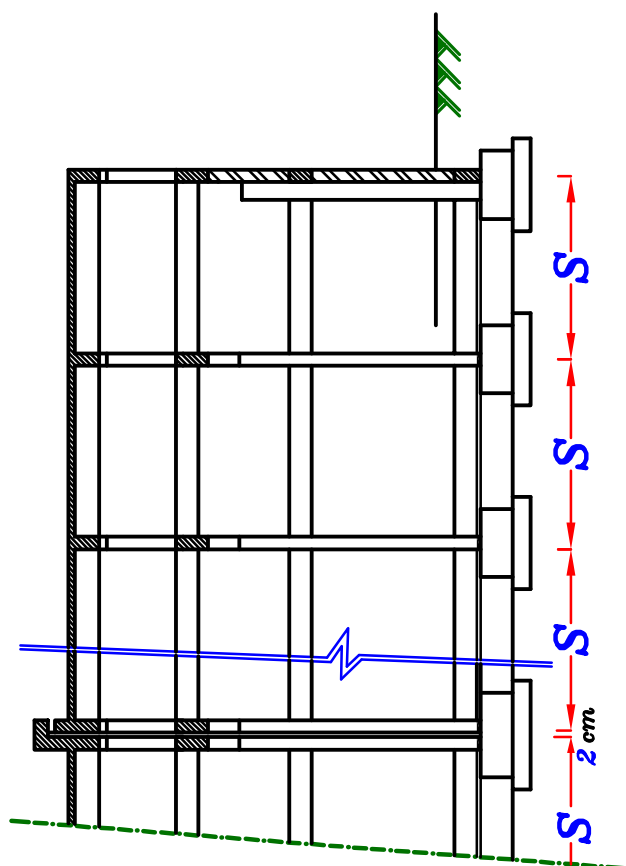




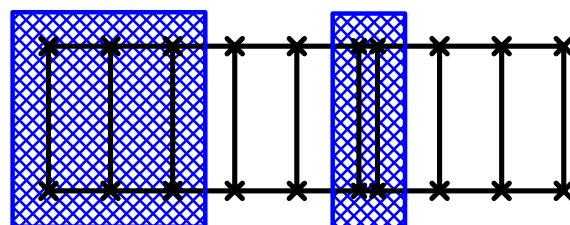
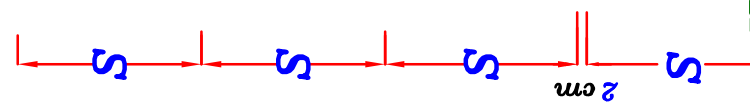
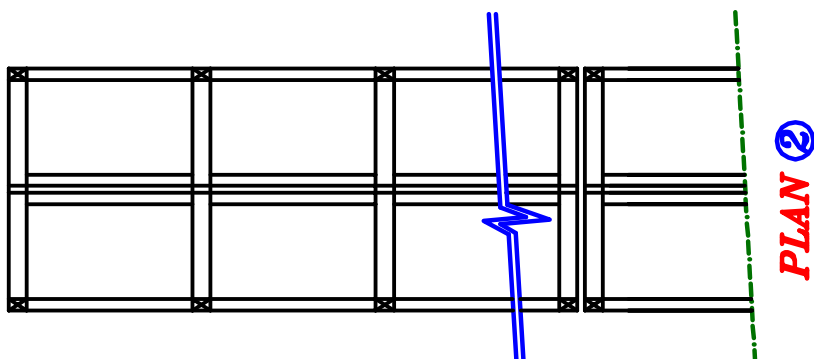
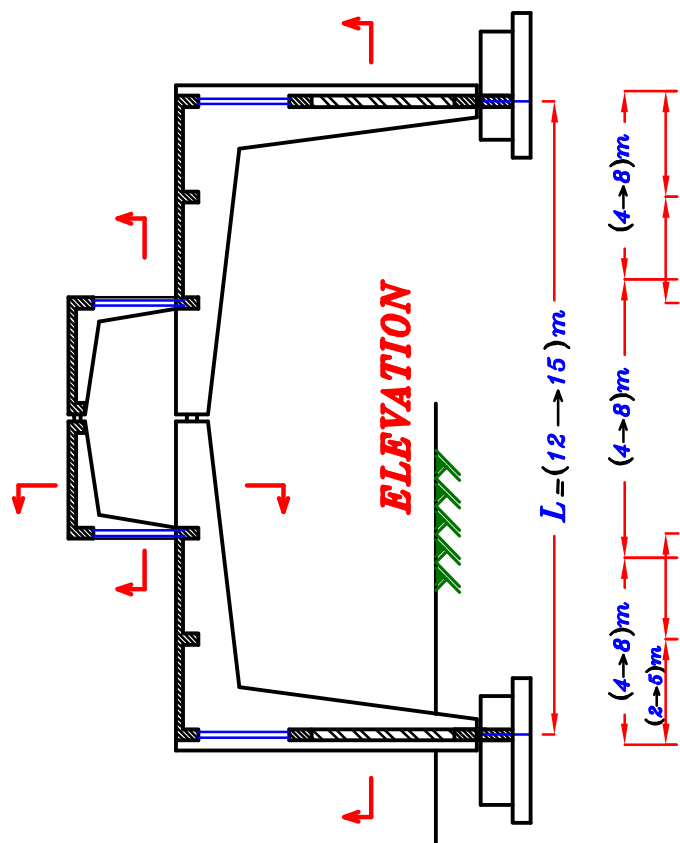
3 Hinged Frame with Sky Light.



3 Hinged Frame with Sky Light.

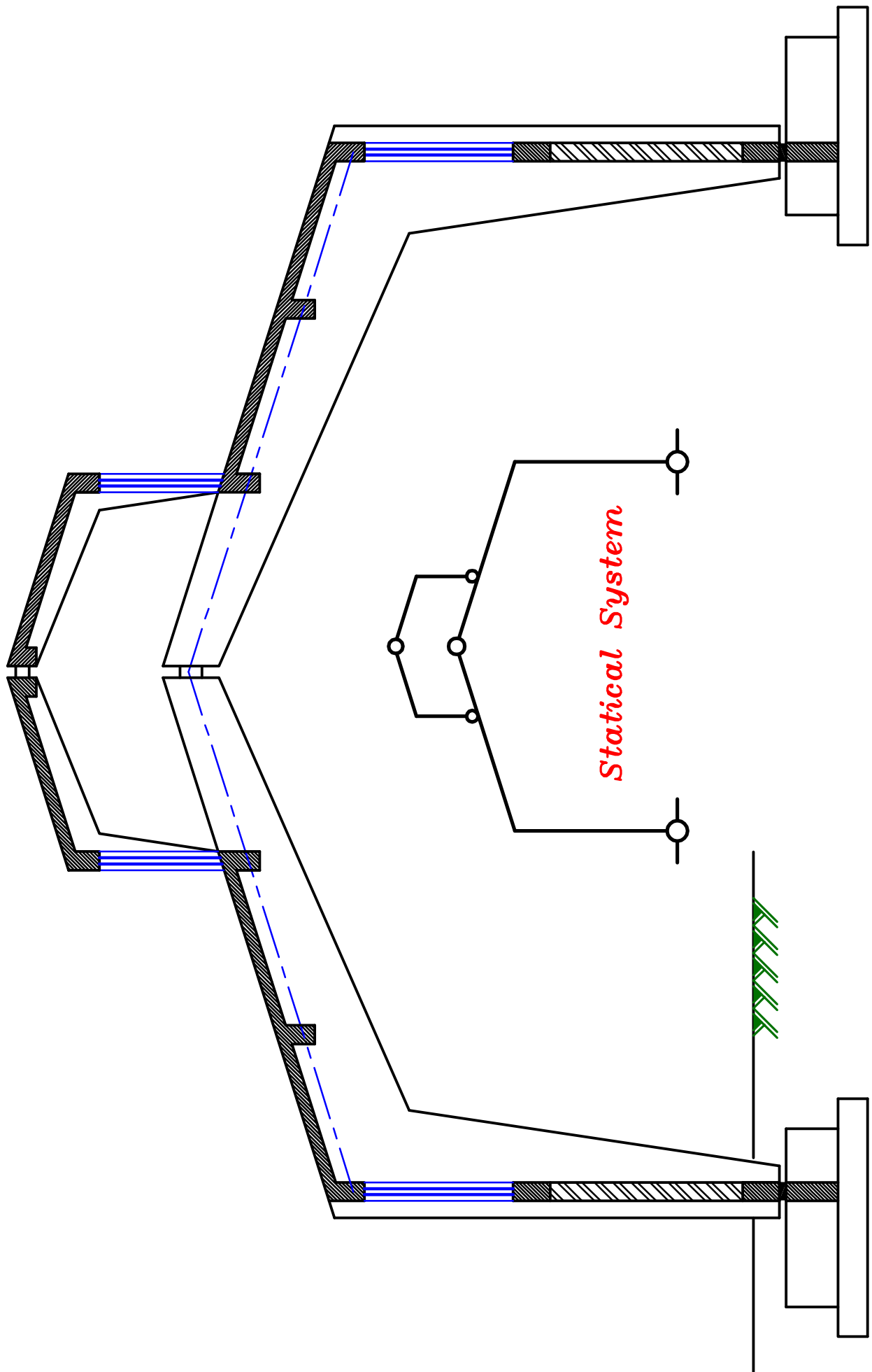


SIDE VIEW



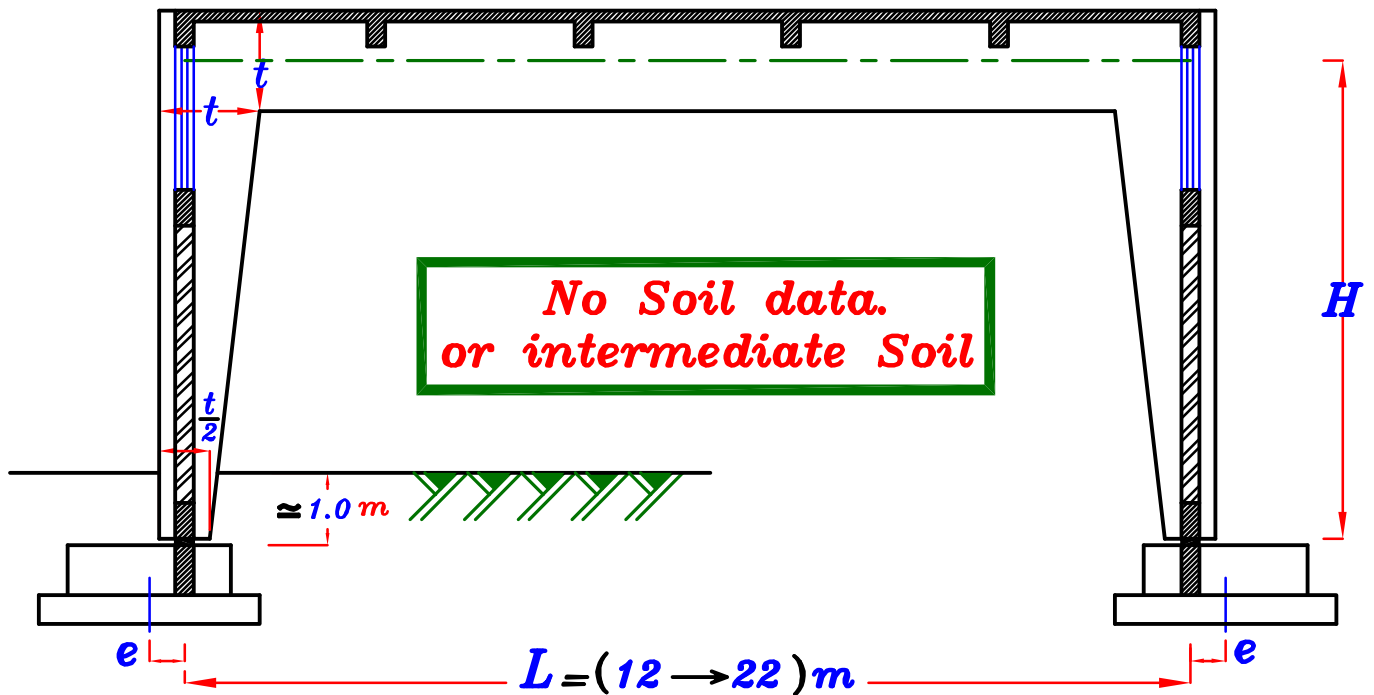
KEY PLAN

1:200 → 1:400



ELEVATION

Two Hinged Straight Frame.



– Statical System

The 2 hinged Frame is
Once Statically indeterminate structure

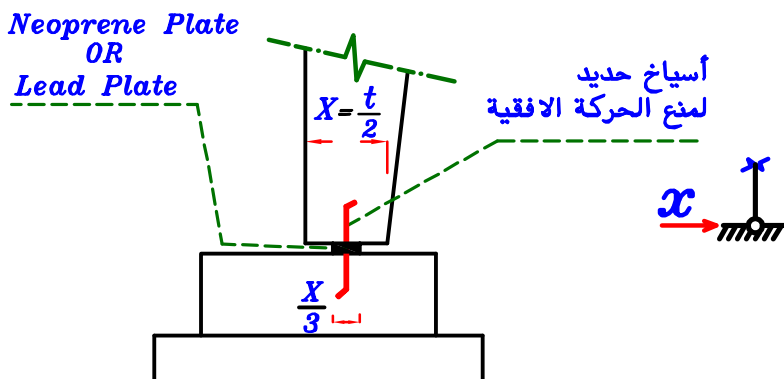


– Concrete Dimensions.

* **Span** (L) = (12 → 22) m

* $t \approx \frac{L}{12 \rightarrow 14}$

* $b = 0.30 \text{ m}$
 $\frac{\text{Spacing}}{20}$ } الأكبر

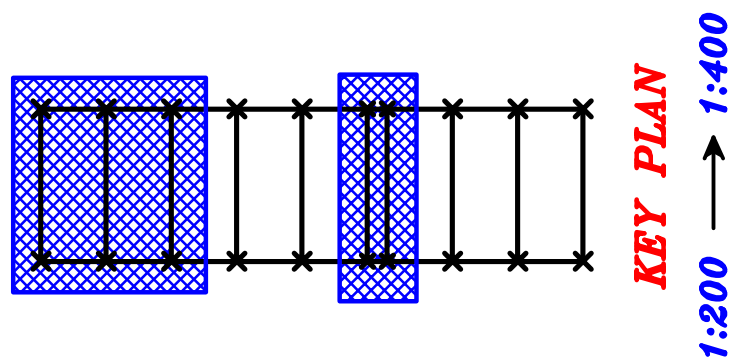
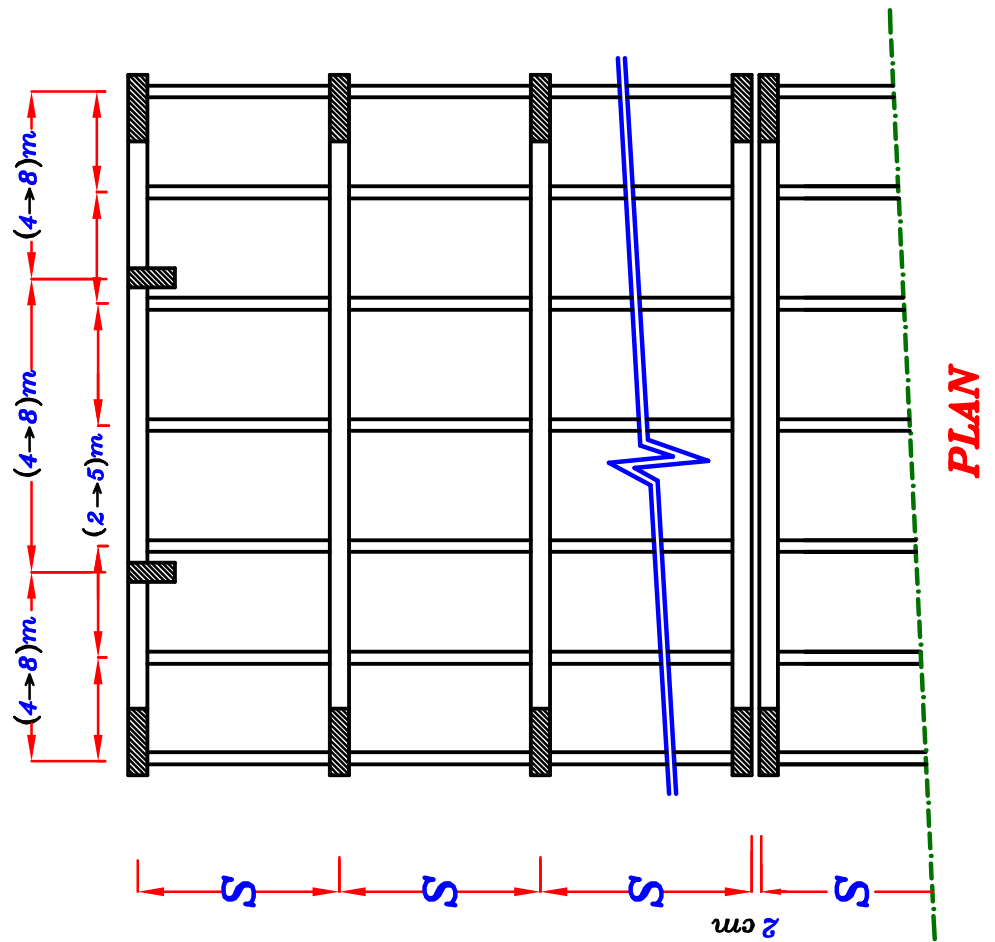
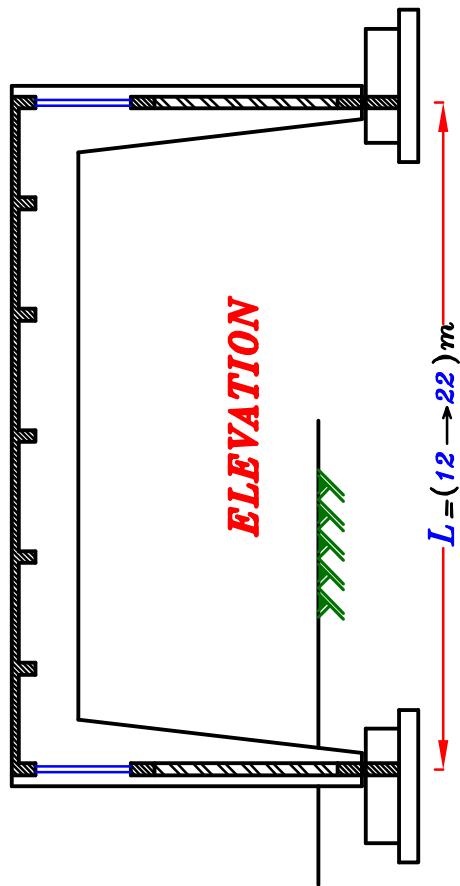
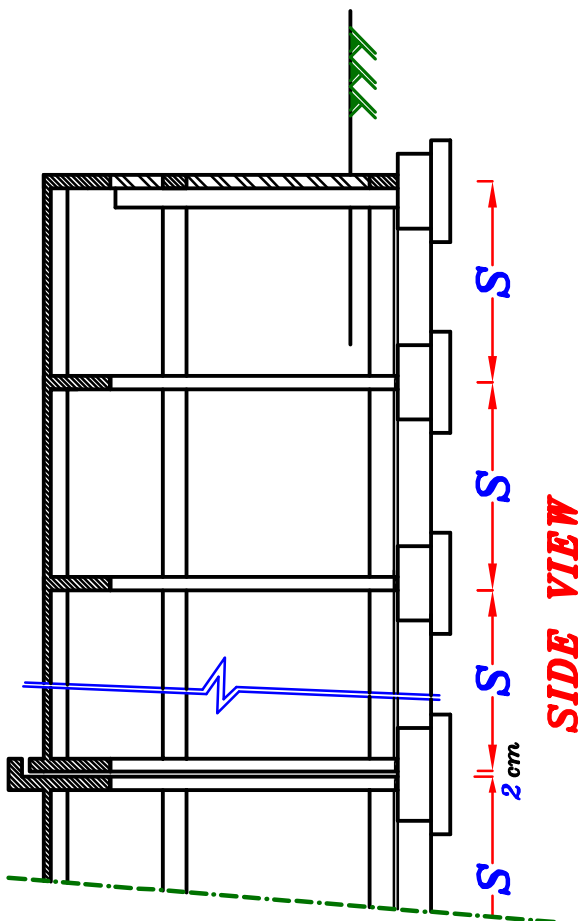


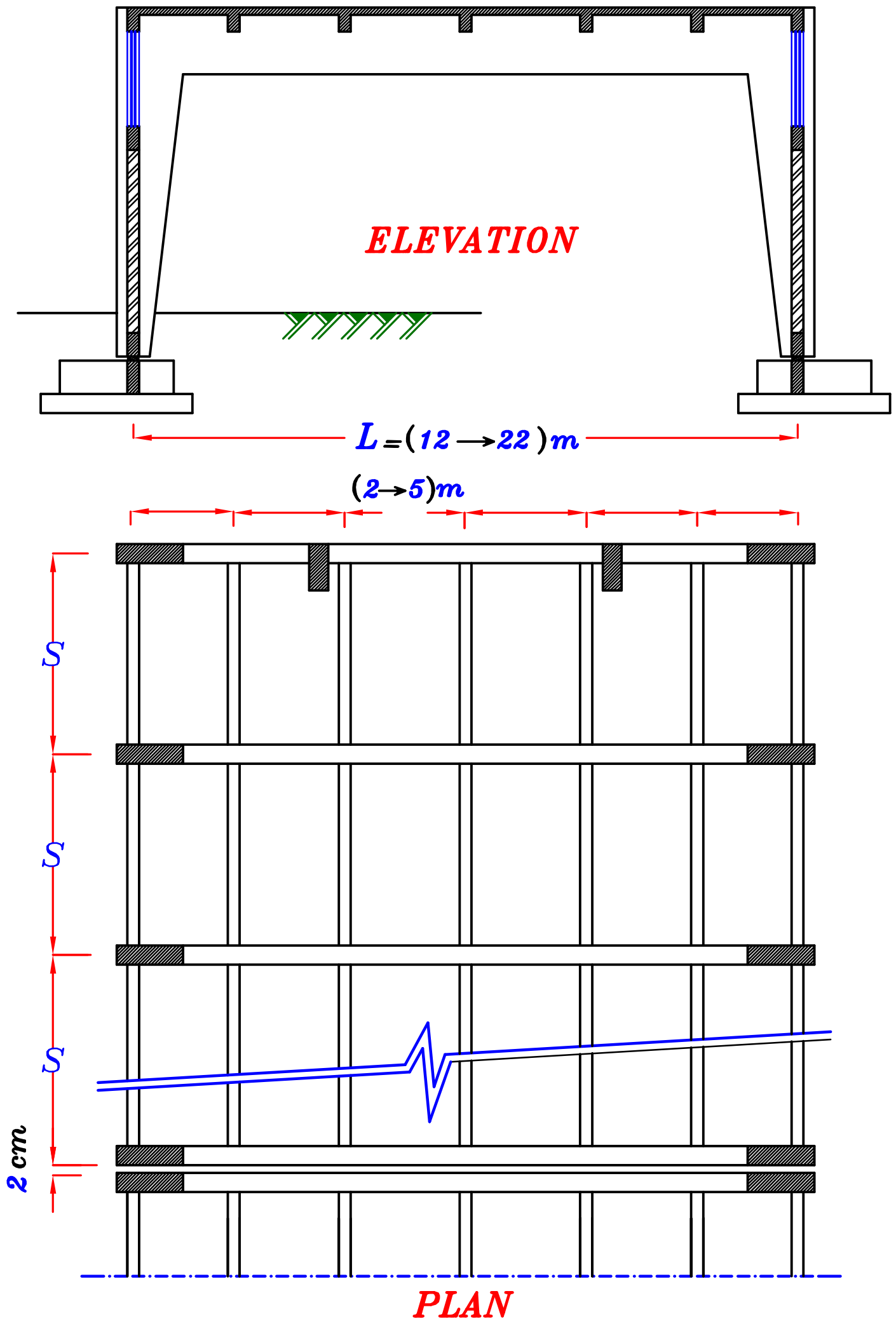
– القواعد عبارة عن **Real Hinge**

ترحل القواعد عكس إتجاه الـ (x)

أى ترحل القواعد للخارج مسافه (e)

لعمل **uniform stress** على التربة





Steps of Design.

خطوات المسألة .

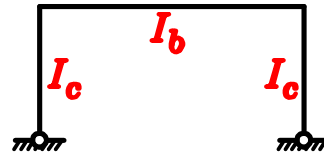
- ١- اختيار ال *system*
- ٢- رسم *concrete Dim.* في ال *elevation & Plan*
- ٣- رسم تسليح البلاطه على نفس ال *Plan*
- ٤- عمل *Load distribution* للبلاطات و حساب الاحمال على ال *System*
- ٥- حل ال *System* و رسم *B.M.D. & N.F.D.*
- ٦- تصميم مقاطعات ال *System* على *M,N*
- ٧- رسم تسليح ال *System* في ال *elevation & cross-sec.*

Moment Distribution Method.

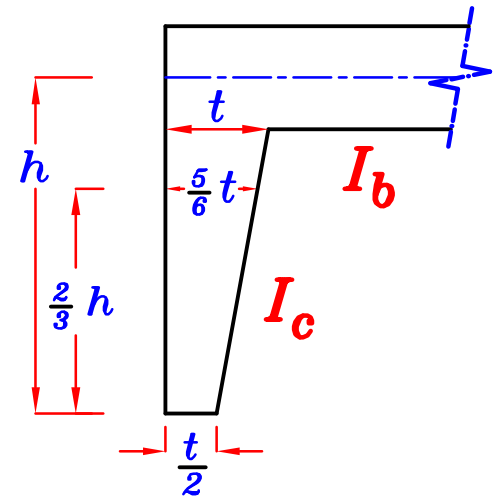
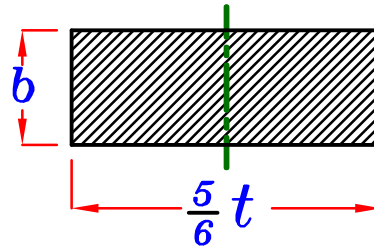
- Ⓐ Get Moment of Inertia For all members. (*I*)
- Ⓑ Get Distribution Factors at all Joints. (*D.F.*)
- Ⓒ Get Fixed End Moments For Beams. (*F.E.M.*)
- Ⓓ Get the Final Moment. (*M_F*)
- Ⓔ Get *B.M.D. , N.F.D. , S.F.D.*

1 – Calculate Moment of Inertia For members.

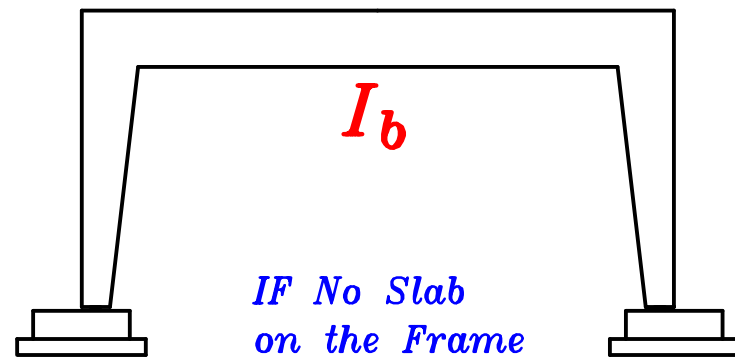
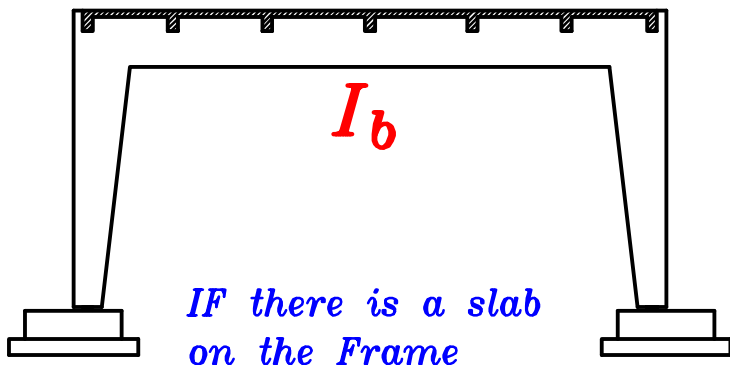
* For Column.



$$I_c = \frac{b \left(\frac{5}{6} t \right)^3}{12}$$



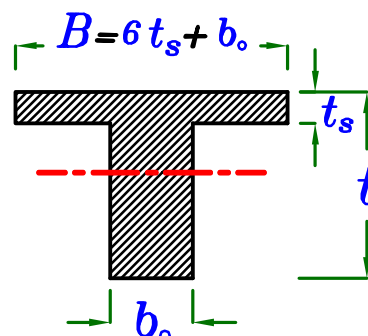
* For Beams.



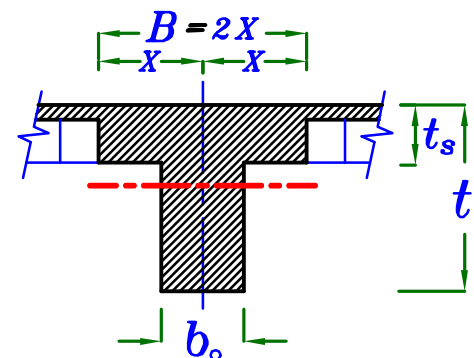
① IF there is a slab on the Frame.

$$I_b = (\mu * 10^{-4}) B t^3$$

old Tables page 91



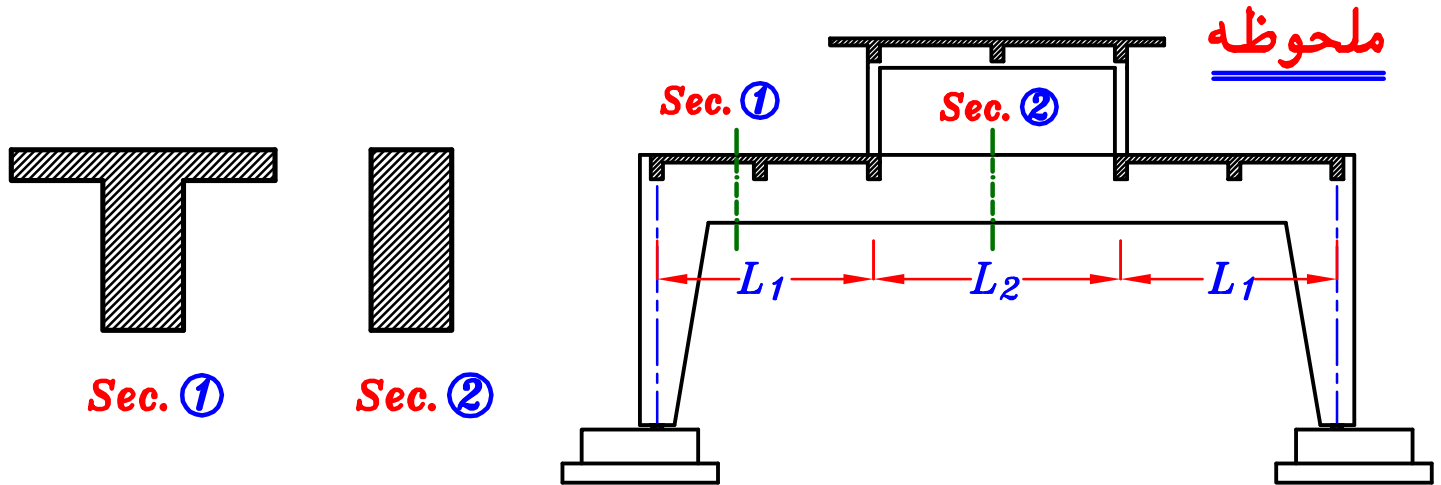
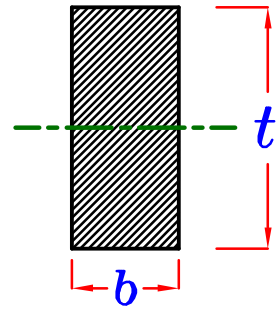
For Solid slab.



For H.B. slab.

② IF there is no slab on the Frame.

$$I_b = \frac{b(t)^3}{12}$$



عند وجود شخشيخة يوجد قطاعان في كمره ال **Frame**

$$I_b = \frac{I_{b1} * 2L_1 + I_{b2} * L_2}{2L_1 + L_2}$$

نأخذ المتوسط

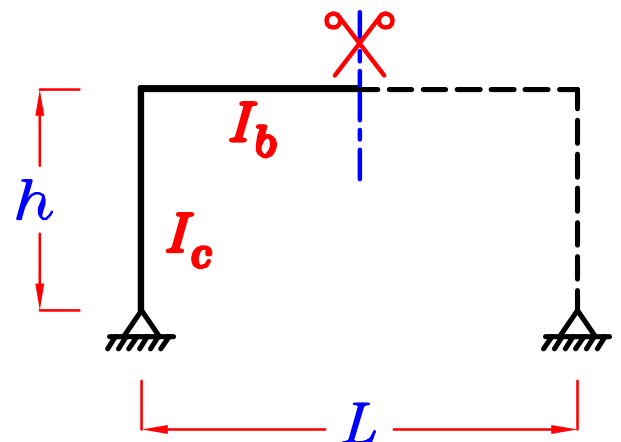
2- Get the Distribution Factor.

$$K_b = \frac{1}{2} \frac{I_b}{L}$$

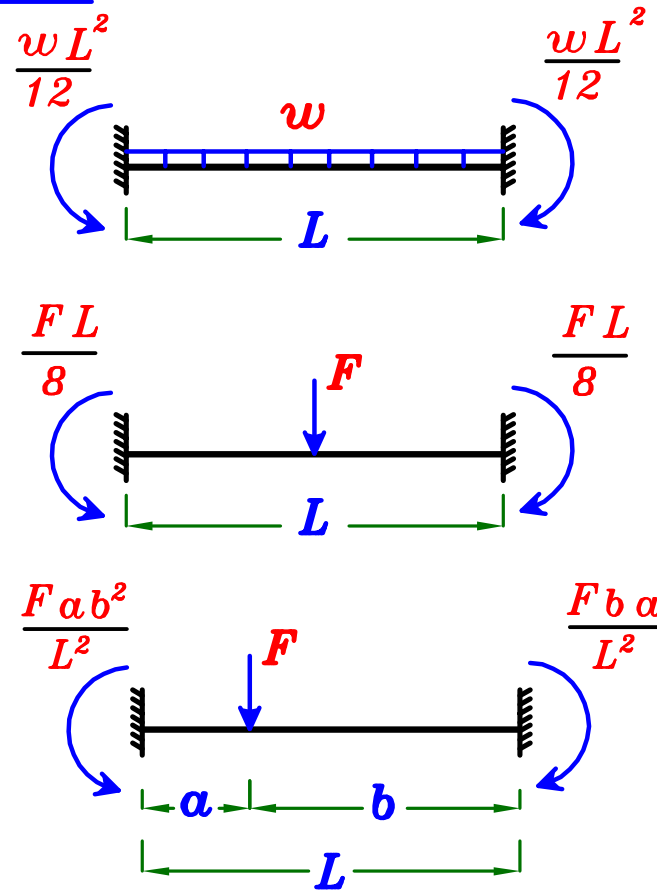
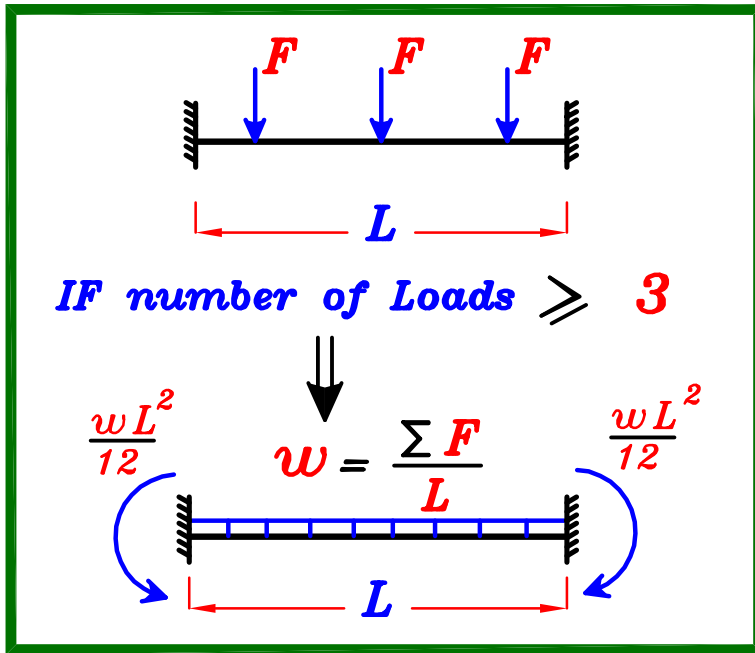
$$K_c = \frac{3}{4} \frac{I_c}{h}$$

$$D.F._c = \frac{K_c}{K_b + K_c}$$

$$D.F._b = \frac{K_b}{K_b + K_c}$$

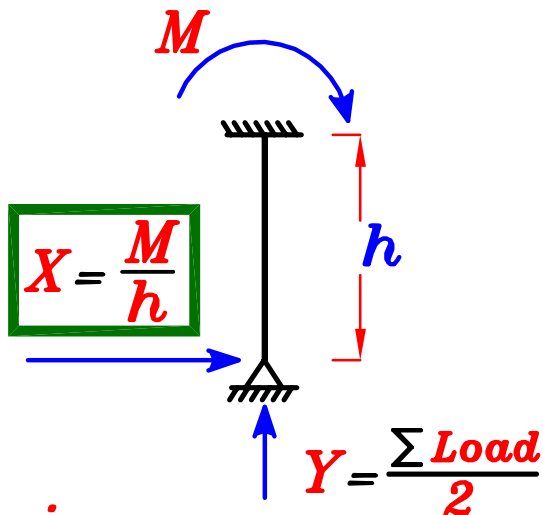


3- Get Fixed End Moment.



4- Calculate the moment.

$$M = F.E.M. (Beam) * D.F. (Col.)$$

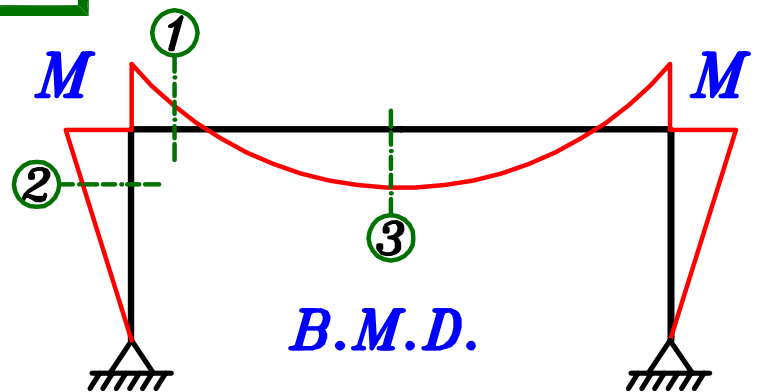


Design:

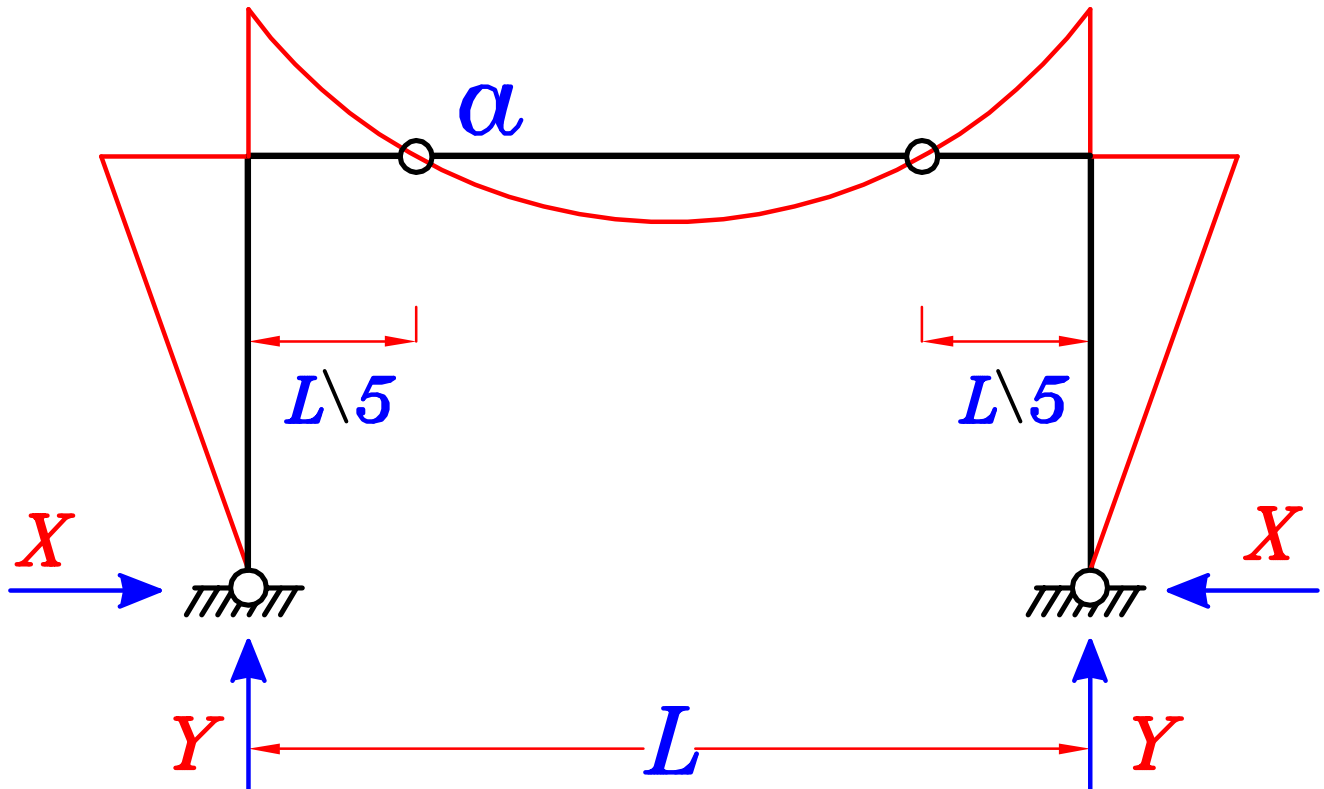
Sec. ① on M , P R-Sec.

Sec. ② on M , P R-Sec.

Sec. ③ on M , P T-Sec.



Approximate Solution.



assume that in the beam there is an intermediate hinge at $\frac{L}{5}$

$$Y = \frac{\sum \text{Loads}}{2}$$

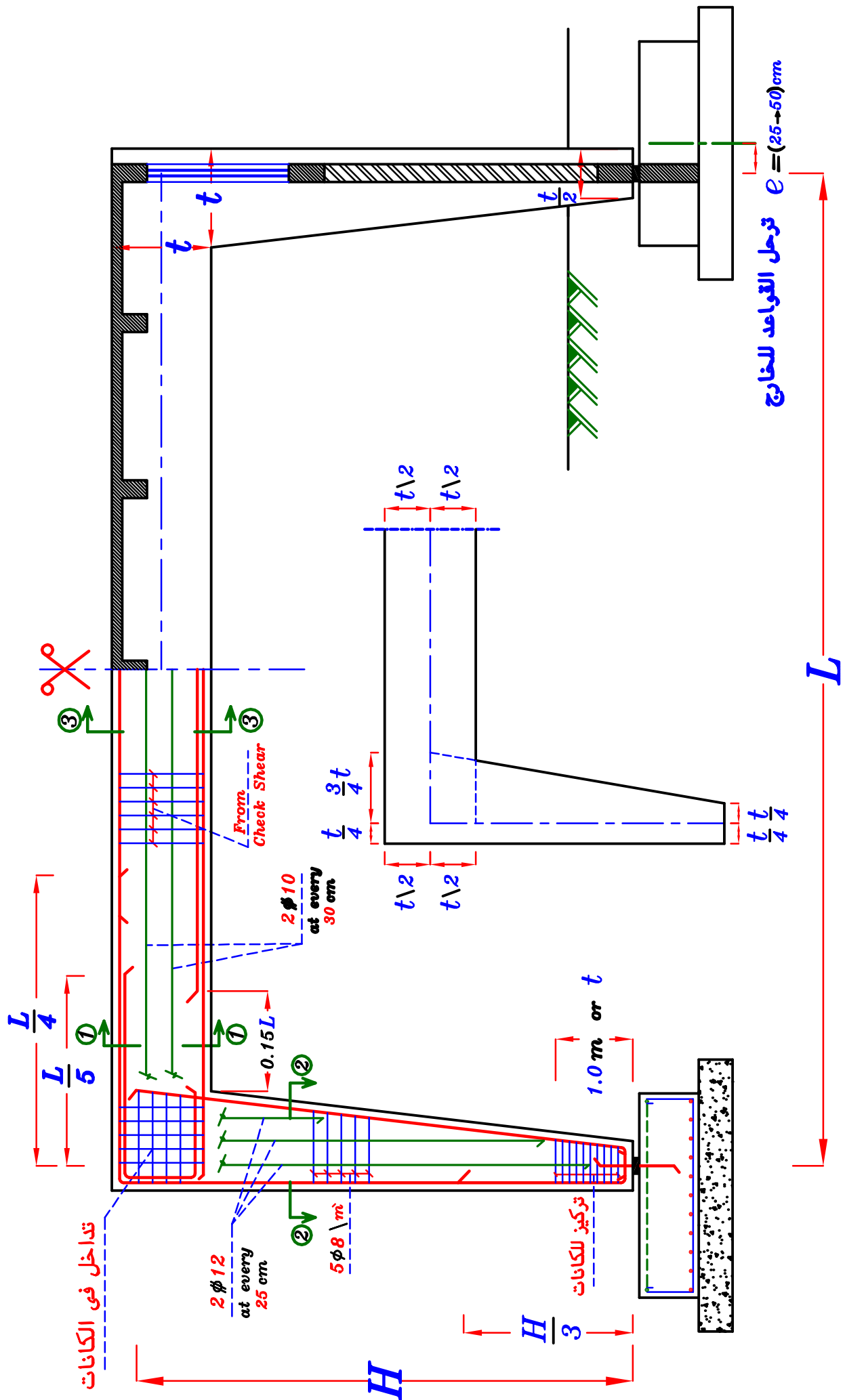
To get the reactions X

Take the moment at Point $a = \text{Zero}$

Then Draw Internal Forces Diagrams.

ملحوظه هامه

هذا الحل حل تقريبي جدا و غير دقيق ، لذا لن نستخدم هذا الحل
الا مع تعذر الوقت في الامتحان



Stirrup Hangers
(0.1 → 0.2) A_s

$A_{s1} - A_{s2}$

A_{s2}

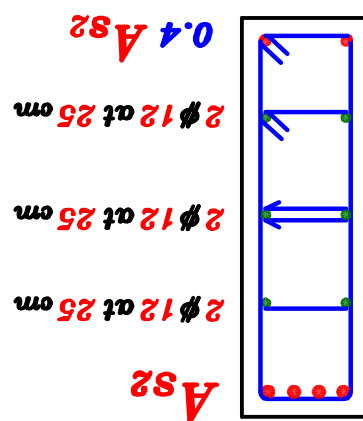
$\frac{1}{2} A_{s2}$

$\frac{1}{2} A_{s2}$

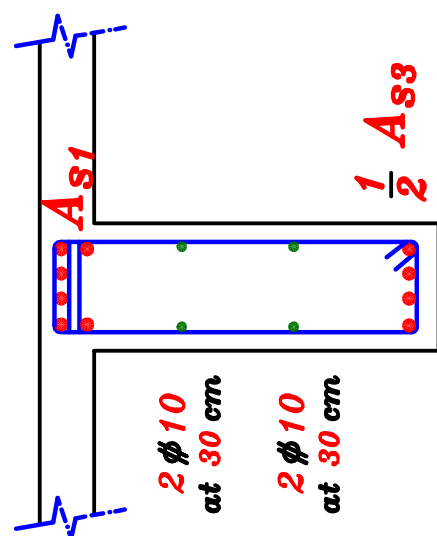
$\frac{1}{2} A_{s3}$

$\frac{1}{2} A_{s3}$

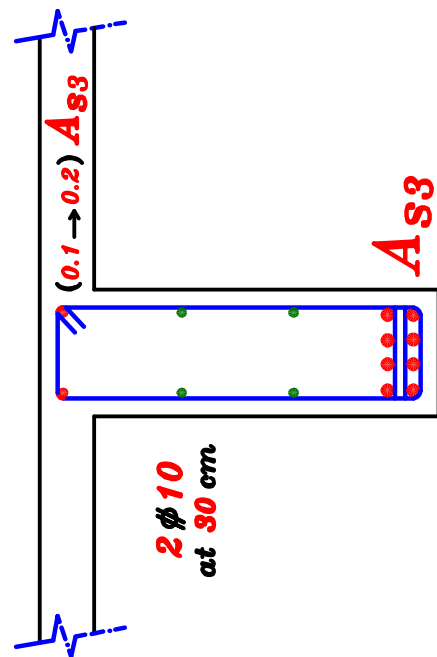
Stirrup Hangers $\approx 0.4 A_{s2}$



Sec. (2-2)

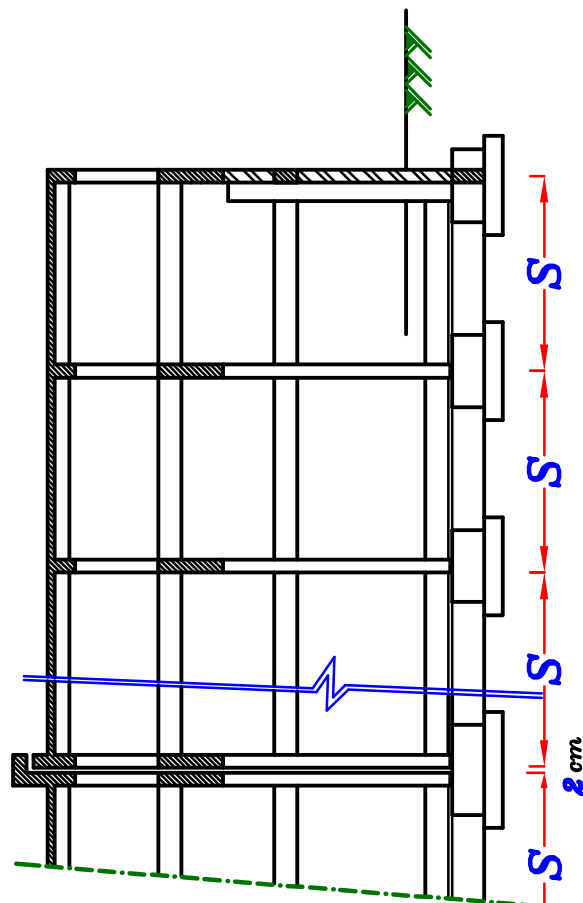
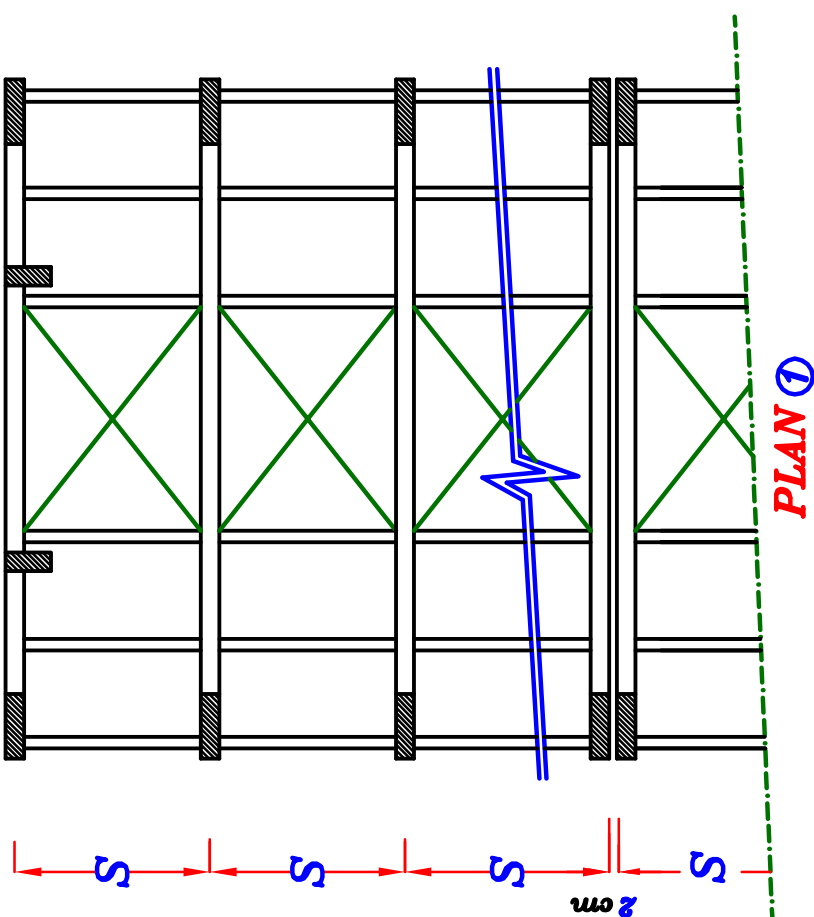
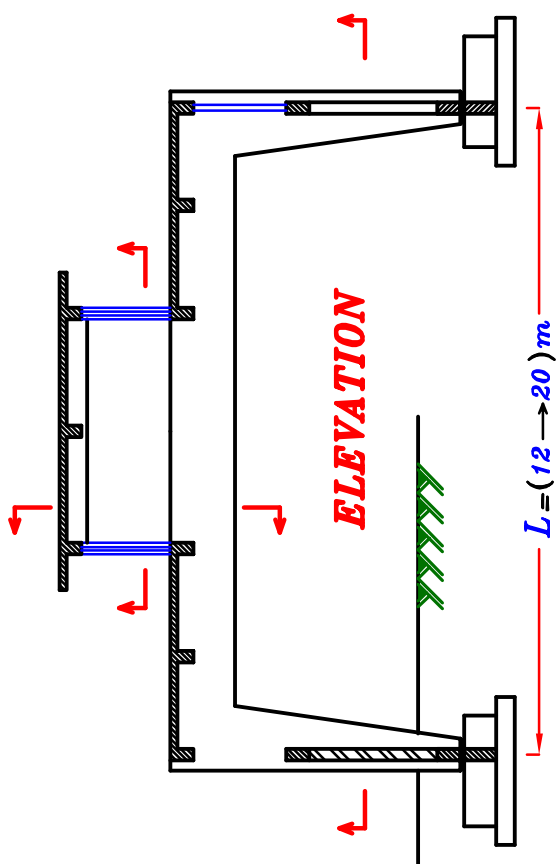


Sec. (1-1)

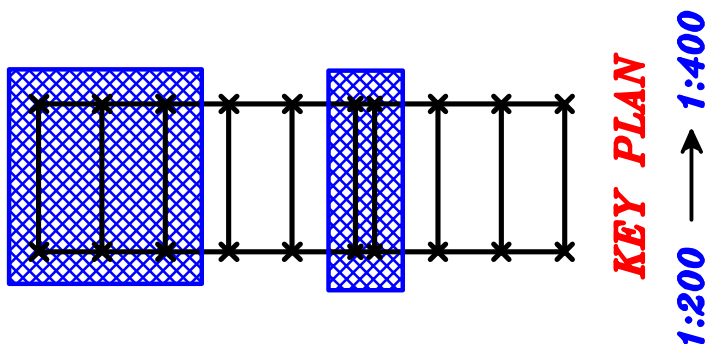
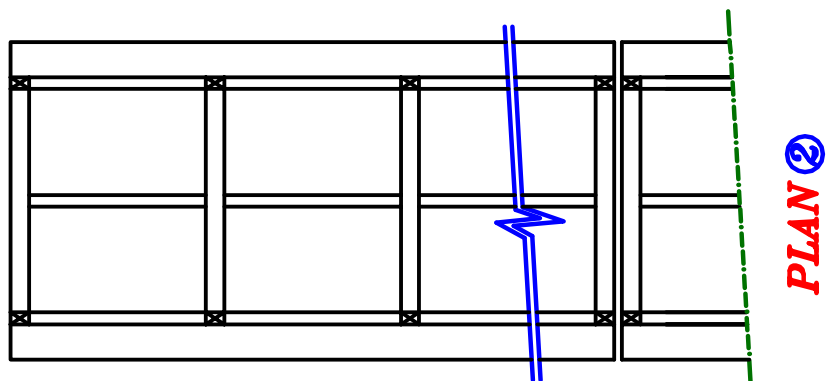


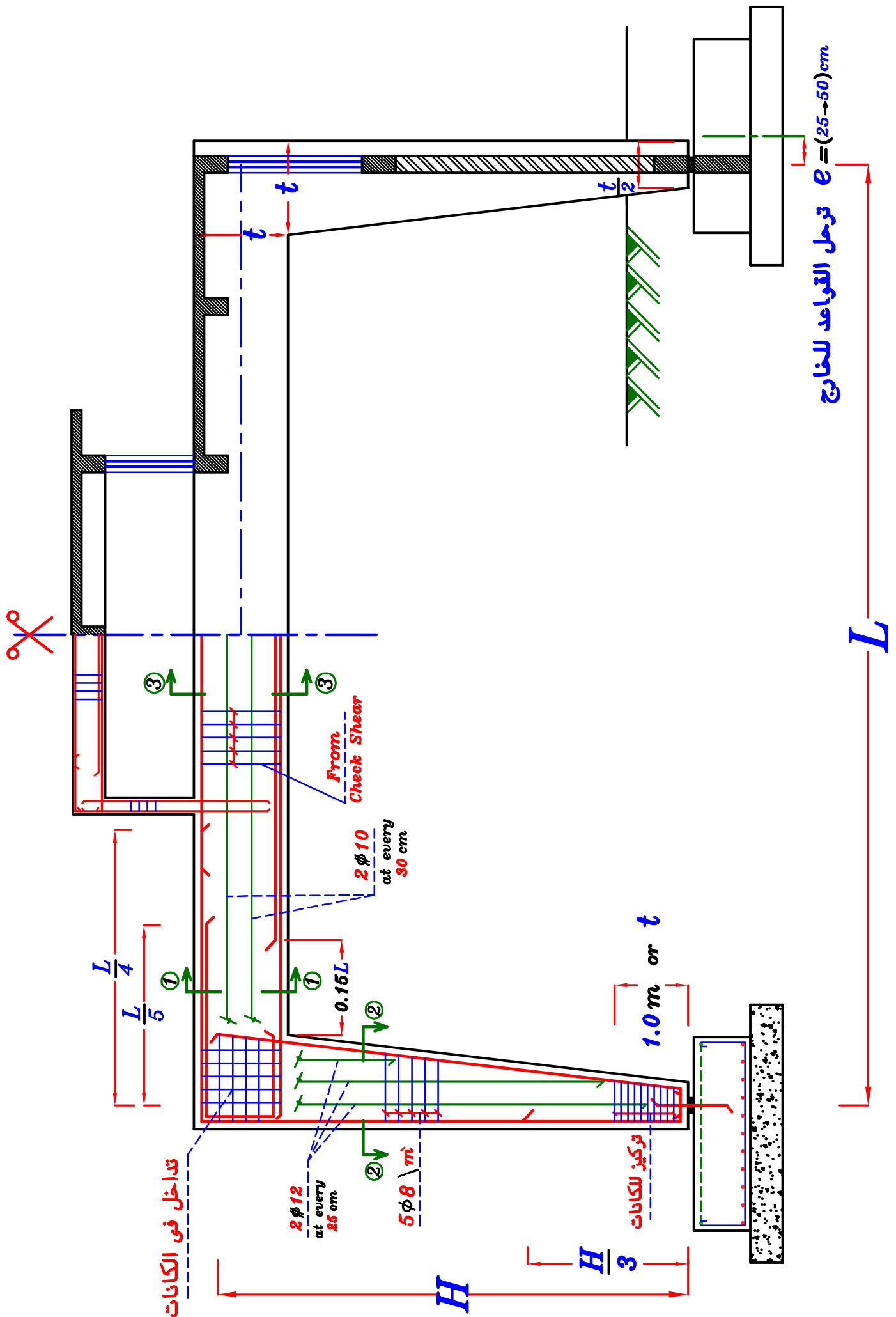
Sec. (3-3)

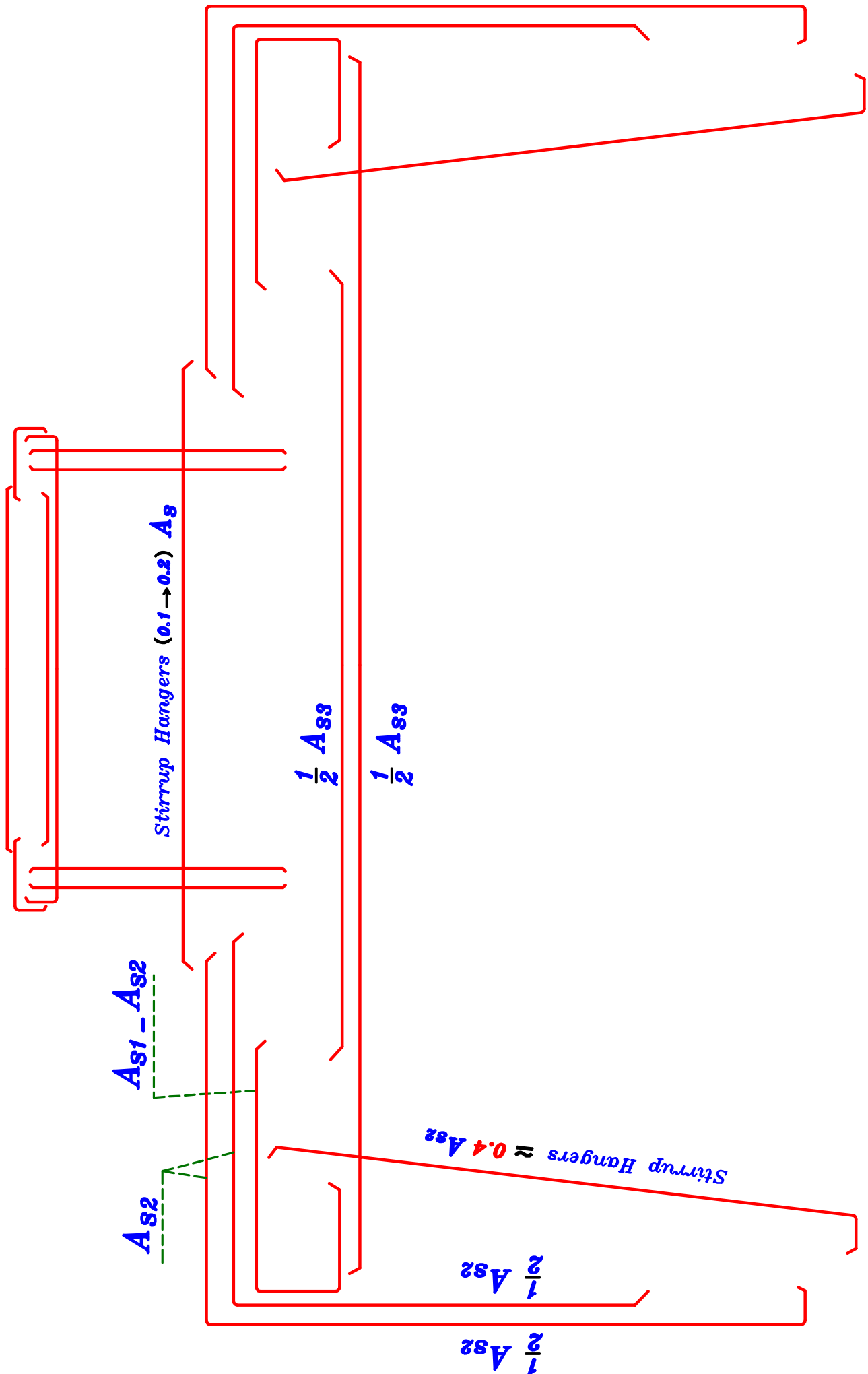
2 Hinged Frame with Sky Light.



SIDE VIEW







Example.

$$F_{cu} = 25 \text{ N/mm}^2 \quad F_y = 360 \text{ N/mm}^2$$

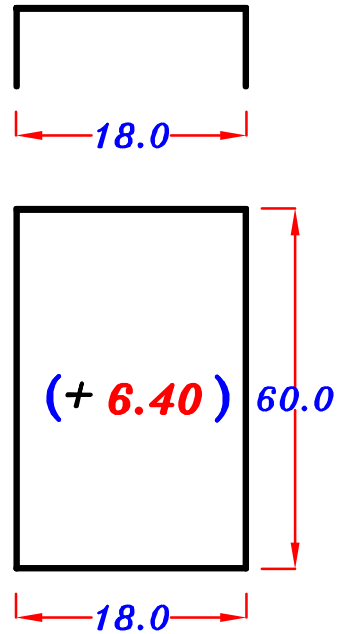
$$L.L. = 1.0 \text{ kN/m}^2 \quad F.C. = 2.0 \text{ kN/m}^2$$

$$\text{Slab Level} = (+ 6.40) \text{ m}$$

$$\text{Foundation Level} = - 2.5 \text{ m}$$

$$\text{Window height} = 1.5 \text{ m}$$

$$\text{Spacing} = 6.5 \text{ m}$$

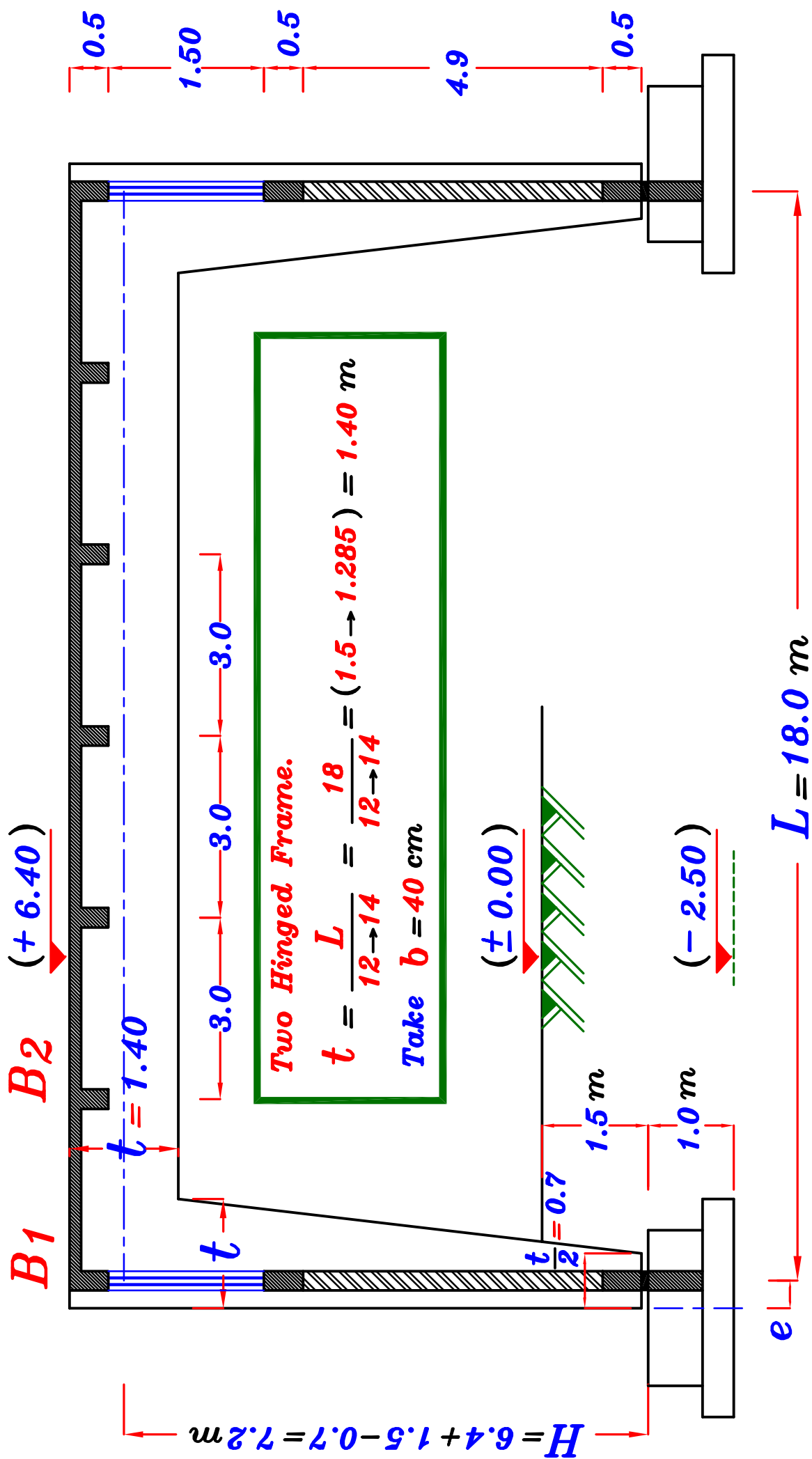


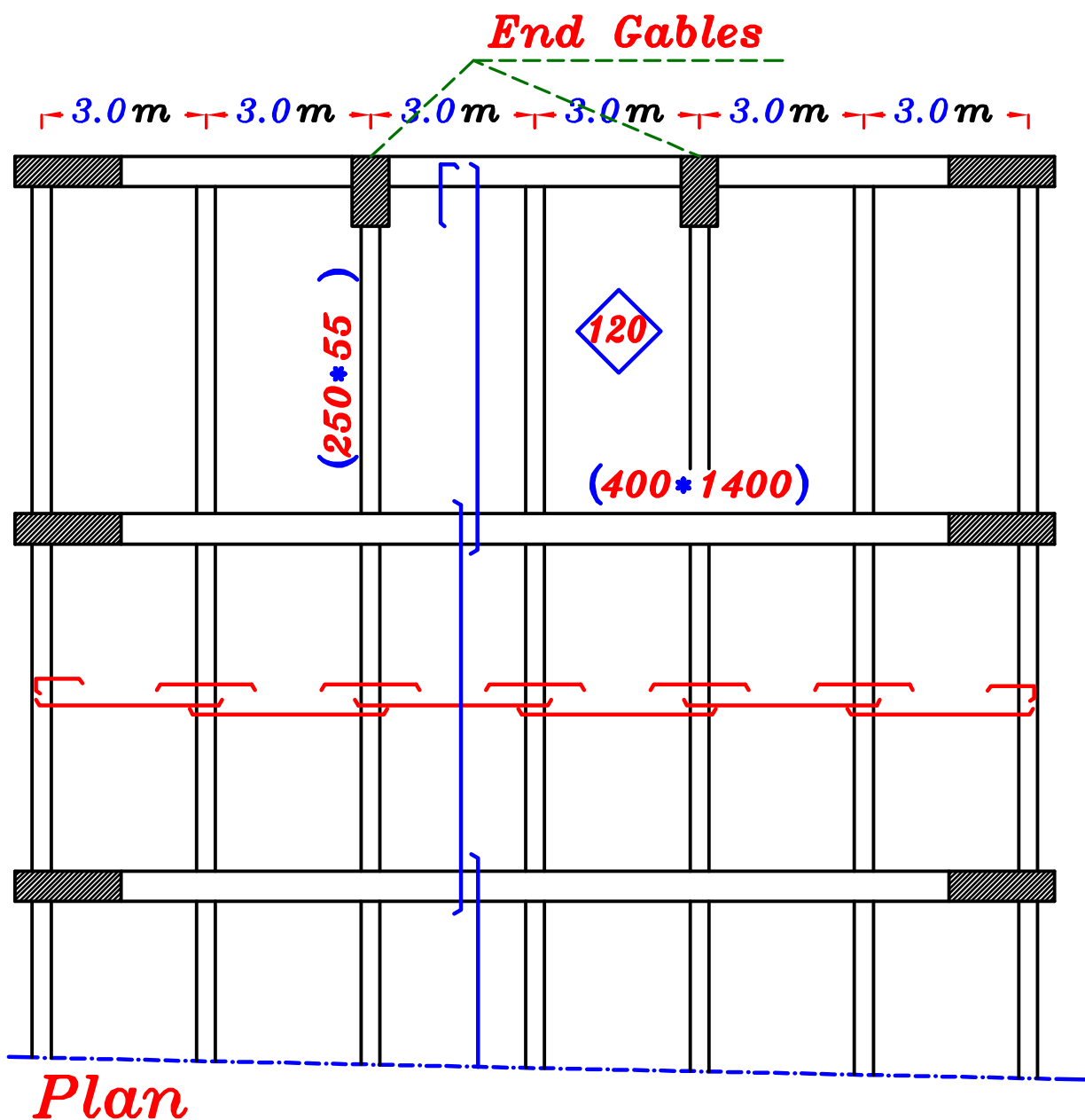
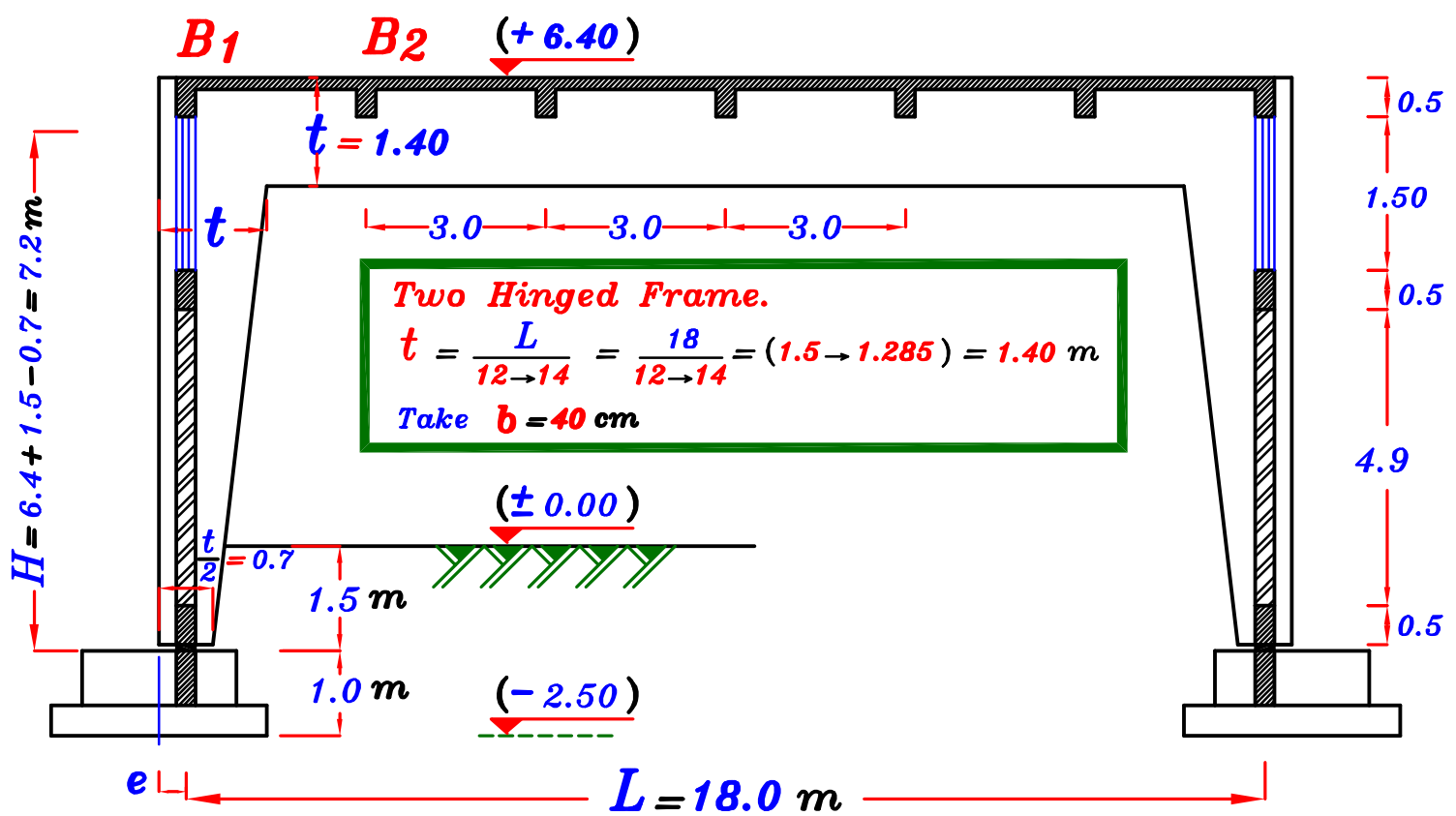
Req.

- 1- Choose a suitable system to cover this area & draw concrete dimensions in elevation For the main supporting element.
- 2- Design the main supporting element & draw its details of RFT.

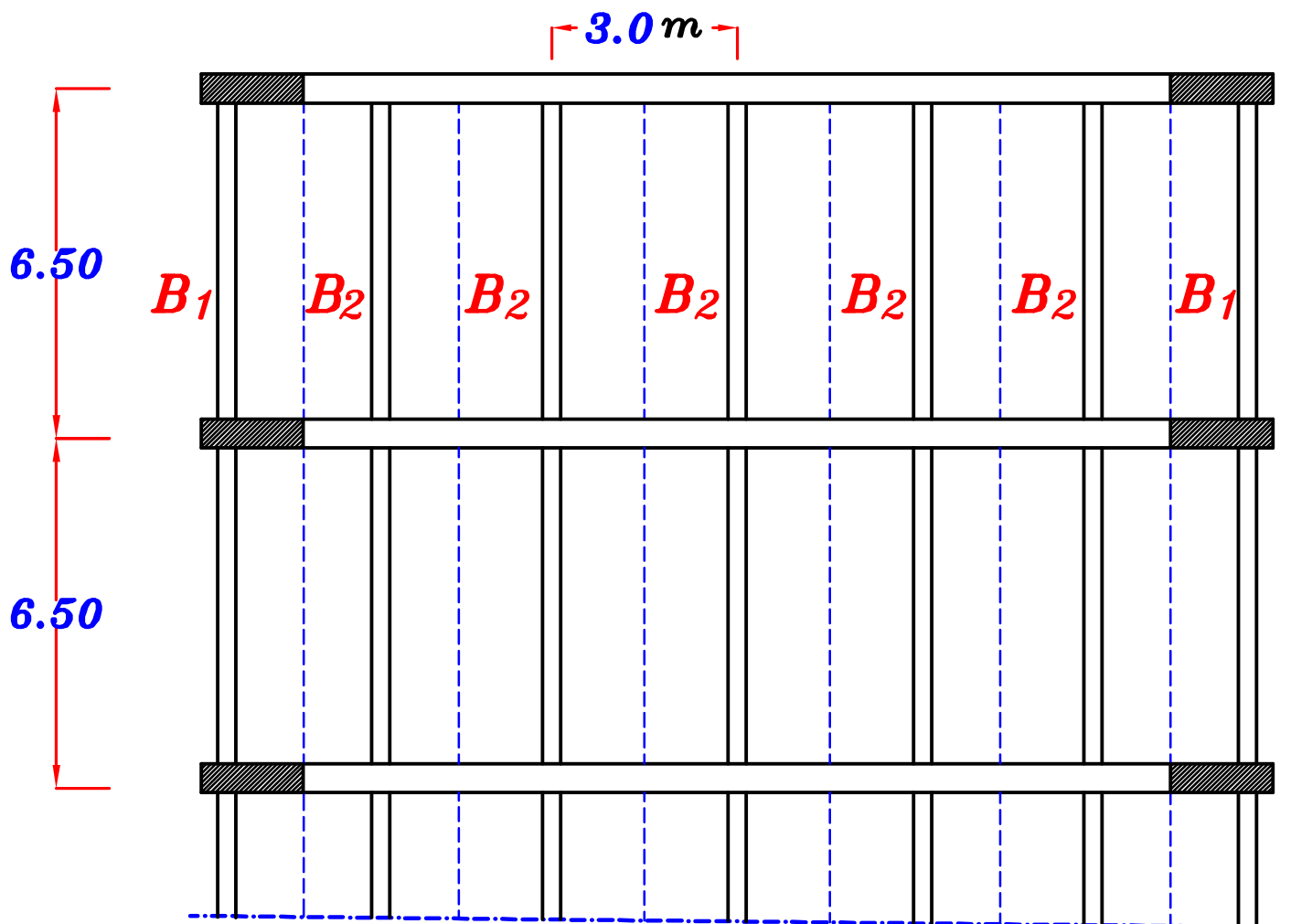
خطوات المسألة

- ١ - اختيار ال *system*
- ٢ - رسم *concrete Dim.* في ال *elevation & Plan*
- ٣ - رسم تسليح البلاطة على نفس ال *Plan*
- ٤ - عمل *Load distribution* للبلاطات و حساب الاحمال على ال *System*
- ٥ - حل ال *System* و رسم *B.M.D. & N.F.D.*
- ٦ - تصميم مقاطعات ال *System* على *M, N*
- ٧ - رسم تسليح ال *System* في ال *elevation & cross-sec.*





Load Distribution on Beams.



One way Slab $t_s = \frac{300}{30} = 100 \text{ mm}$ Take $t_s = 120 \text{ mm}$

$$w_s = 1.4 (0.12 * 25 + 2.0) + 1.6 (1.0) = 8.60 \text{ kN/m}^2$$

B₁

Take o.w.(U.L.) = $3.0 * 1.4 = 4.20 \text{ kN/m}$

$$w_a = \text{o.w.} + w_s \frac{L_s}{2} = 4.20 + (8.60) \left(\frac{3}{2}\right) = 17.1 \text{ kN/m}$$

$$R_1 = 17.1 * 6.5 = 111.15 \text{ kN}$$

B₂

$$w_a = \text{o.w.} + 2w_s \frac{L_s}{2} = 4.20 + 2(8.60) \left(\frac{3}{2}\right) = 30.0 \text{ kN/m}$$

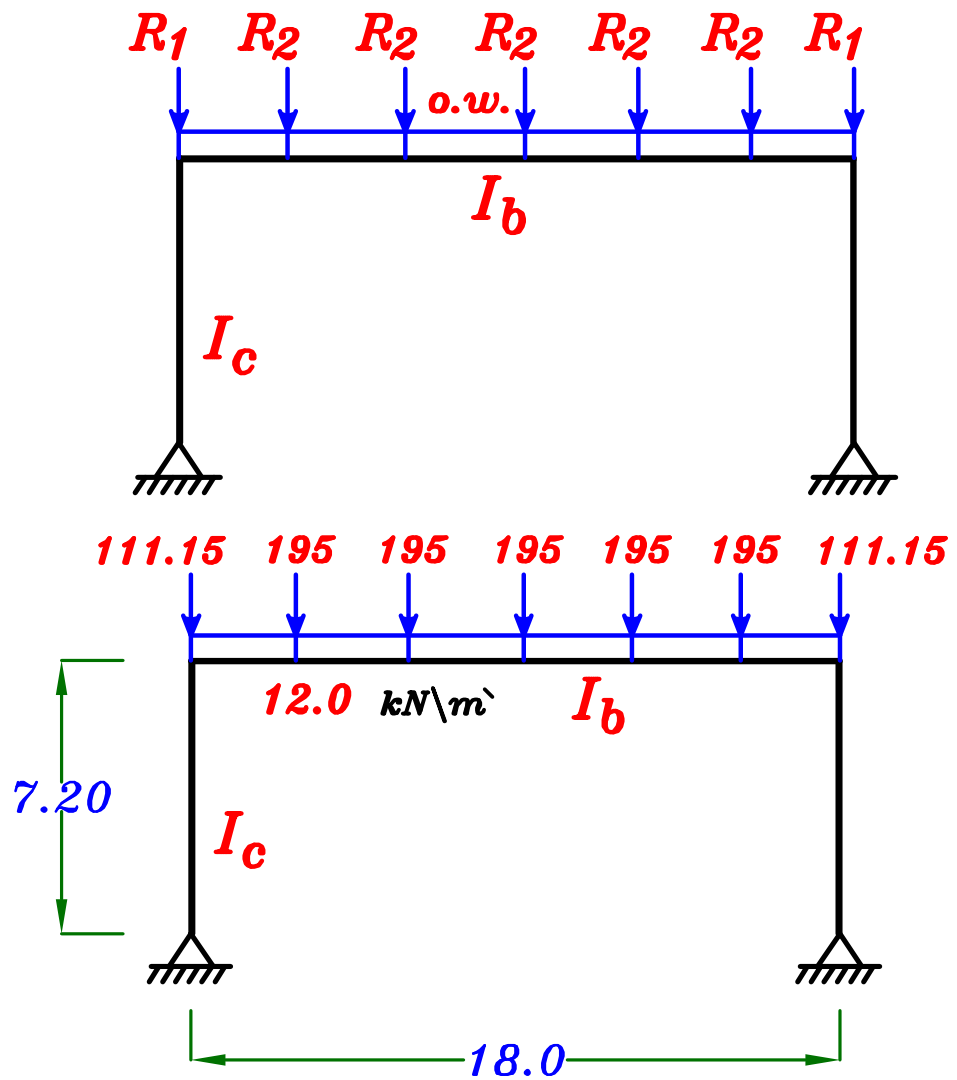
$$R_2 = 30.0 * 6.5 = 195.0 \text{ kN}$$

Loads on Frame.

Take

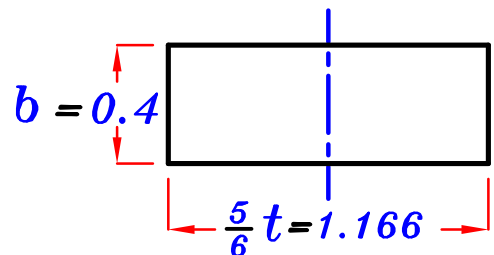
o.w. (U.L.)

$$= 12.0 \text{ kN/m}$$



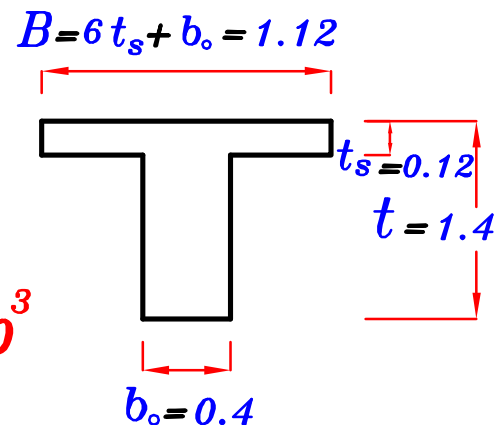
I_c

$$I_c = \frac{b \left(\frac{5}{6} t \right)^3}{12} = \frac{0.4 \left(\frac{5}{6} * 1.40 \right)^3}{12} = 0.05293 \text{ m}^4$$



$$\left. \begin{aligned} \frac{t_s}{t} &= \frac{0.12}{1.40} = 0.085 \\ \frac{b_o}{B} &= \frac{0.40}{1.12} = 0.36 \end{aligned} \right\} \text{From Tables page 91} \quad \mu = 398$$

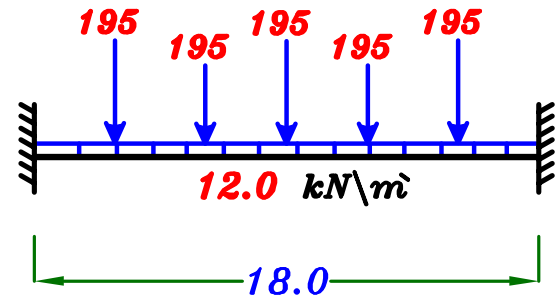
$$I_b = (\mu * 10^{-4}) B t^3 = 398 * 10^{-4} * 1.12 * 1.40^3 = 0.1223 \text{ m}^4$$



Using Moment Distribution.

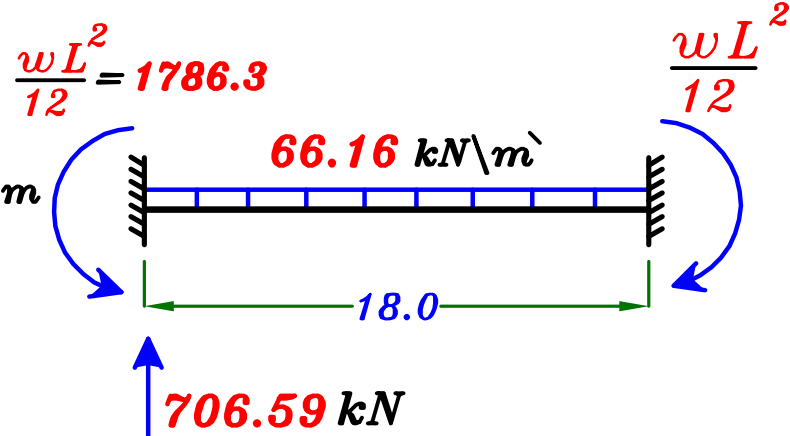
$$w = o.w. + \frac{\sum P}{\text{span}}$$

$$= 12.0 + \frac{5(195)}{18} = 66.16 \text{ kN/m}$$



F.E.M.

$$\frac{wL^2}{12} = \frac{66.16 * (18.0)^2}{12} = 1786.3 \text{ kN.m}$$



D.F.

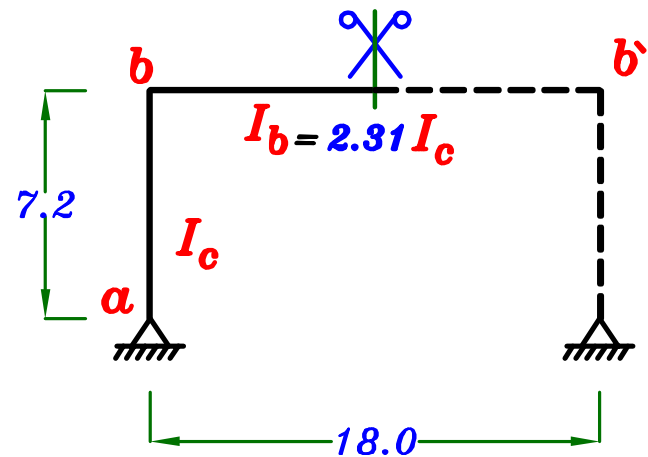
For Joint b

$$K_c = \frac{3}{4} \frac{I_c}{h} = \frac{3}{4} * \frac{I_c}{7.20} = 0.104 I_c$$

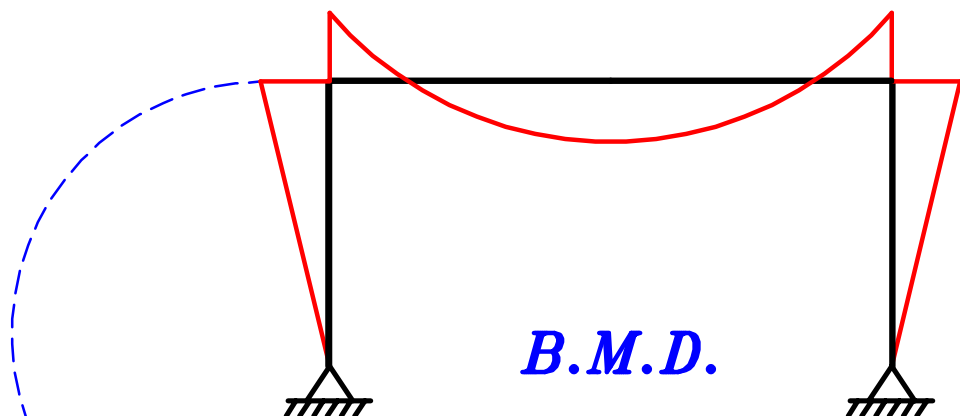
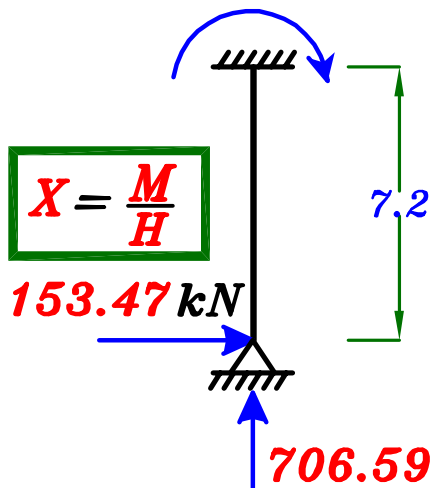
$$K_b = \frac{1}{2} \frac{I_b}{L} = \frac{1}{2} * \frac{(2.31)I_c}{18.0} = 0.0641 I_c$$

$$D.F._c = \frac{0.104}{0.104 + 0.0641} = 0.6186$$

$$D.F._b = 1 - 0.6186 = 0.3814$$

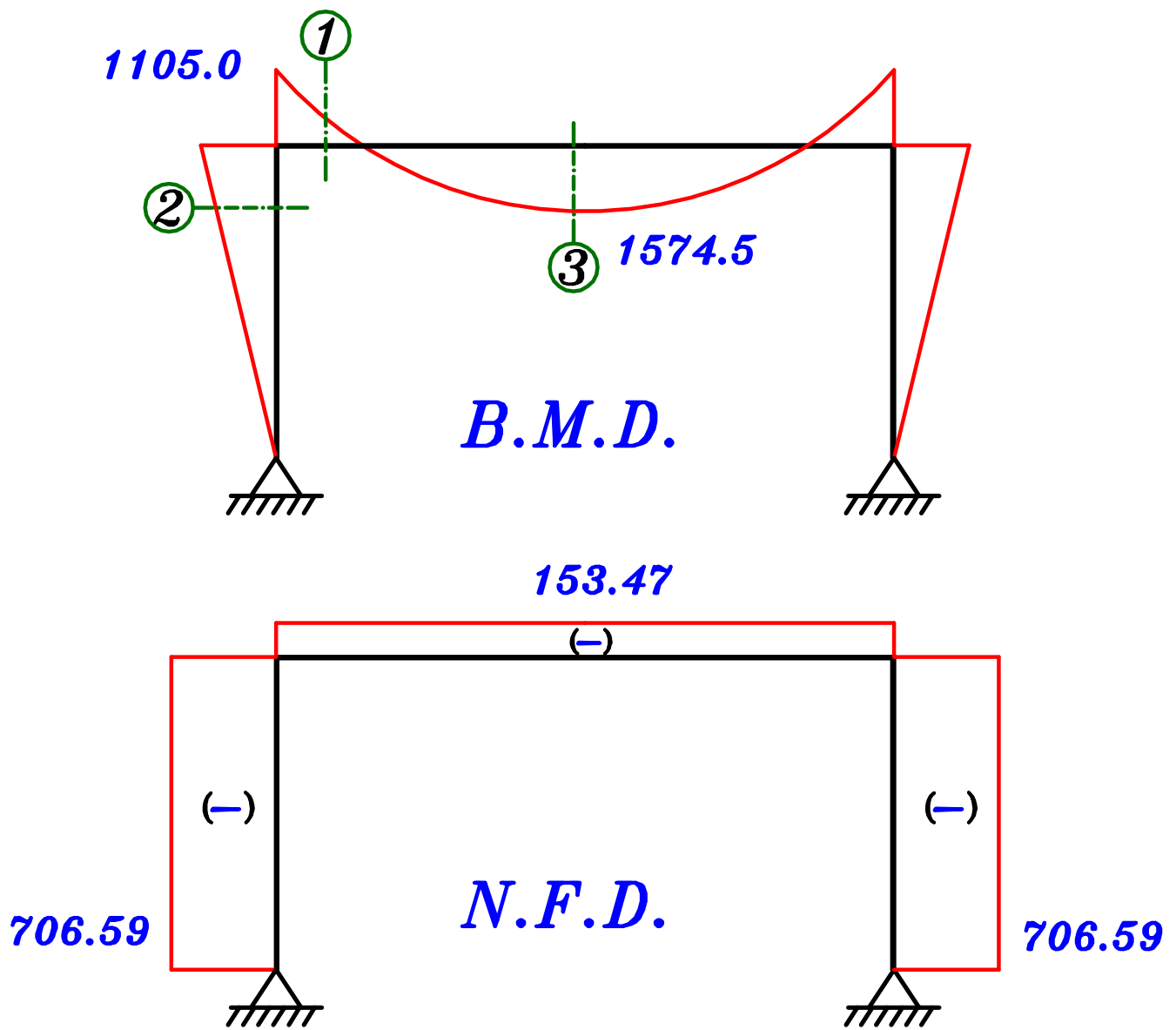


1105.0 kN.m



$$F.E.M. (Beam) * D.F. (Col.)$$

$$1786.3 * 0.6186 = 1105.0$$



Design of Sections.

Sec. ① R-Sec.

$$M = 1105.0 \text{ kN.m} , P = 153.47 \text{ kN} , b = 400 \text{ mm} , t = 1400 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{153.47 \cdot 10^3}{25 \cdot 400 \cdot 1400} = 0.0109 < 0.04 \text{ (neglect } P \text{)}$$

$$\therefore 1300 = C_1 \sqrt{\frac{1105.0 \cdot 10^6}{25 \cdot 400}} \rightarrow C_1 = 3.91 \rightarrow J = 0.80$$

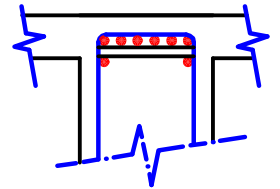
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1105.0 \cdot 10^6}{0.80 \cdot 360 \cdot 1300} = 2951.4 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2951.4 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1300 = 1625 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2951.4 \text{ mm}^2$ **8 ϕ 22**

$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{22 + 25} = 7.97 = 7.0 \text{ bars}$



Sec. ② R-Sec. Neglect Effect of Buckling.

$M = 1105.0 \text{ kN.m}$, $P = 706.59 \text{ kN}$

Check $\frac{P}{F_{cu} b t} = \frac{706.59 * 10^3}{25 * 400 * 1400} = 0.0504 > 0.04$ (Don't neglect P)

$e = \frac{M}{P} = \frac{1105.0}{706.59} = 1.563 \text{ m}$ $\therefore \frac{e}{t} = \frac{1.563}{1.40} = 1.116 > 0.5 \xrightarrow{\text{use}} e_s$

$e_s = e + \frac{t}{2} - c = 1.563 + \frac{1.4}{2} - 0.1 = 2.163 \text{ m}$

$M_s = P * e_s = 706.59 * 2.163 = 1528.35 \text{ kN.m}$

$\therefore 1300 = C_1 \sqrt{\frac{1528.35 * 10^6}{25 * 400}} \rightarrow C_1 = 3.32 \rightarrow J = 0.769$

$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \phi_s)} = \frac{1528.35 * 10^6}{0.769 * 360 * 1300} - \frac{706.59 * 10^3}{(360 \setminus 1.15)}$
 $= 1989.5 \text{ mm}^2$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1989.5 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1300 = 1625 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 1989.5 \text{ mm}^2$ **6 ϕ 22**

Sec. ③ T-Sec.

$$M = 1574.5 \text{ kN.m}, P = 153.47 \text{ kN}, b = 400 \text{ mm}, t = 1400 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{153.47 * 10^3}{25 * 400 * 1400} = 0.011 < 0.04 \text{ (neglect } P \text{)}$$

$$B = \left\{ \begin{array}{l} C.L. - C.L. = \text{Spacing} = 6.5 \text{ m} = 6500 \text{ mm} \\ 16 t_s + b = 16 * 120 + 400 = 2320 \text{ mm} \\ K \frac{L}{5} + b = 0.7 * \frac{18000}{5} + 400 = 2920 \text{ mm} \end{array} \right\} \boxed{B = 2320 \text{ mm}}$$

$$\therefore 1300 = C_1 \sqrt{\frac{1574.5 * 10^6}{25 * 2320}} \rightarrow C_1 = 7.89 \rightarrow J = 0.826$$

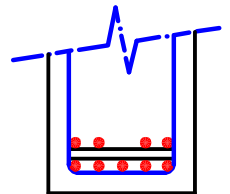
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1574.5 * 10^6}{0.826 * 360 * 1300} = 4073.0 \text{ mm}^2$$

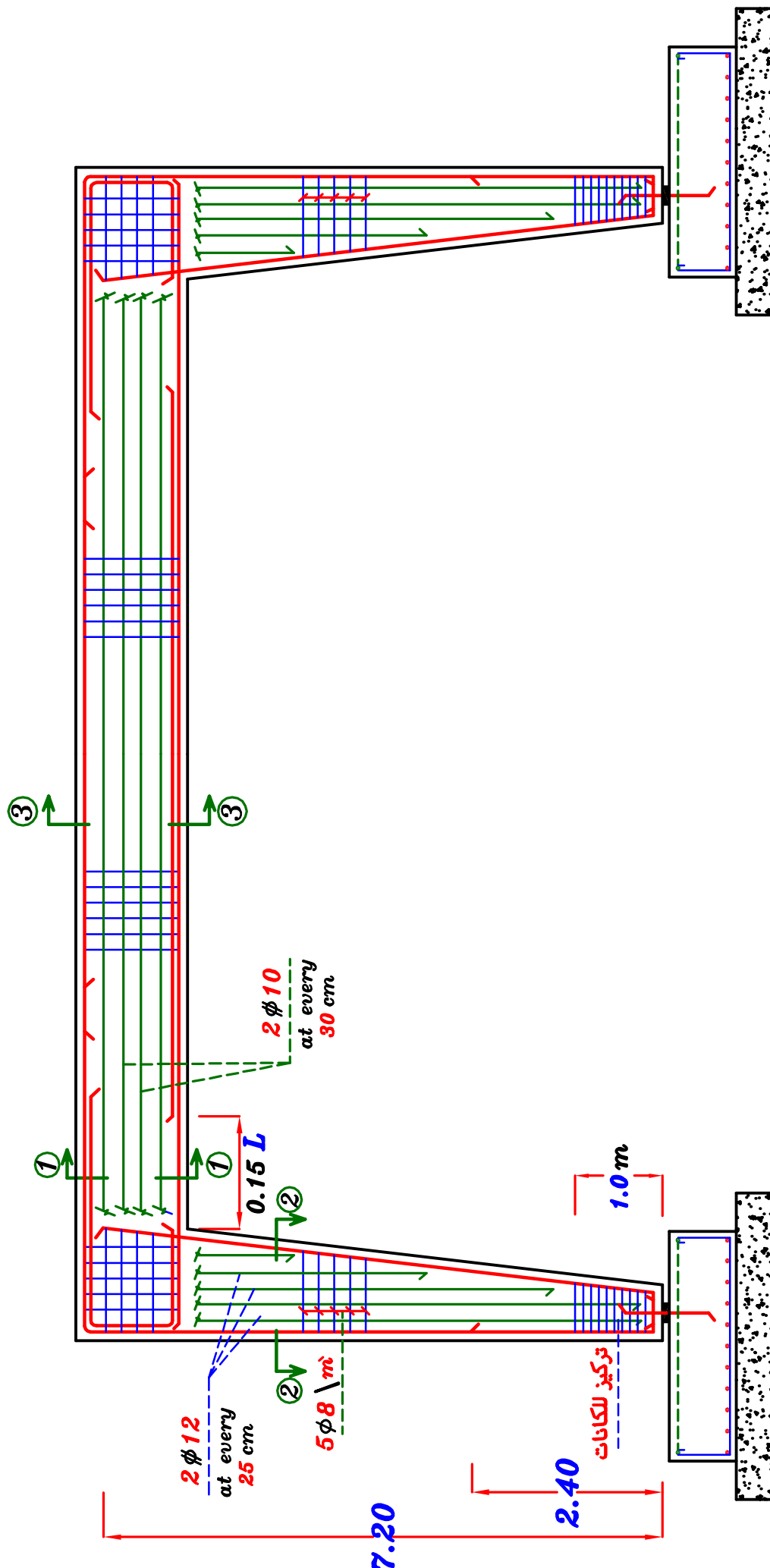
$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 4073.0 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1300 = 1625 \text{ mm}^2$$

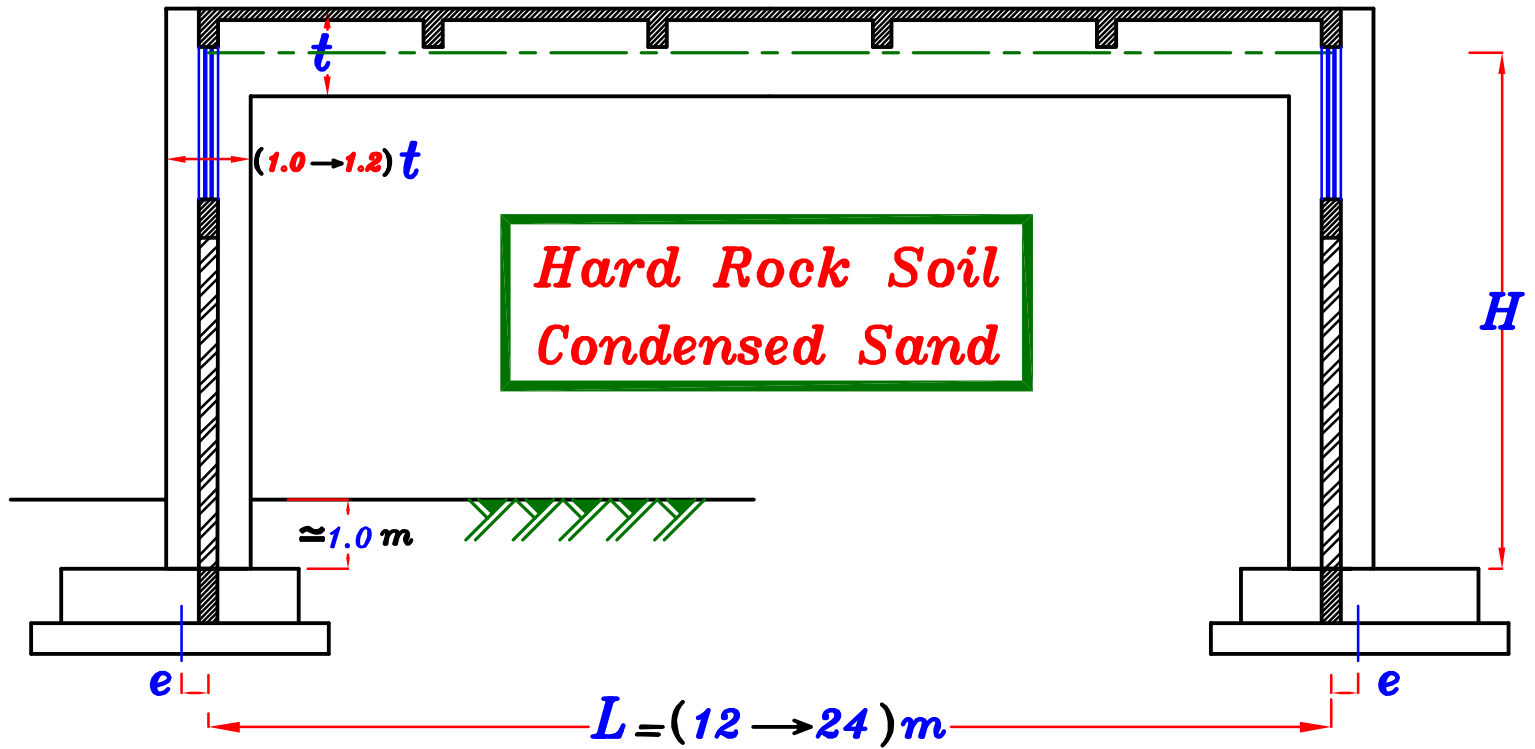
$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 4073.0 \text{ mm}^2 \quad \textcircled{9\phi 25}$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$





Fixed Straight Frame.



– Statical System

The Fixed Frame is Two Times Statically indet. symmetric لانه



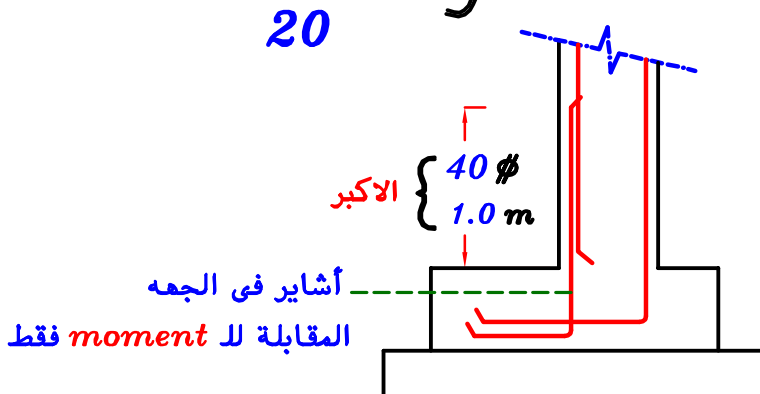
– Concrete Dimensions.

* $Span (L) = (12 \rightarrow 24) m$

* $t \approx \frac{L}{14 \rightarrow 16}$

* $b = 0.30 m$

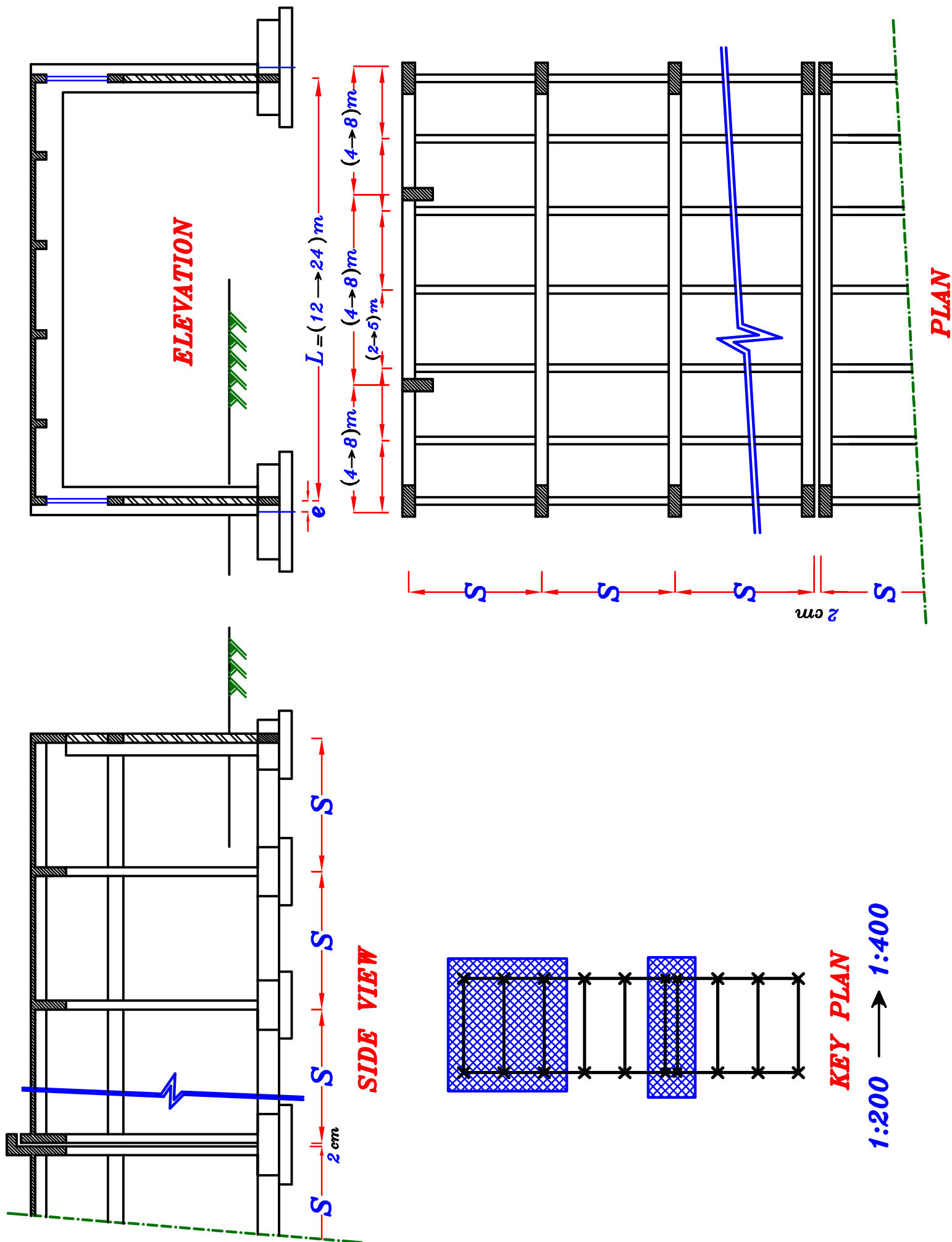
$\left. \begin{array}{l} \text{Spacing} \\ 20 \end{array} \right\} \text{الأكبر}$

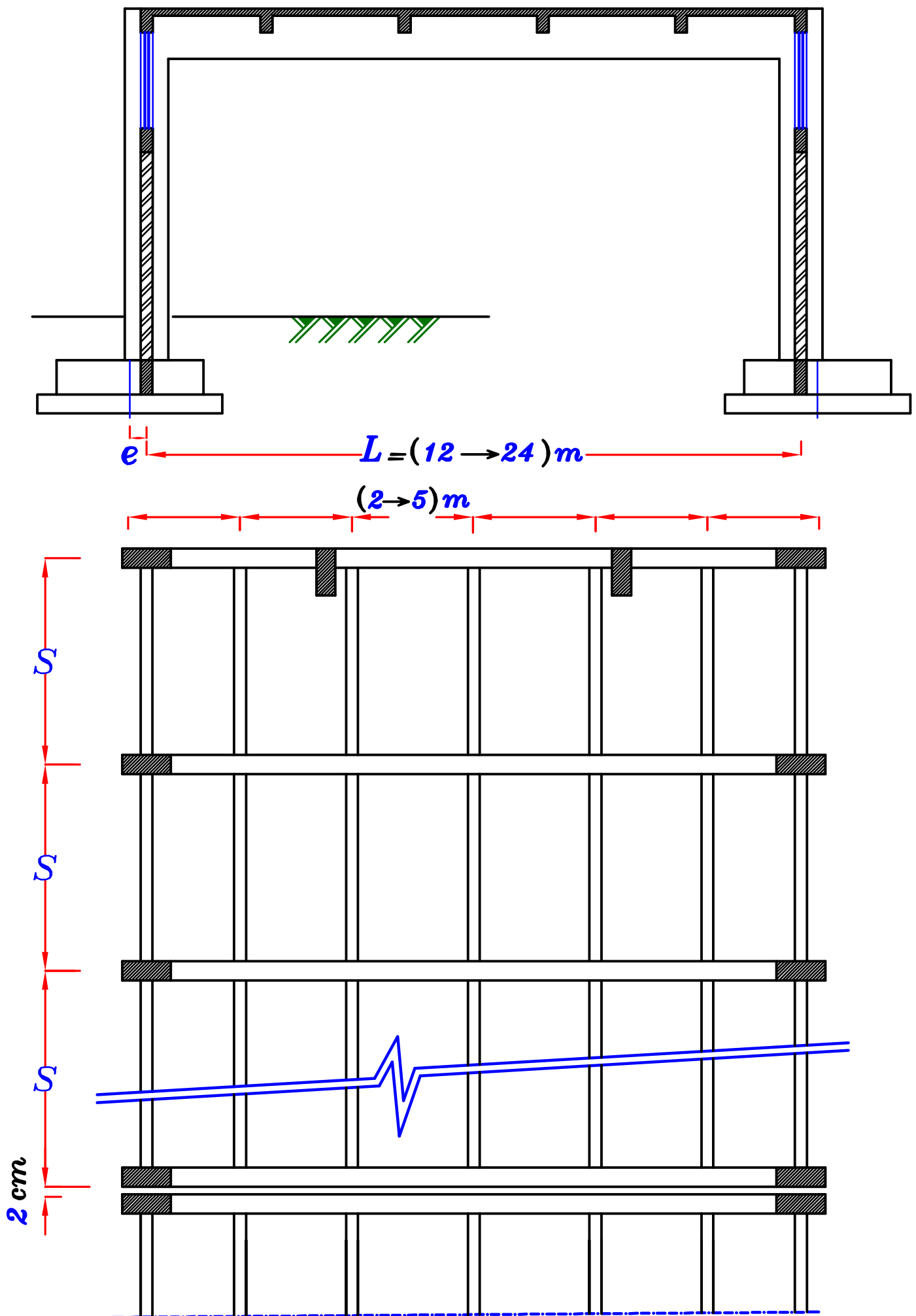


ترحل القواعد عكس إتجاه ال (M)

ترحل القواعد للخارج مسافة (e)

لعمل $uniform stress$ على التربة





PLAN

Steps of Design.

خطوات المسألة .

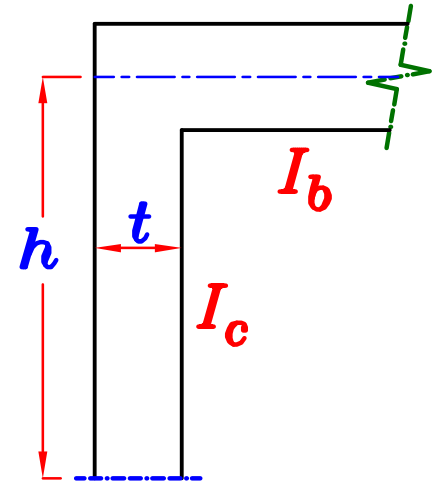
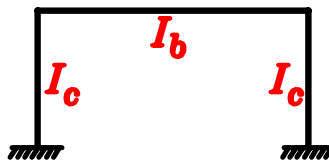
- ١- اختيار ال *system*
- ٢- رسم *concrete Dim.* في ال *elevation & Plan*
- ٣- رسم تسليح البلاطة على نفس ال *Plan*
- ٤- عمل *Load distribution* للبلاطات و حساب الاحمال على ال *System*
- ٥- حل ال *System* و رسم *B.M.D. & N.F.D.*
- ٦- تصميم مقاطعات ال *System* على *M,N*
- ٧- رسم تسليح ال *System* في ال *elevation & cross-sec.*

Moment Distribution Method.

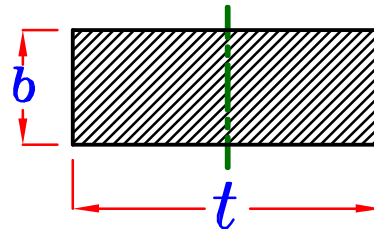
- Ⓐ Get Moment of Inertia For all members. (*I*)
- Ⓑ Get Distribution Factors at all Joints. (*D.F.*)
- Ⓒ Get Fixed End Moments For Beams. (*F.E.M.*)
- Ⓓ Get the Final Moment. (*M_F*)
- Ⓔ Get *B.M.D.* , *N.F.D.* , *N.F.D.*

1 – Calculate Moment of Inertia For members.

* **For Column.**

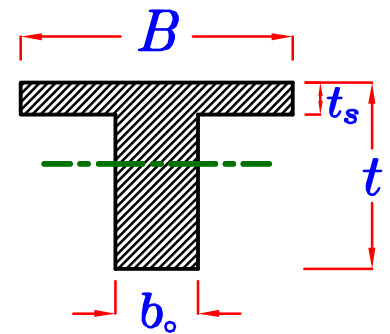


$$I_c = \frac{b(t)^3}{12}$$



* **For Beams.**

$$I_b = (\mu * 10^{-4}) B t^3$$



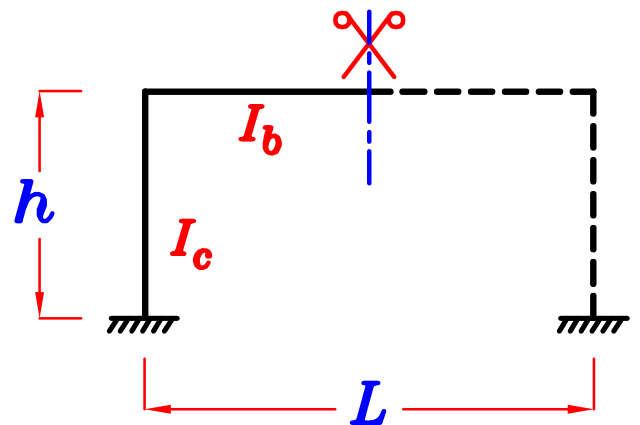
2 – Get the Distribution Factor.

$$K_b = \frac{1}{2} \frac{I_b}{L}$$

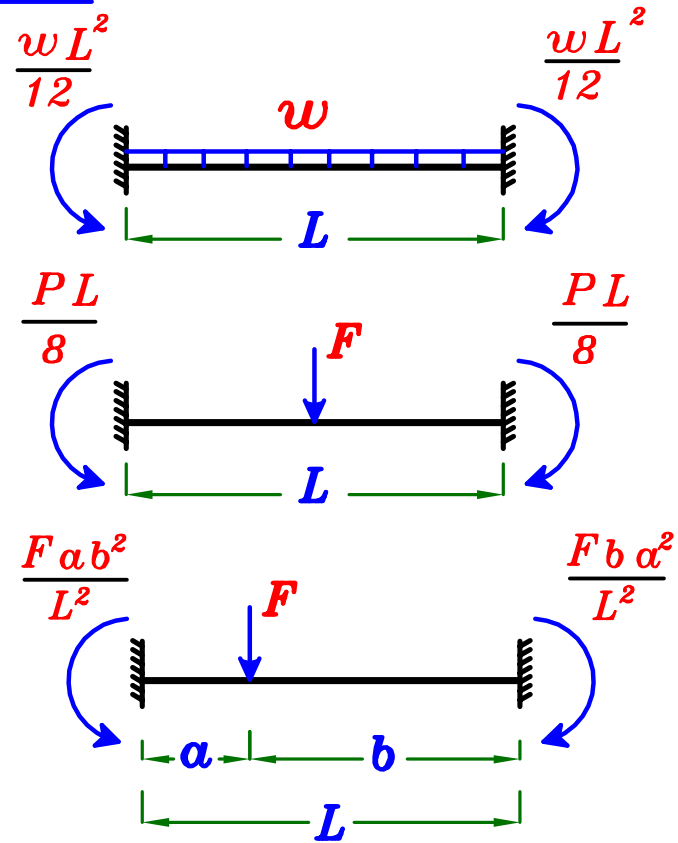
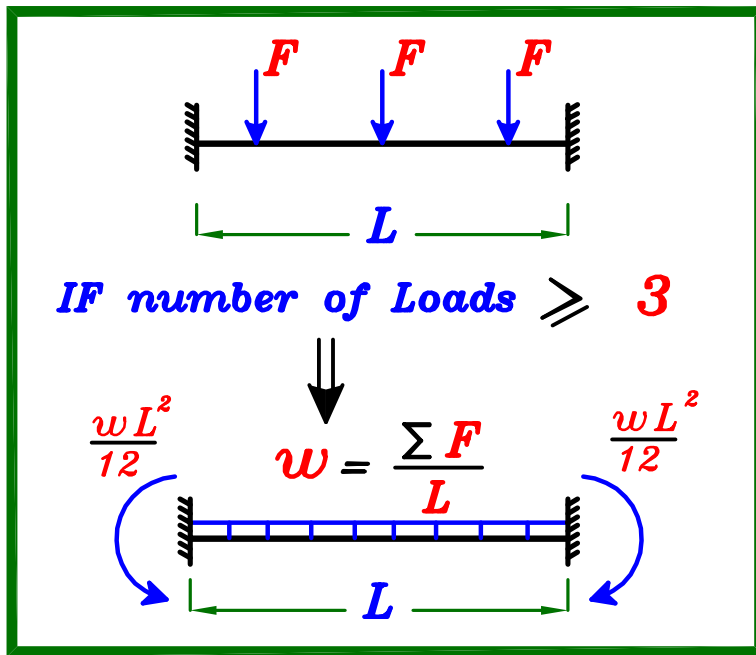
$$K_c = \frac{I_c}{h}$$

$$D.F._c = \frac{K_c}{K_b + K_c}$$

$$D.F._b = \frac{K_b}{K_b + K_c}$$

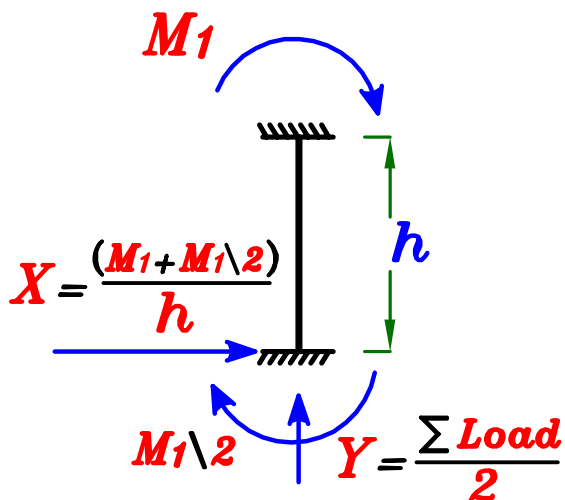
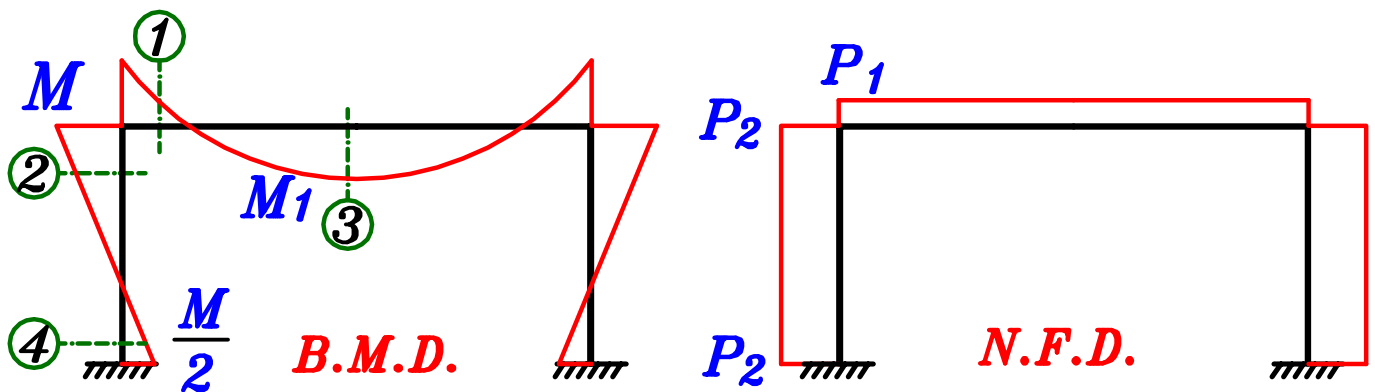


3- Get Fixed End Moment.



4- Calculate the moment.

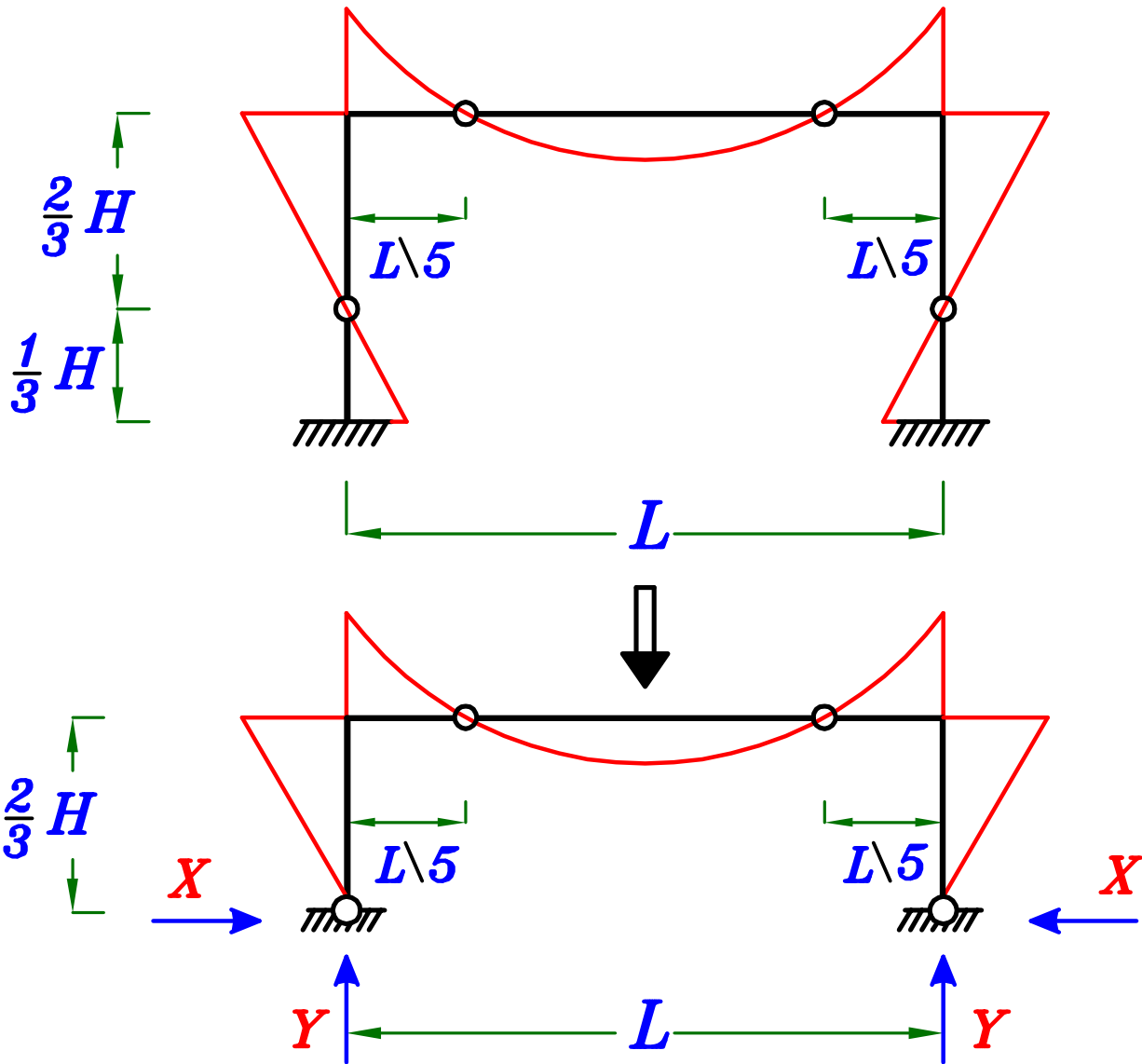
$$M = F.E.M. (Beam) * D.F. (Col.)$$



Design:

- | | | | | |
|--------|----|---------------|---------|--------|
| Sec. ① | on | M | , P_1 | R-Sec. |
| Sec. ② | on | M | , P_2 | R-Sec. |
| Sec. ③ | on | M_1 | , P_1 | T-Sec. |
| Sec. ④ | on | $\frac{M}{2}$ | , P_2 | R-Sec. |

Approximate Solution.



assume that in the column there is an intermediate hinge at $\frac{H}{3}$
 so we can solve the Frame as Two hinged Frame but with height $\frac{2}{3}H$
 assume that in the beam there is an intermediate hinge at $\frac{L}{5}$

$$Y = \frac{\sum \text{Loads}}{2}$$

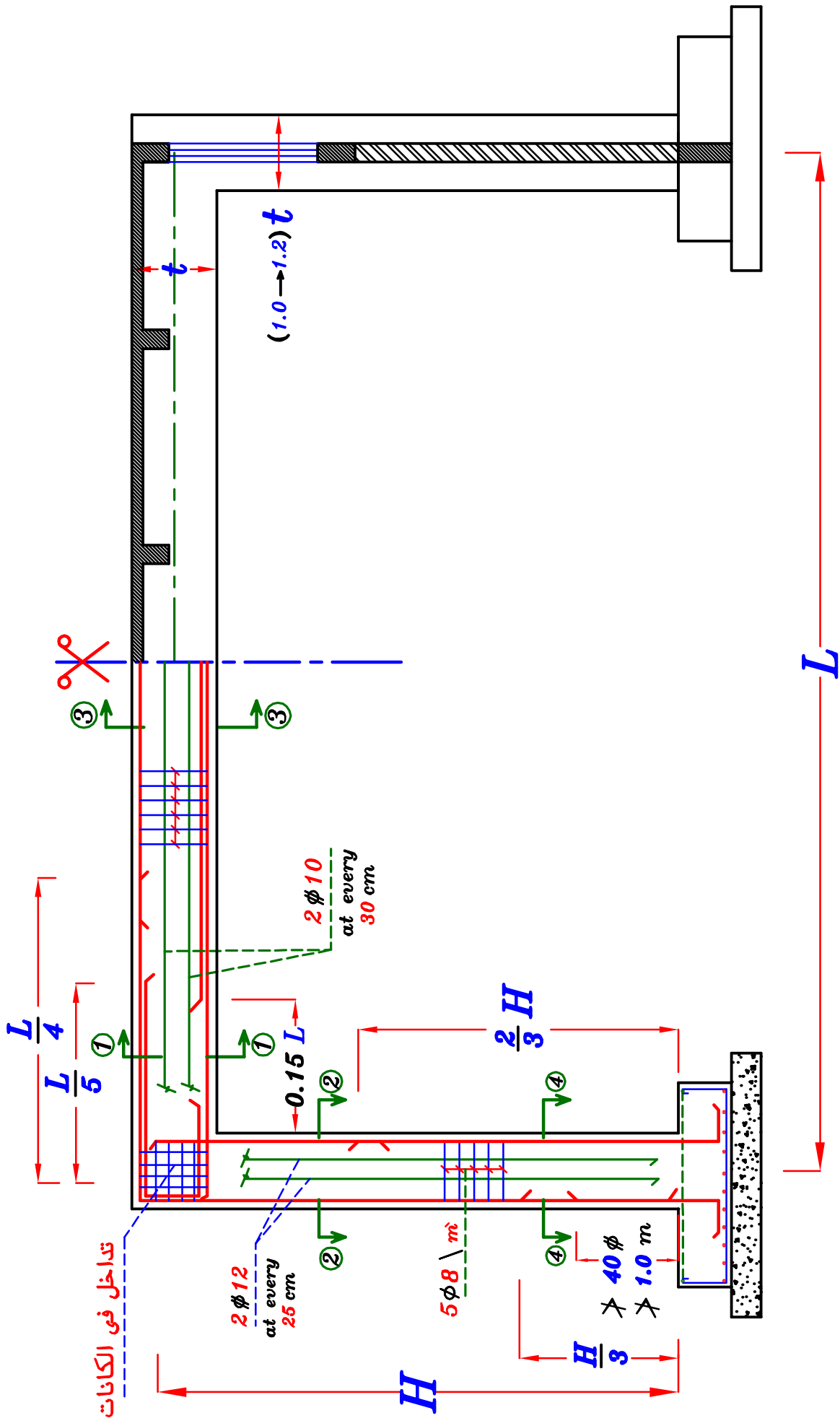
To get the reactions X

Take the moment at Point $a = \text{Zero}$

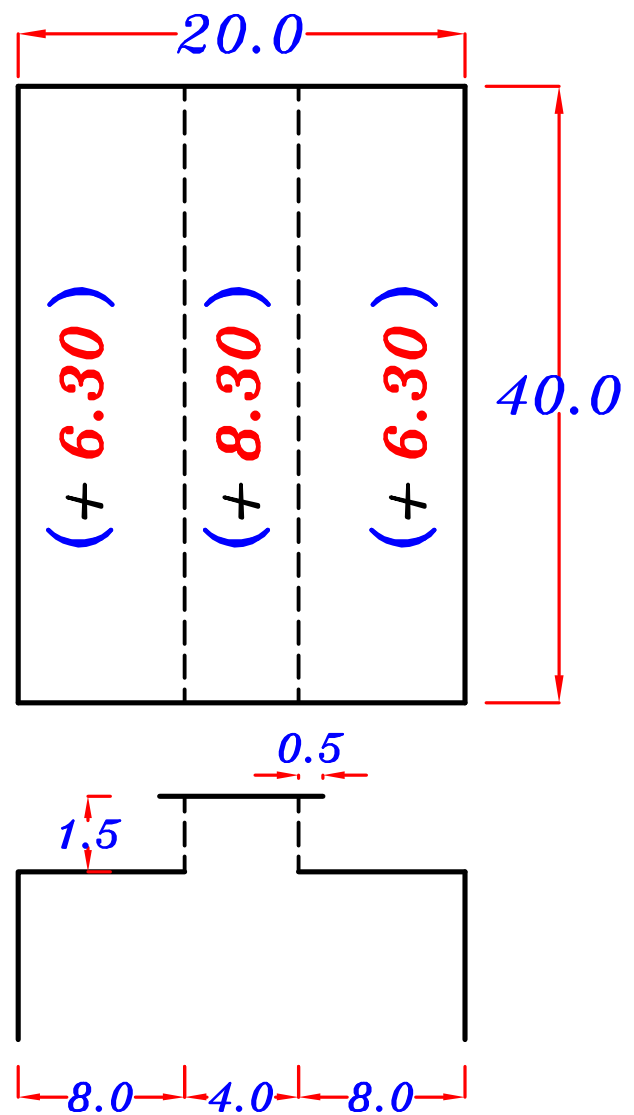
Then Draw Internal Forces Diagrams.

ملحوظة هامة

هذا الحل حل تقريبي جدا و غير دقيق ، لذا لن نستخدم هذا الحل
 الا مع تعذر الوقت في الامتحان



Example.



$$F_{cu.} = 25 \text{ N/mm}^2 \quad F_y = 360 \text{ N/mm}^2$$

$$L.L. = 2.0 \text{ kN/m}^2 \quad F.C. = 1.50 \text{ kN/m}^2$$

$$\text{Foundation Level.} = -2.0 \text{ m}$$

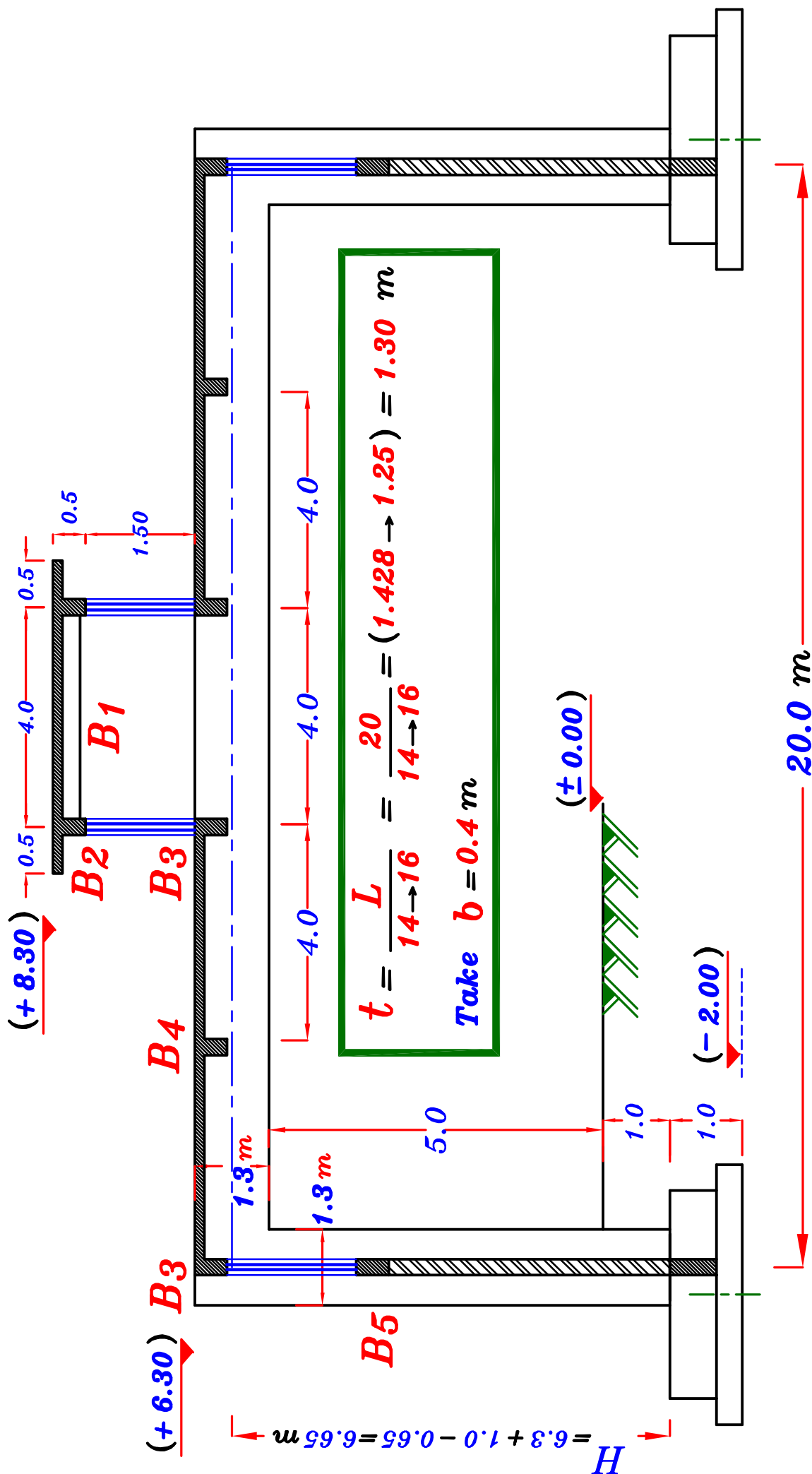
$$\text{Window height} = 1.50 \text{ m}$$

Hard soil.

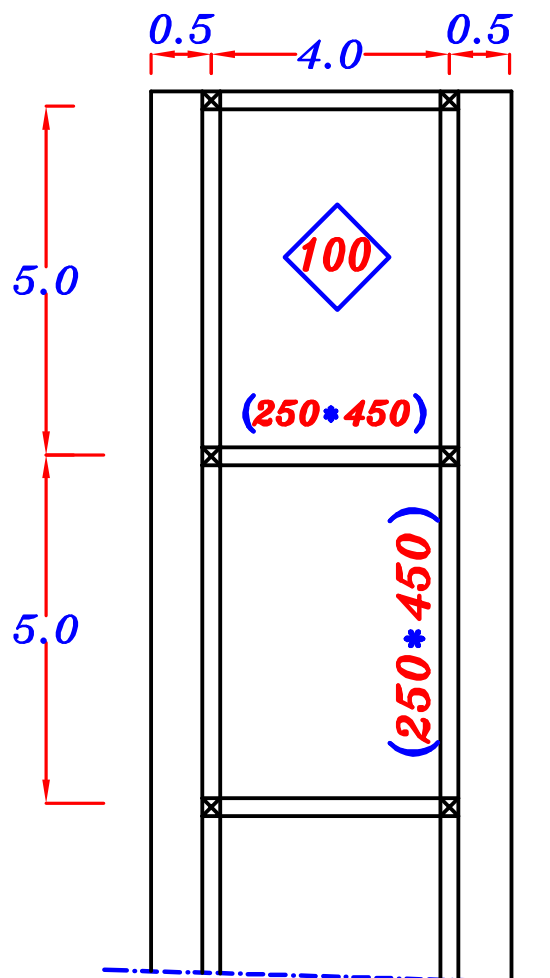
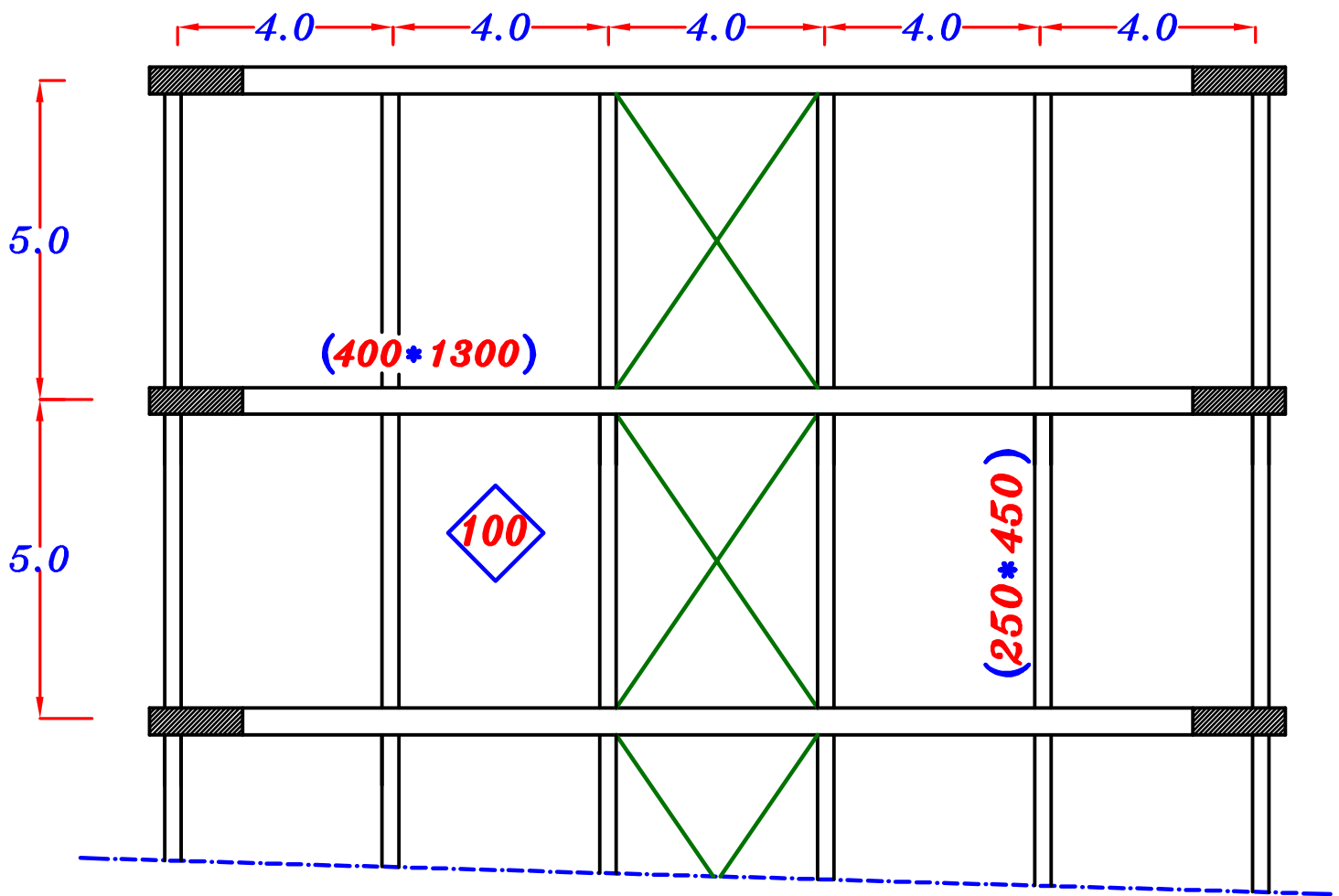
$$\text{Spacing} = 5.0 \text{ m}$$

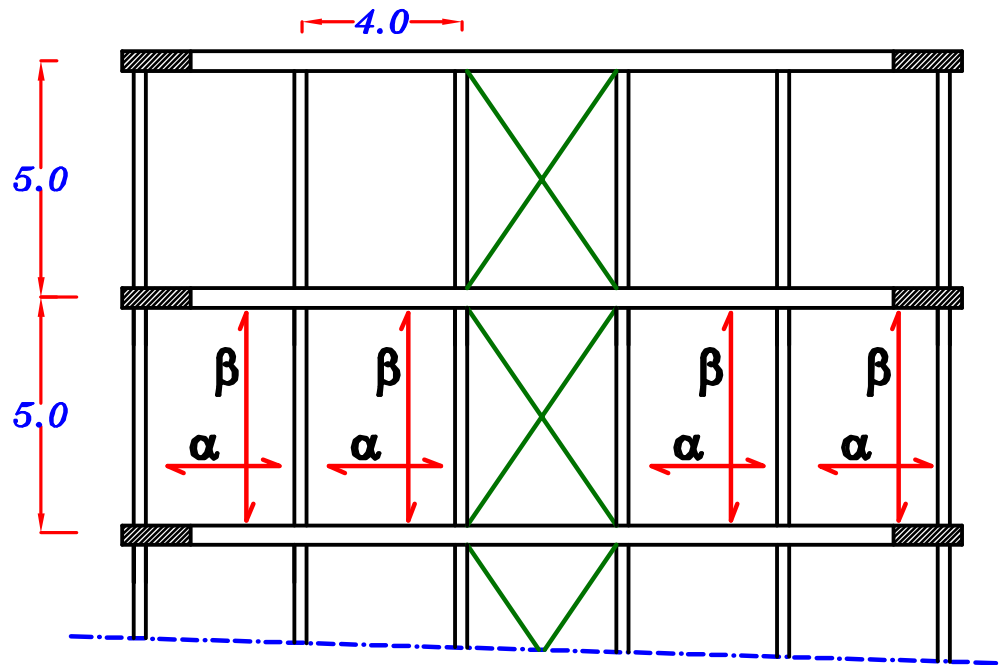
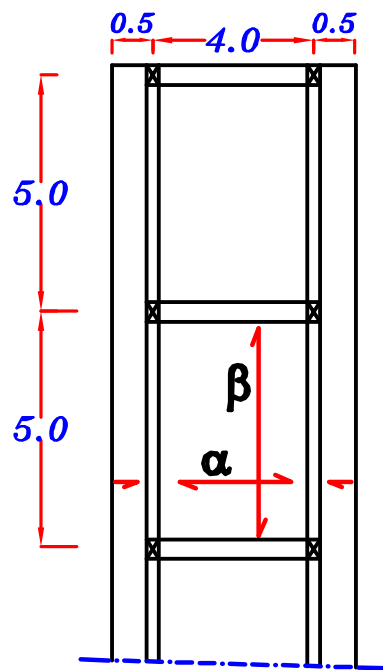
Req.

- 1- Choose a suitable system to cover this area & draw concrete dimensions in elevation For the main supporting element.
- 2- Design all slabs & draw its details of RFT. in plan.
- 3- Design the main supporting element & draw its details of RFT.



ELEVATION





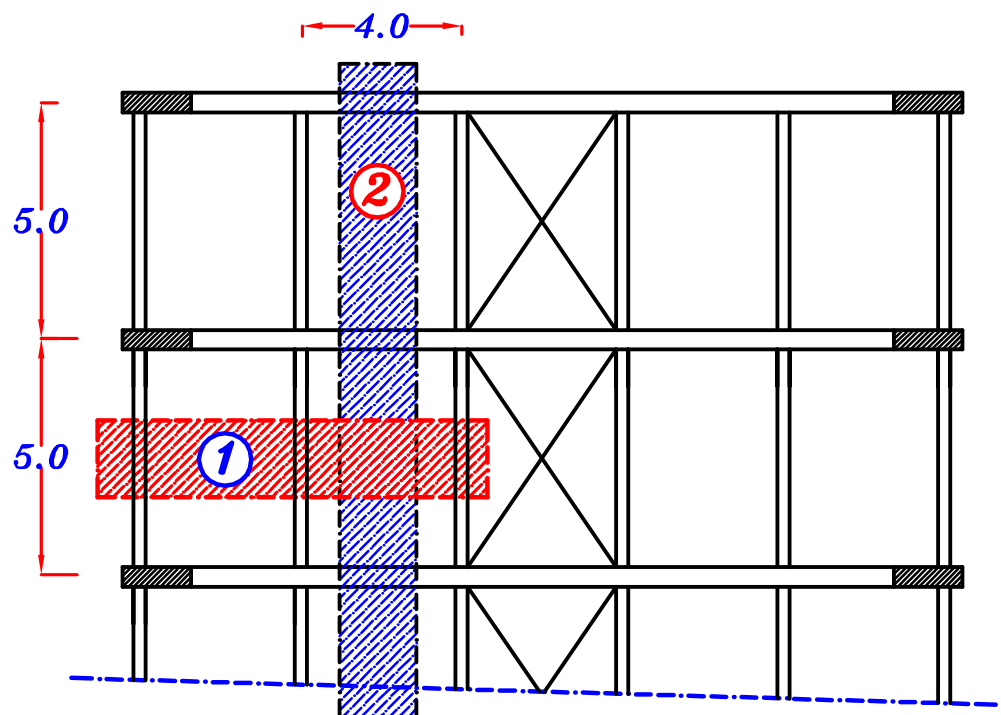
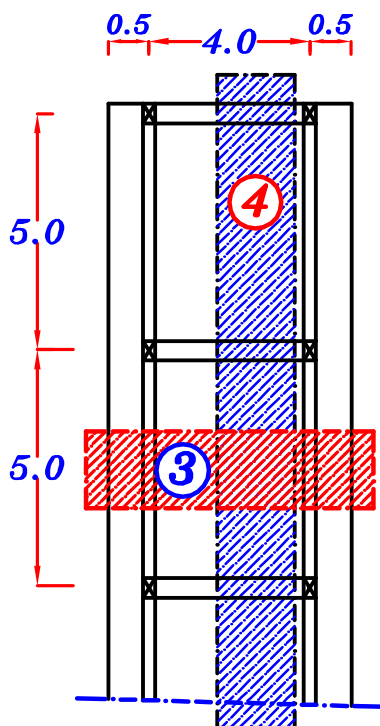
$$t_s = \frac{4000}{40} = 100 \text{ mm} \quad \text{Take } t_s = 100 \text{ mm}$$

$$W_s = 1.4 (0.10 * 25 + 1.50) + 1.6 (2.0) = 8.80 \text{ kN/m}^2$$

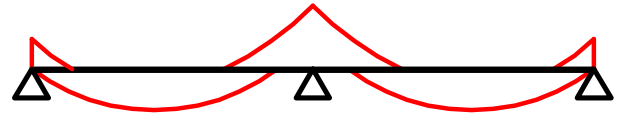
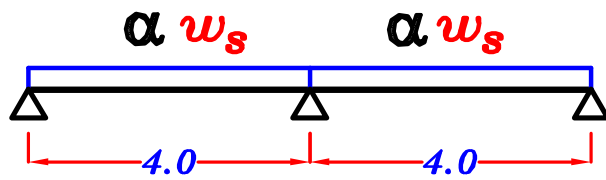
$$\text{Take } m = 0.76, \quad m_s = 0.87 \quad r = \frac{m L}{m_s L_s} = \frac{0.76 * 5.0}{0.87 * 4.0} = 1.09$$

$$\alpha = 0.5 r - 0.15 = 0.5 (1.09) - 0.15 = 0.395$$

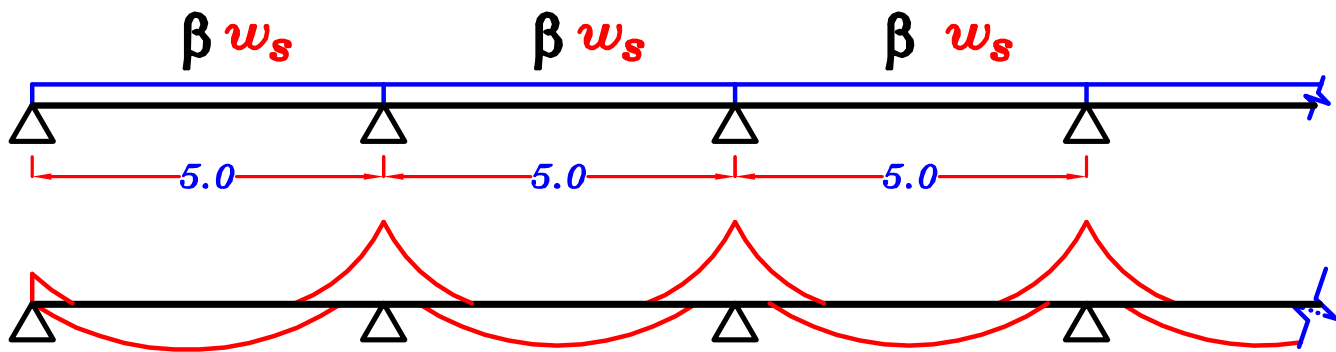
$$\beta = \frac{0.35}{r^2} = \frac{0.35}{(1.09)^2} = 0.295$$



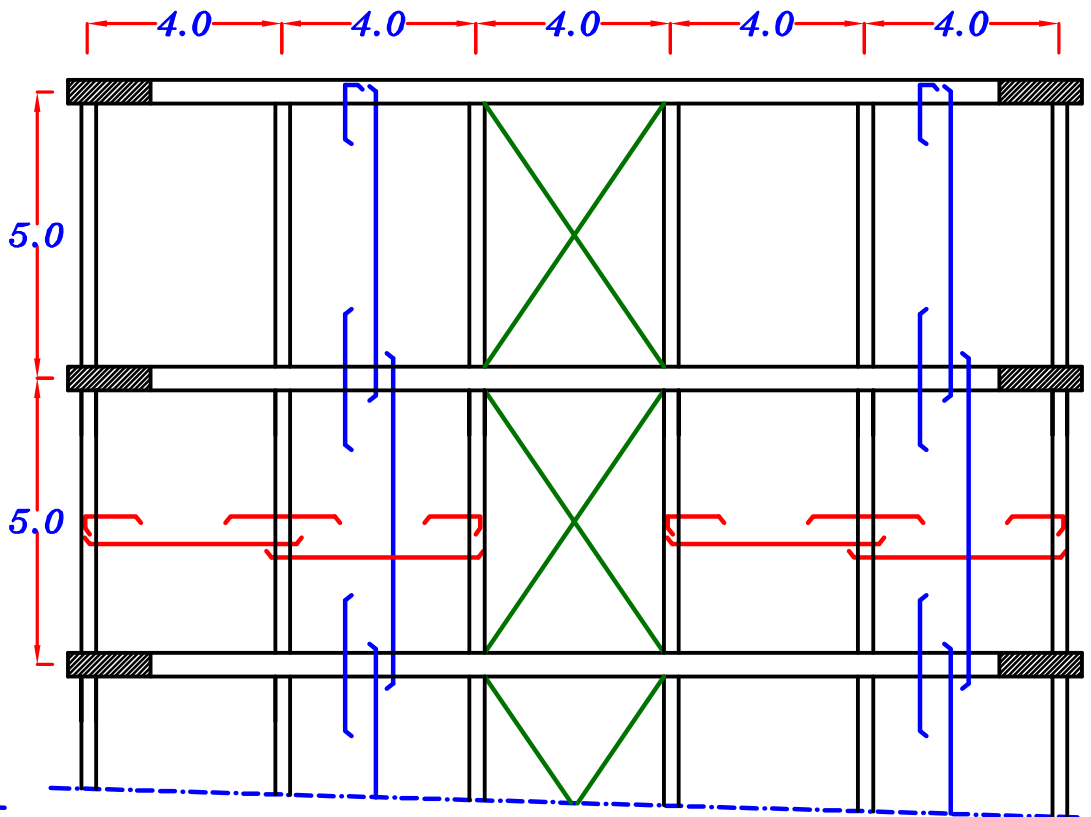
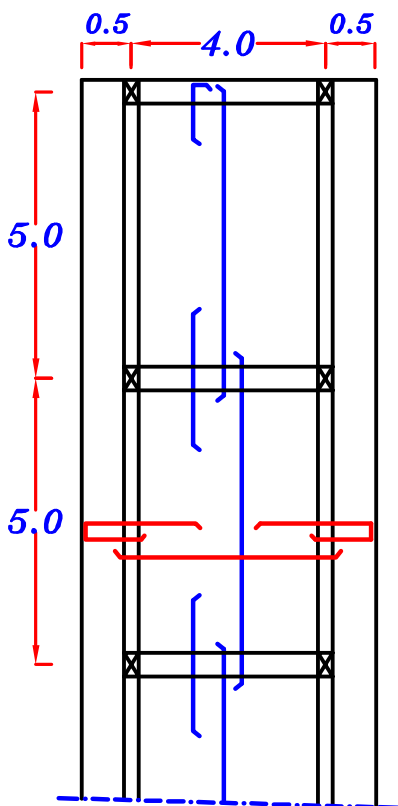
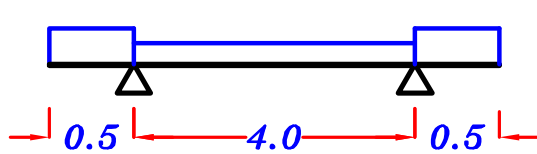
Strip ①



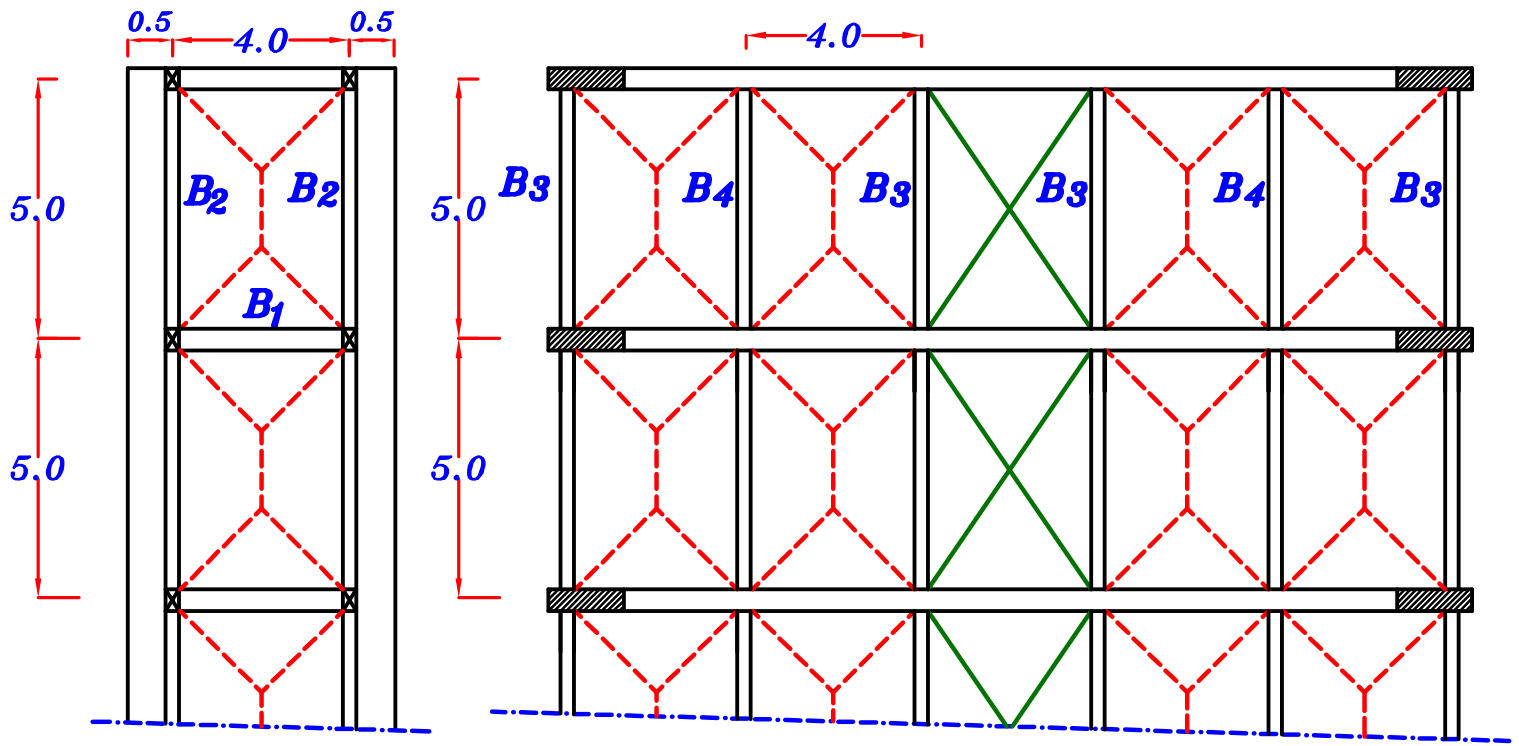
Strip ② & Strip ④



Strip ③



Load Distribution on Beams.



Loads on Beams.

For Trapezoid $C_a = 1 - \frac{1}{2} \left(\frac{L_s}{L} \right) = 1 - \frac{1}{2} \left(\frac{4.0}{5.0} \right) = 0.60$

B1 $w_a = o.w. + 2 C_a w_s \frac{L_s}{2} = 4.20 + 2 (0.50) (8.80) \left(\frac{4.0}{2} \right) = 21.8 \text{ kN/m}$

$R_1 = 21.8 * \frac{4.0}{2} = 43.6 \text{ kN}$ $R_1 = 43.6 \text{ kN}$

B2 $w_a = o.w. + C_a w_s \frac{L_s}{2} + w_s L_c = 4.20 + (0.60) (8.80) \left(\frac{4.0}{2} \right) + (8.80)(0.5) = 19.16 \text{ kN/m}$

$R_2 = 19.16 * 5.0 = 95.8 \text{ kN}$ $R_2 = 95.8 \text{ kN}$

B3 $w_a = o.w. + C_a w_s \frac{L_s}{2} = 4.20 + (0.60) (8.80) \left(\frac{4.0}{2} \right) = 14.76 \text{ kN/m}$

$R_3 = 14.76 * 5.0 = 73.8 \text{ kN}$ $R_3 = 73.8 \text{ kN}$

B4 $w_a = o.w. + 2 C_a w_s \frac{L_s}{2} = 4.20 + 2 (0.60) (8.80) \left(\frac{4.0}{2} \right) = 25.32 \text{ kN/m}$

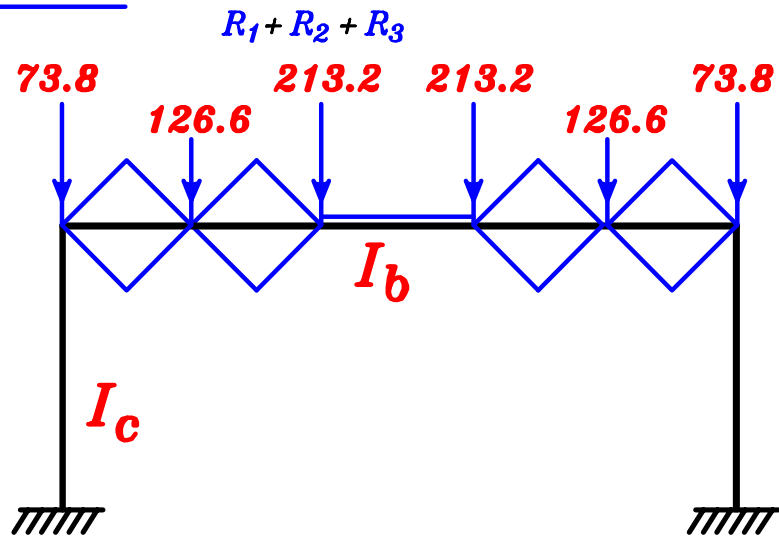
$R_4 = 25.32 * 5.0 = 126.6 \text{ kN}$ $R_4 = 126.6 \text{ kN}$

B5 Can be neglected.

Loads on Frame.

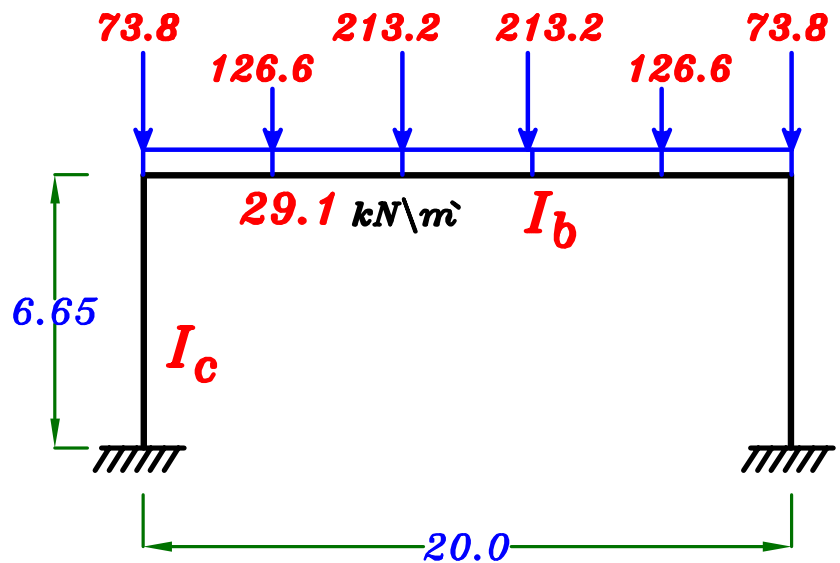
Take o.w.(U.L.) = 15.0 kN/m

$$\frac{\sum \text{area}}{\text{span}} = \frac{8 \left[\left(\frac{1}{2} \right) (4.0) \left(\frac{4.0}{2} \right) \right]}{20} = 1.60$$



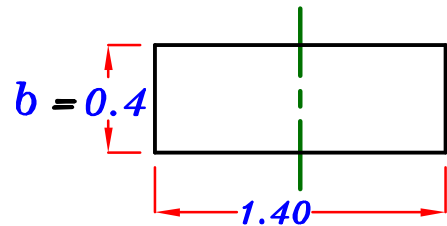
$$w_a = \text{o.w.} + \frac{\sum \text{area}}{\text{span}} * w_s$$

$$w_a = w_e = 15.0 + (1.6)(8.80) = 29.1 \text{ kN/m}$$



I_c

$$I_c = \frac{b(t)^3}{12} = \frac{0.4(1.40)^3}{12} = 0.09146 \text{ m}^4$$

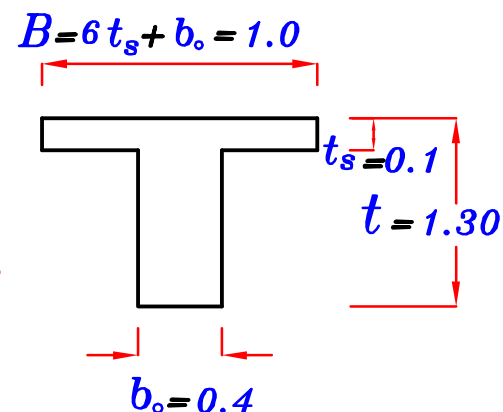


I_{b1}

$$\left. \begin{aligned} \frac{t_s}{t} &= \frac{0.1}{1.30} = 0.077 \\ \frac{b_o}{B} &= \frac{0.4}{1.0} = 0.40 \end{aligned} \right\} \text{From Tables page 91}$$

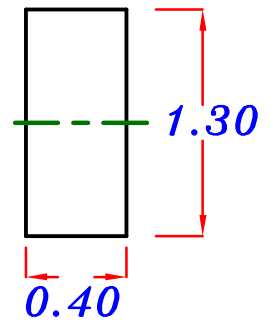
$$\mu = 420.76$$

$$I_{b1} = (\mu * 10^{-4}) B t^3 = 420.76 * 10^{-4} * 1.0 * 1.30^3 = 0.0924 \text{ m}^4$$



$$\underline{\underline{I_{b2}}}$$

$$I_{b2} = \frac{b(t)^3}{12} = \frac{0.40(1.30)^3}{12} = 0.0732 \text{ m}^4$$



$$\underline{\underline{I_b}}$$

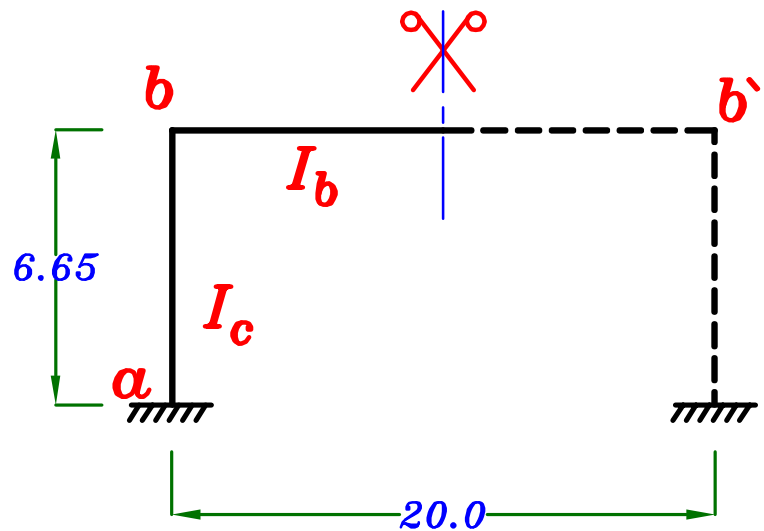
$$I_b = \frac{I_{b1} * 2L_1 + I_{b2} * L_2}{2L_1 + L_2} \quad \text{نأخذ المتوسط}$$

$$I_b = \frac{0.0924 * 16.0 + 0.0732 * 4.0}{16.0 + 4.0} = 0.08856$$

$$\therefore \boxed{I_b = 0.968 I_c}$$

Distribution Factor.

D.F.



For Joint b

$$K_c = \frac{I_c}{h} = \frac{I_c}{6.65} = 0.150 I_c$$

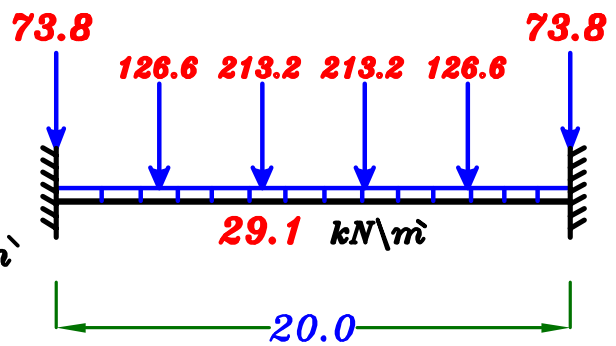
$$K_b = \frac{1}{2} \frac{I_b}{L} = \frac{1}{2} * \frac{(0.968) I_c}{20.0} = 0.0242 I_c$$

$$D.F. \text{ } c = \frac{0.150}{0.150 + 0.0242} = 0.861$$

$$D.F. \text{ } b = 1 - 0.861 = 0.139$$

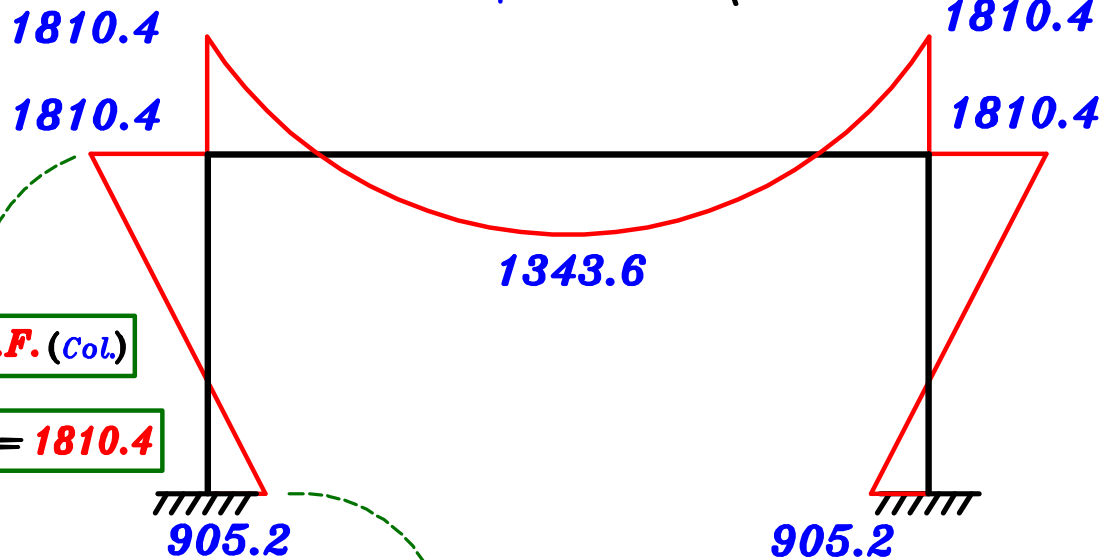
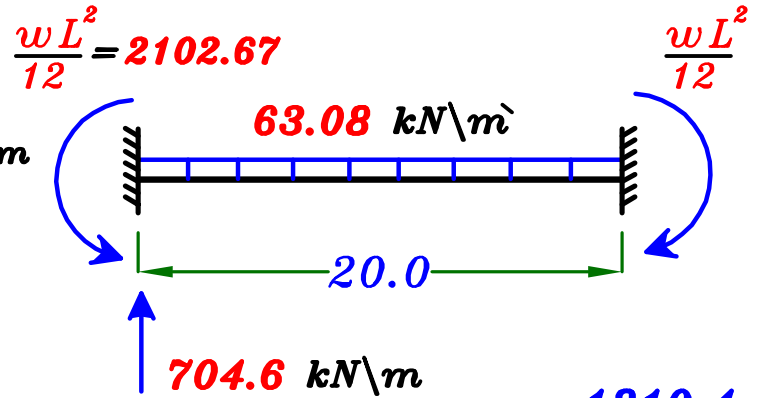
$$w = o.w. + \frac{\sum P}{span}$$

$$= 29.1 + \frac{2(126.6) + 2(213.2)}{20.0} = 63.08 \text{ kN/m}$$



F.E.M.

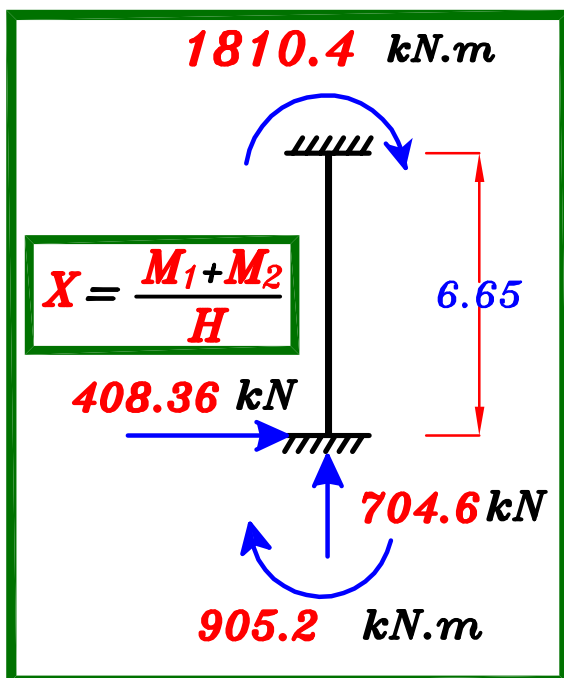
$$\frac{wL^2}{12} = \frac{63.08 * (20.0)^2}{12} = 2102.67 \text{ kN.m}$$

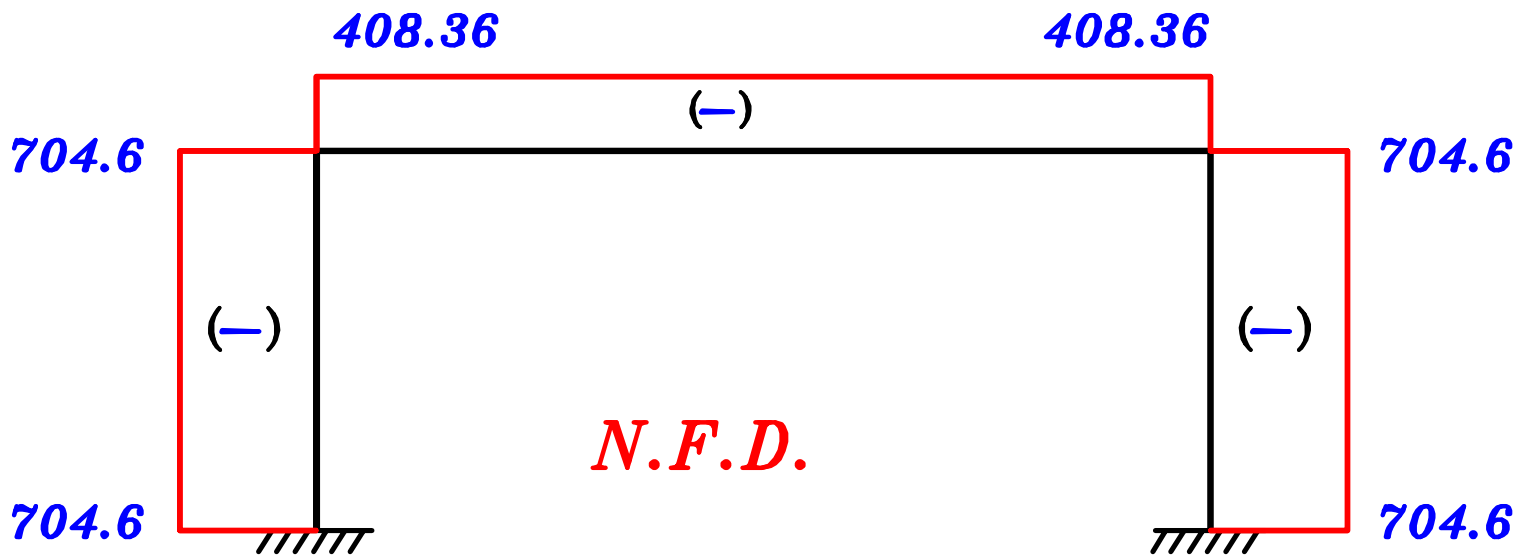
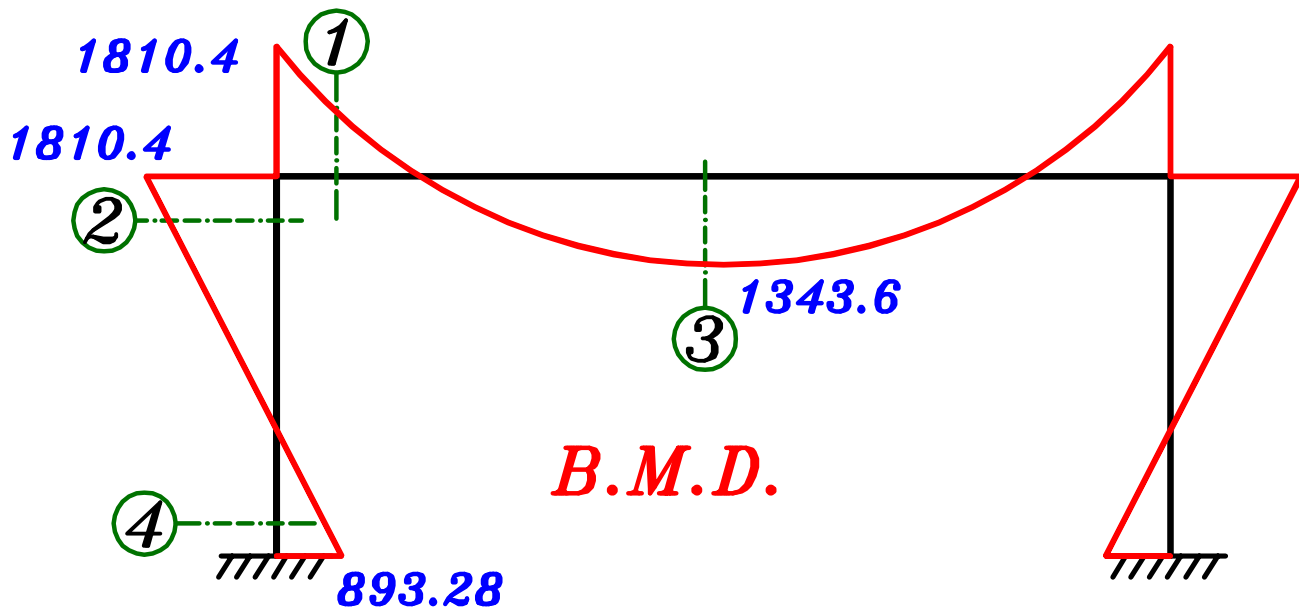


F.E.M. (Beam) * D.F. (Col.)

$$2102.67 * 0.861 = 1810.4$$

$$\frac{1}{2} [F.E.M. (Beam) * D.F. (Col.)]$$





Design of Sections.

Sec. ① R-Sec.

$$M = 1810.4 \text{ kN.m} , P = 408.36 \text{ kN} , b = 400 \text{ mm} , t = 1300 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{408.36 * 10^3}{25 * 400 * 1300} = 0.0314 < 0.04 \text{ (neglect } P \text{)}$$

$$\therefore 1200 = C_1 \sqrt{\frac{1810.4 * 10^6}{25 * 400}} \rightarrow C_1 = 2.82 \rightarrow J = 0.730$$

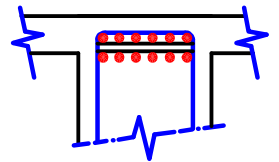
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1810.4 * 10^6}{0.730 * 360 * 1200} = 5740.7 \text{ mm}^2$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 5740.7 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1200 = 1640.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 5740.7 \text{ mm}^2 \quad \textcircled{12 \phi 25}$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$



Sec. ② R-Sec.

Neglect Effect of Buckling.

$$M = 1810.4 \text{ kN.m} , P = 704.6 \text{ kN} , b = 400 \text{ mm} , t = 1300 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{704.6 * 10^3}{25 * 400 * 1300} = 0.054 > 0.04 \text{ (Don't neglect } P \text{)}$$

$$e = \frac{M}{P} = \frac{1810.4}{704.6} = 2.57 \text{ m} \quad \therefore \frac{e}{t} = \frac{2.57}{1.3} = 1.97 > 0.5 \xrightarrow{\text{use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 2.56 + \frac{1.3}{2} - 0.1 = 3.12 \text{ m}$$

$$M_s = P * e_s = 704.6 * 3.12 = 2198.35 \text{ kN.m}$$

$$\therefore 1200 = C_1 \sqrt{\frac{2198.35 * 10^6}{25 * 400}} \rightarrow C_1 = 2.56 < 2.78 \rightarrow \text{Increase Dimensions.}$$

$$\text{Take } t = 1400 \text{ mm} \rightarrow d = 1300 \text{ mm} , b = 400 \text{ mm}$$

$$\therefore 1300 = C_1 \sqrt{\frac{2198.35 * 10^6}{25 * 400}} \rightarrow C_1 = 2.78 \rightarrow J = 0.717$$

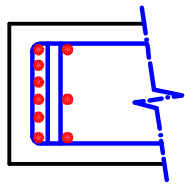
$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \phi_s)} = \frac{2198.35 * 10^6}{0.717 * 360 * 1300} - \frac{704.6 * 10^3}{(360 \setminus 1.15)} = 4300.5 \text{ mm}^2$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 4300.5 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1300 = 1625 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 4300.5 \text{ mm}^2 \quad \textcircled{9 \phi 25}$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$



Sec. ③ R-Sec.

$$M = 1343.6 \text{ kN.m} , P = 408.36 \text{ kN} , b = 400 \text{ mm} , t = 1300 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{408.36 * 10^3}{25 * 400 * 1300} = 0.0314 < 0.04 \text{ (neglect } P \text{)}$$

$$\therefore 1200 = C_1 \sqrt{\frac{1343.6 * 10^6}{25 * 400}} \rightarrow C_1 = 3.27 \rightarrow J = 0.768$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1343.6 * 10^6}{0.768 * 360 * 1200} = 4049.7 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 4049.7 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1200 = 1640.6 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 4049.7 \text{ mm}^2 \quad \textcircled{9 \phi 25}$$

Sec. ④ R-Sec. Neglect Effect of Buckling.

$$M = 905.2 \text{ kN.m} , P = 704.6 \text{ kN} , b = 400 \text{ mm} , t = 1400 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{704.6 * 10^3}{25 * 400 * 1400} = 0.0503 > 0.04 \quad (\text{Don't neglect } P)$$

$$e = \frac{M}{P} = \frac{905.2}{704.6} = 1.267 \text{ m} \quad \therefore \frac{e}{t} = \frac{1.267}{1.40} = 0.905 > 0.5 \xrightarrow{\text{use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.267 + \frac{1.4}{2} - 0.1 = 1.867 \text{ m}$$

$$M_s = P * e_s = 704.6 * 1.867 = 1315.49 \text{ kN.m}$$

$$\therefore 1300 = C_1 \sqrt{\frac{1315.49 * 10^6}{25 * 400}} \rightarrow C_1 = 3.584 \rightarrow J = 0.786$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \delta_s)} = \frac{1315.49 * 10^6}{0.786 * 360 * 1300} - \frac{704.6 * 10^3}{(360 \setminus 1.15)} = 1325.37 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 1325.37 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1300 = 1625 \text{ mm}^2$$

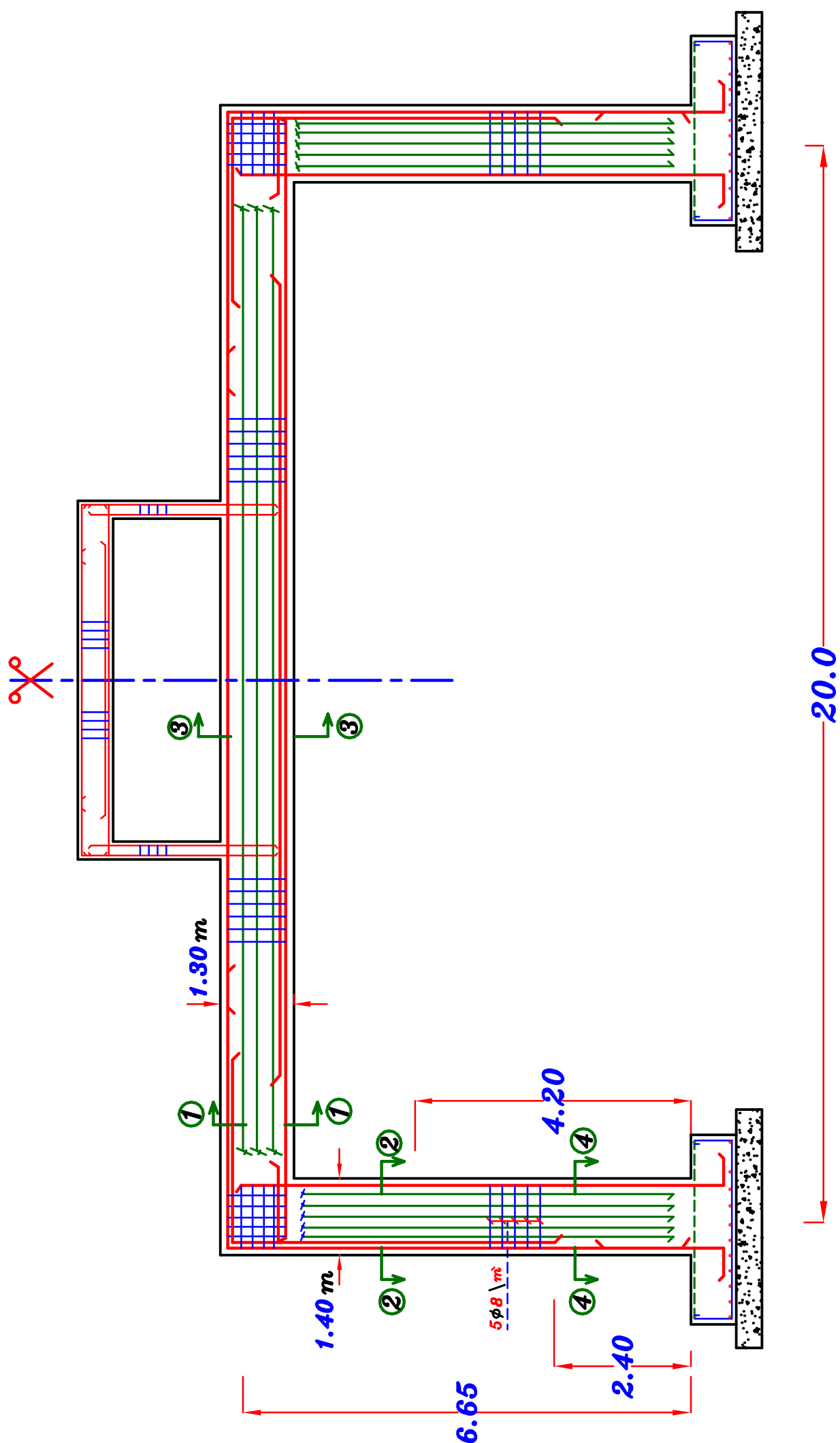
$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

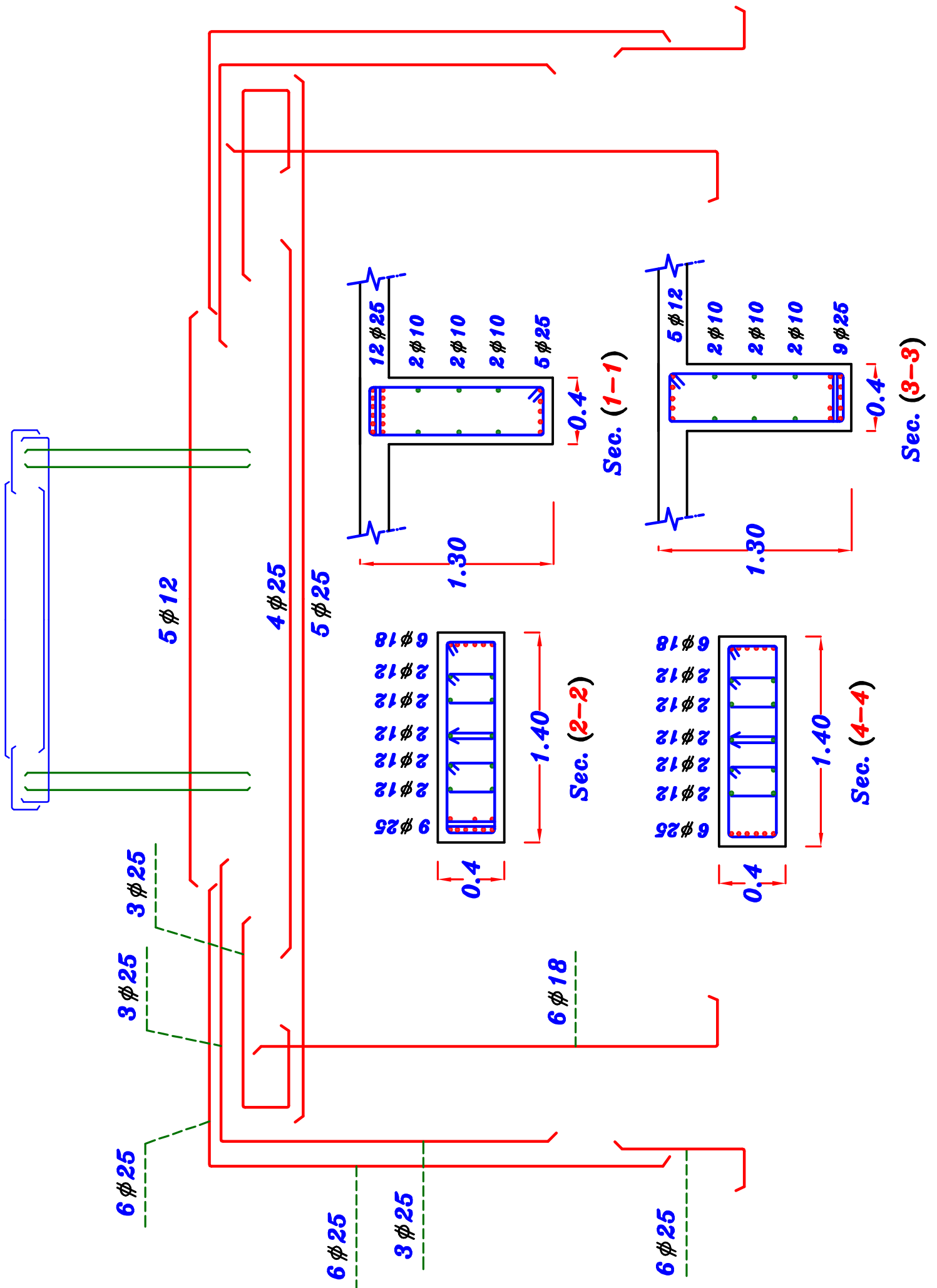
$$A_{s_{min.}} = 0.225 * \frac{\sqrt{F_{cu}}}{F_y} b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 400 * 1300 = 1625$$

$$1.3 A_{s_{req.}} = 1.3 * 1325.37 = 1722.98$$

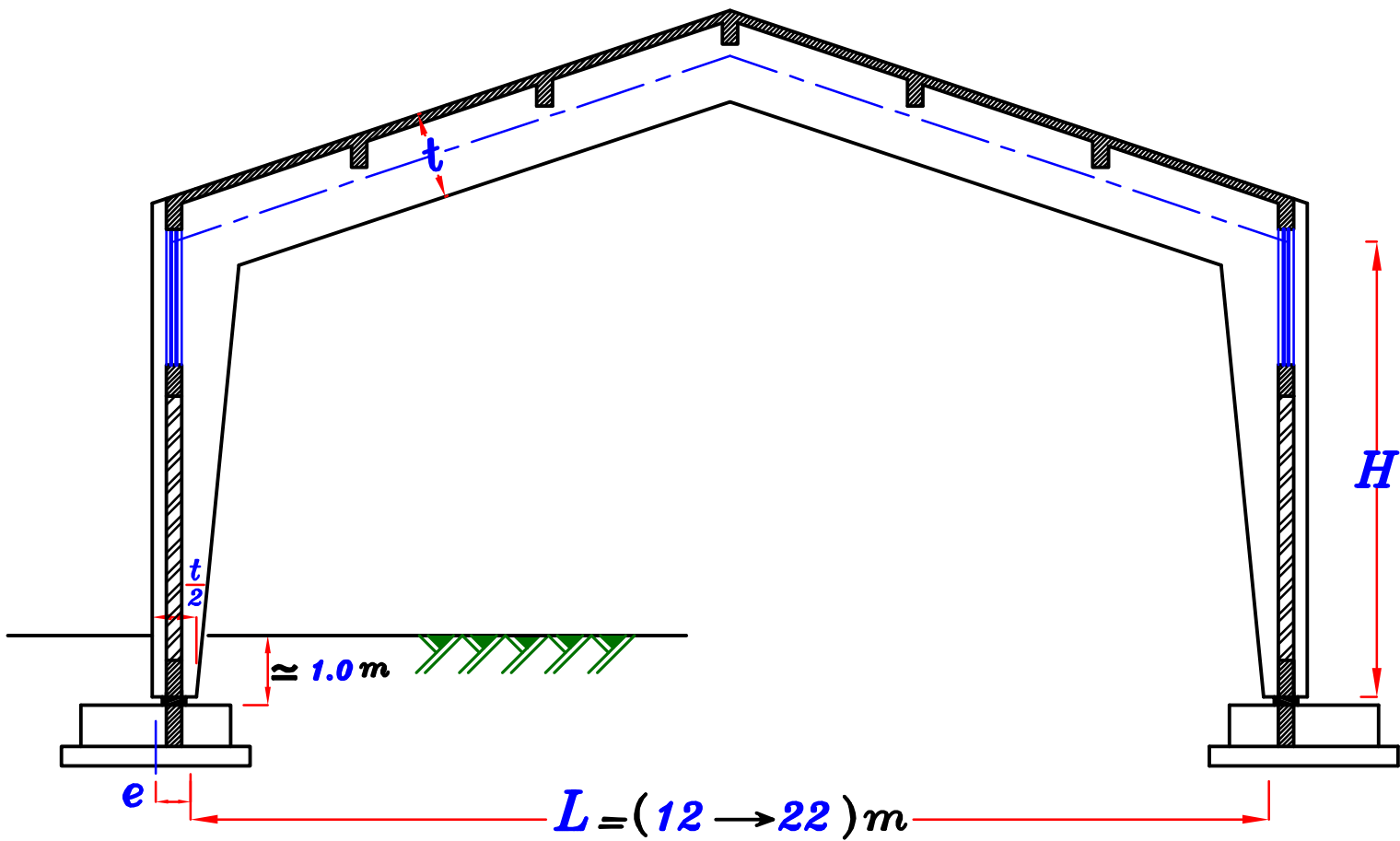
$$\text{st. } 360/520 \quad \frac{0.15}{100} b d = \frac{0.15}{100} * 400 * 1300 = 780 \text{ mm}^2$$

الأقل = 1625
الأكثر = 1625 mm²
6 ϕ 18





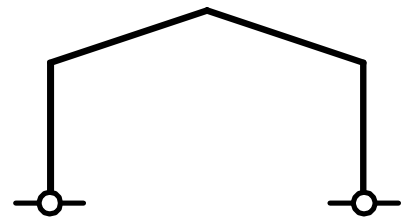
Two Hinged Inclined Frame.



– Statical System

The 2 hinged Frame is

Once Statically indeterminate structure

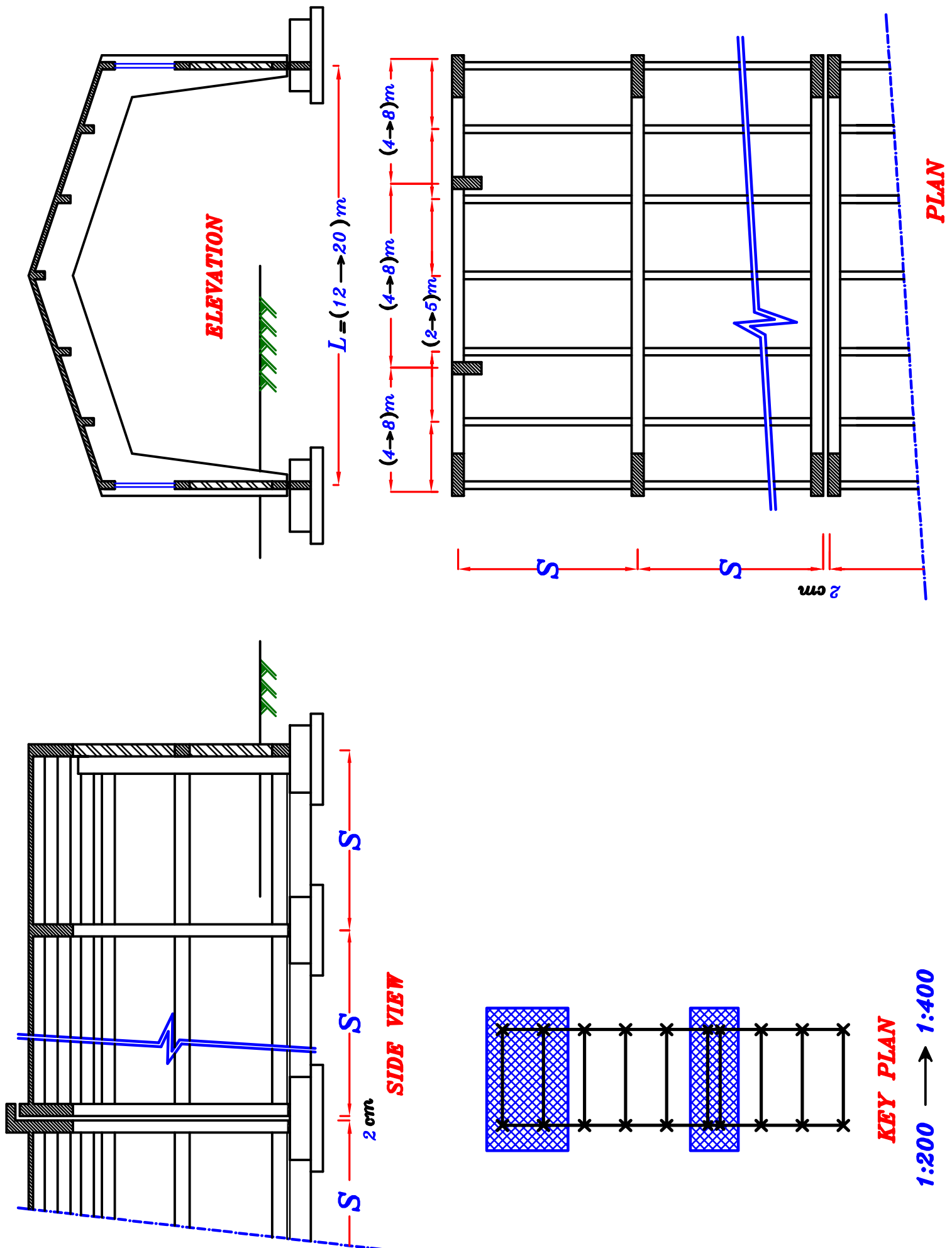


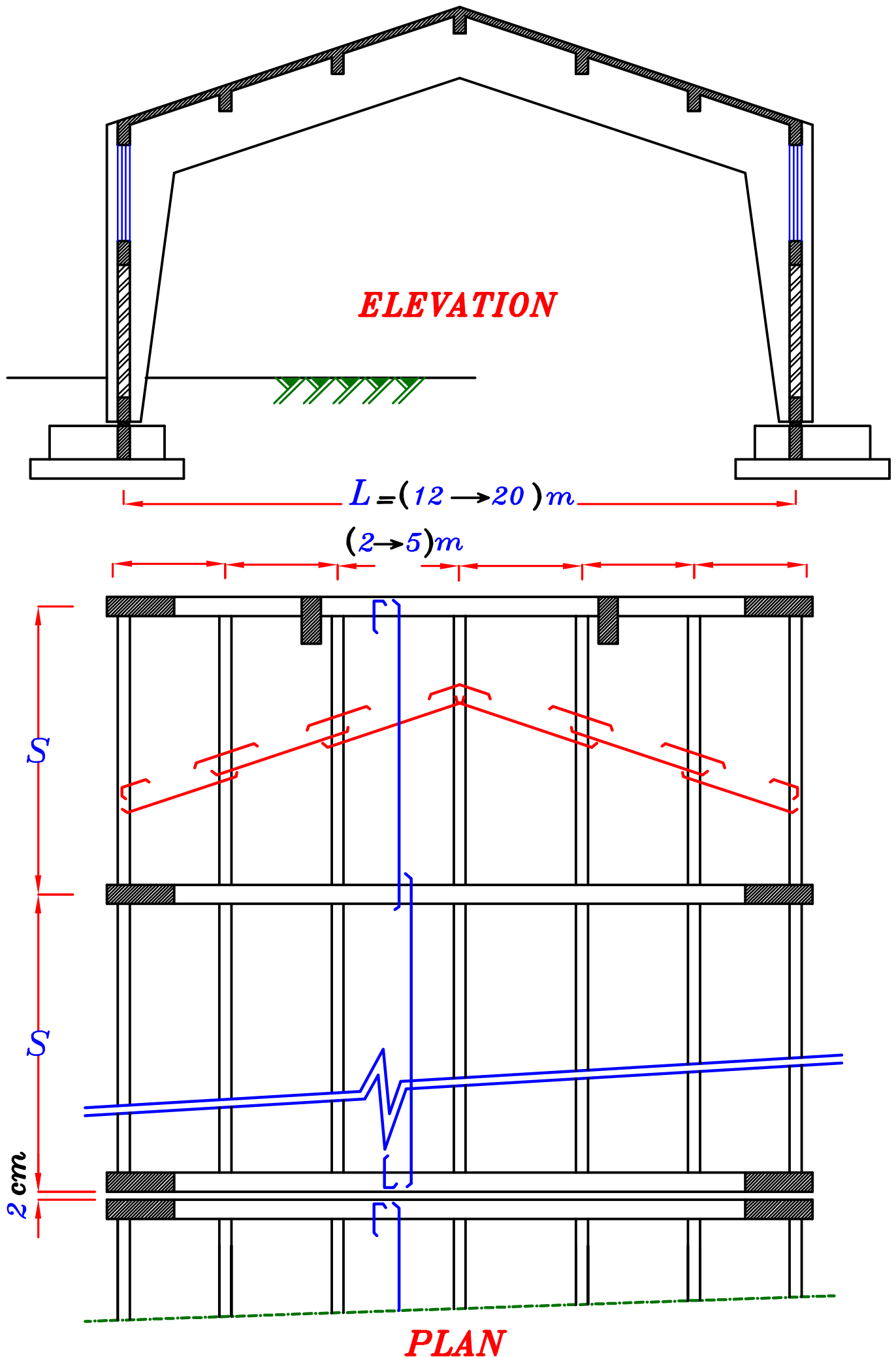
– Concrete Dimensions.

* $\text{Span } (L) = (12 \rightarrow 22) \text{ m}$

* $t \approx \frac{L'}{12 \rightarrow 14}$

* $b = \frac{0.30 \text{ m}}{\frac{\text{Spacing}}{20}}$ } الأكبر





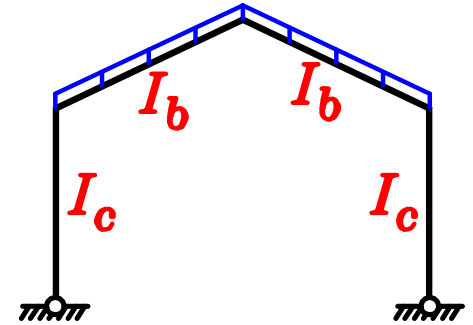
Solving the Inclined Frame.



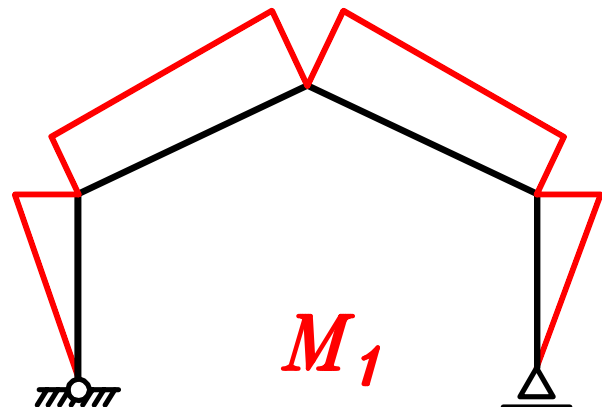
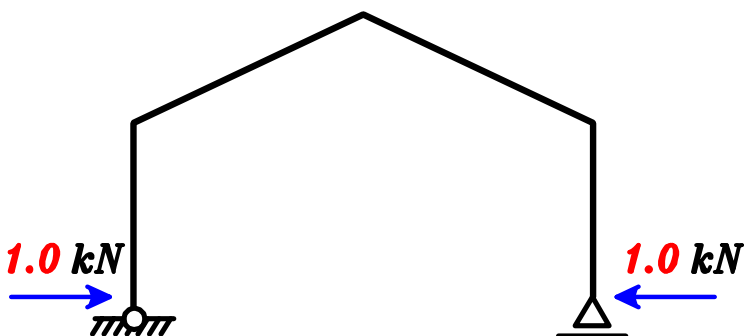
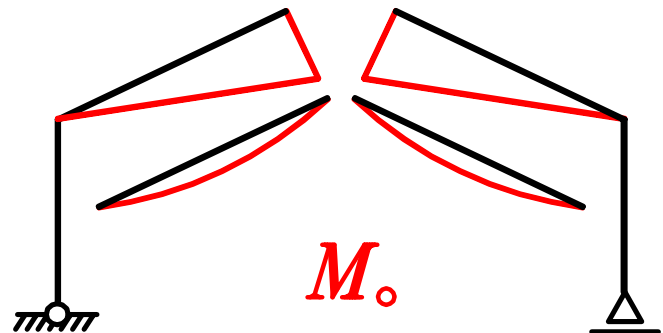
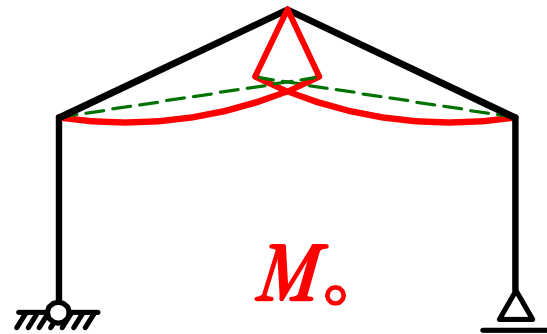
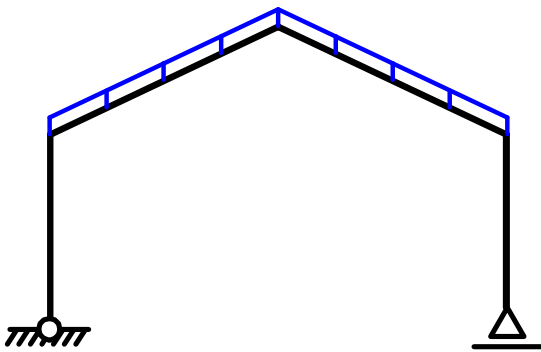
نظرا لوجود *Sway* على ال *Frame*
لذا الاسهل حله بـ *Virtual work*

Virtual work method.

Ⓐ Get Moment of Inertia For all members. (I)



Ⓑ Make the Frame Determinate and Draw B.M.D. (M_o)



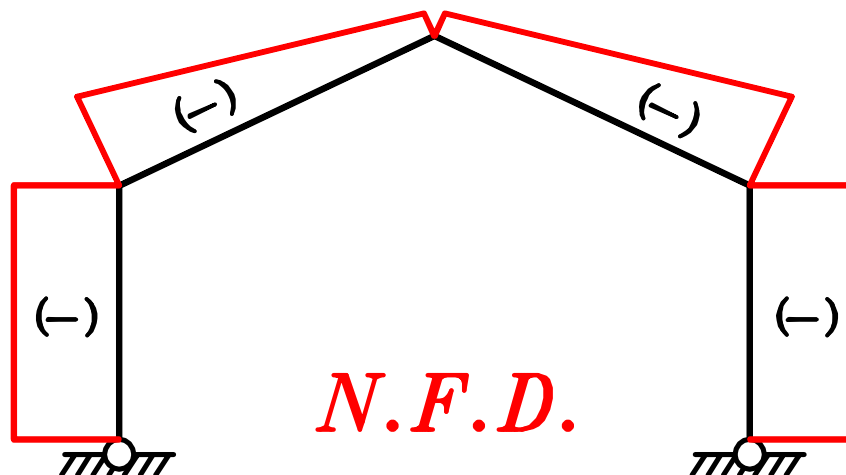
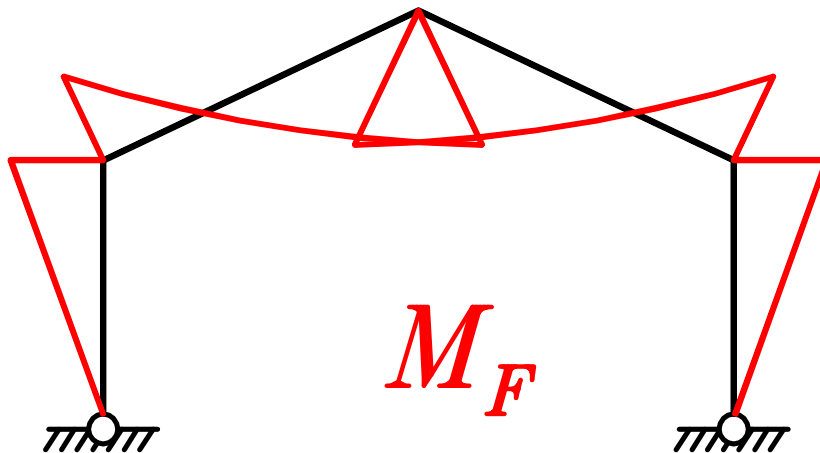
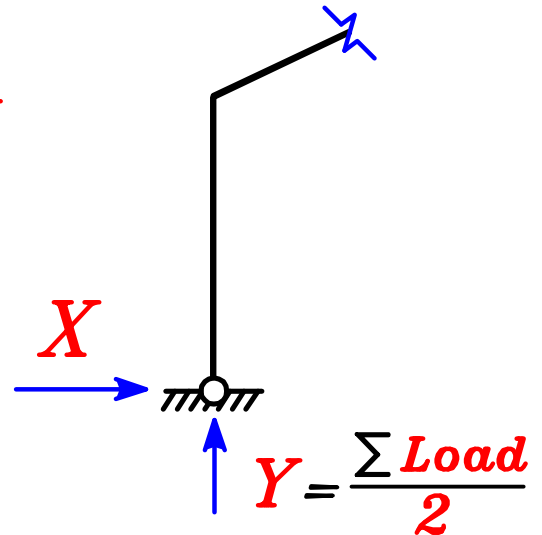
© Calculate the deflections. δ_{10} & δ_{11}

$$\delta_{10} = \frac{1}{E_c I_b} * (M_o * M_1) + \frac{1}{E_c I_c} * (M_o * M_1)$$

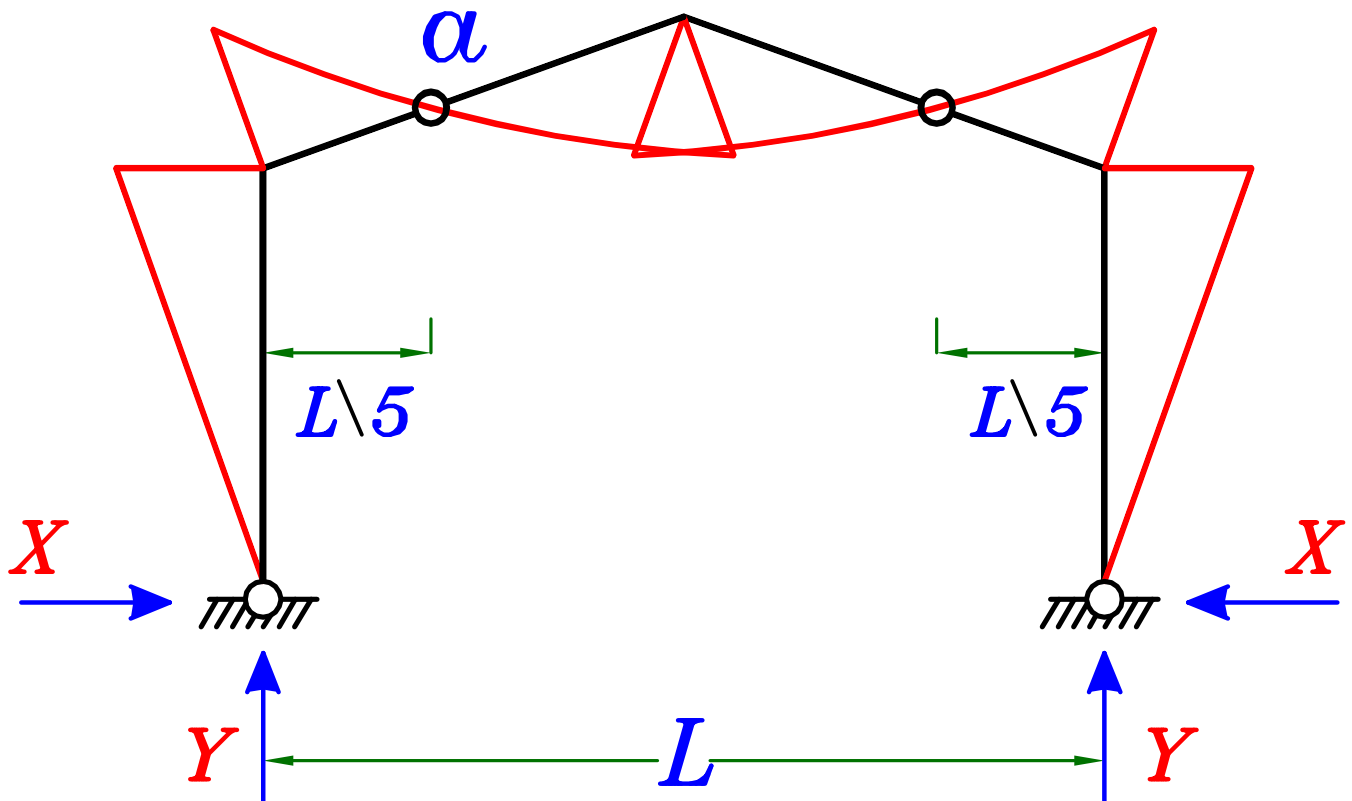
$$\delta_{11} = \frac{1}{E_c I_b} * (M_1 * M_1) + \frac{1}{E_c I_c} * (M_1 * M_1)$$

$$\delta_{10} + X \delta_{11} = \text{Zero} \quad \text{Get } X$$

$$M_F = M_o + X M_1$$



Approximate Solution.



assume that in the beam there is an intermediate hinge at $\frac{L}{5}$

$$Y = \frac{\sum \text{Loads}}{2}$$

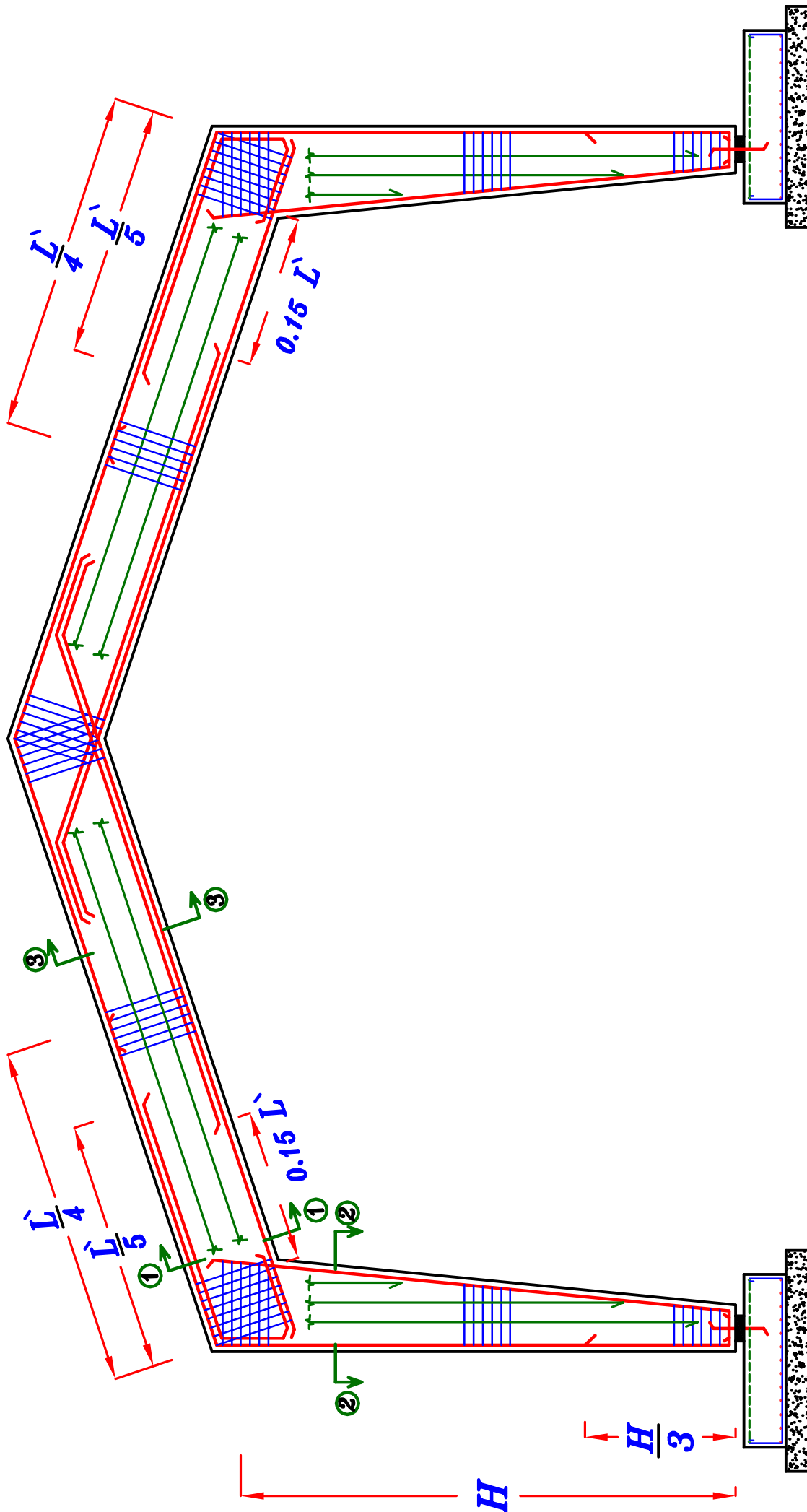
To get the reactions X

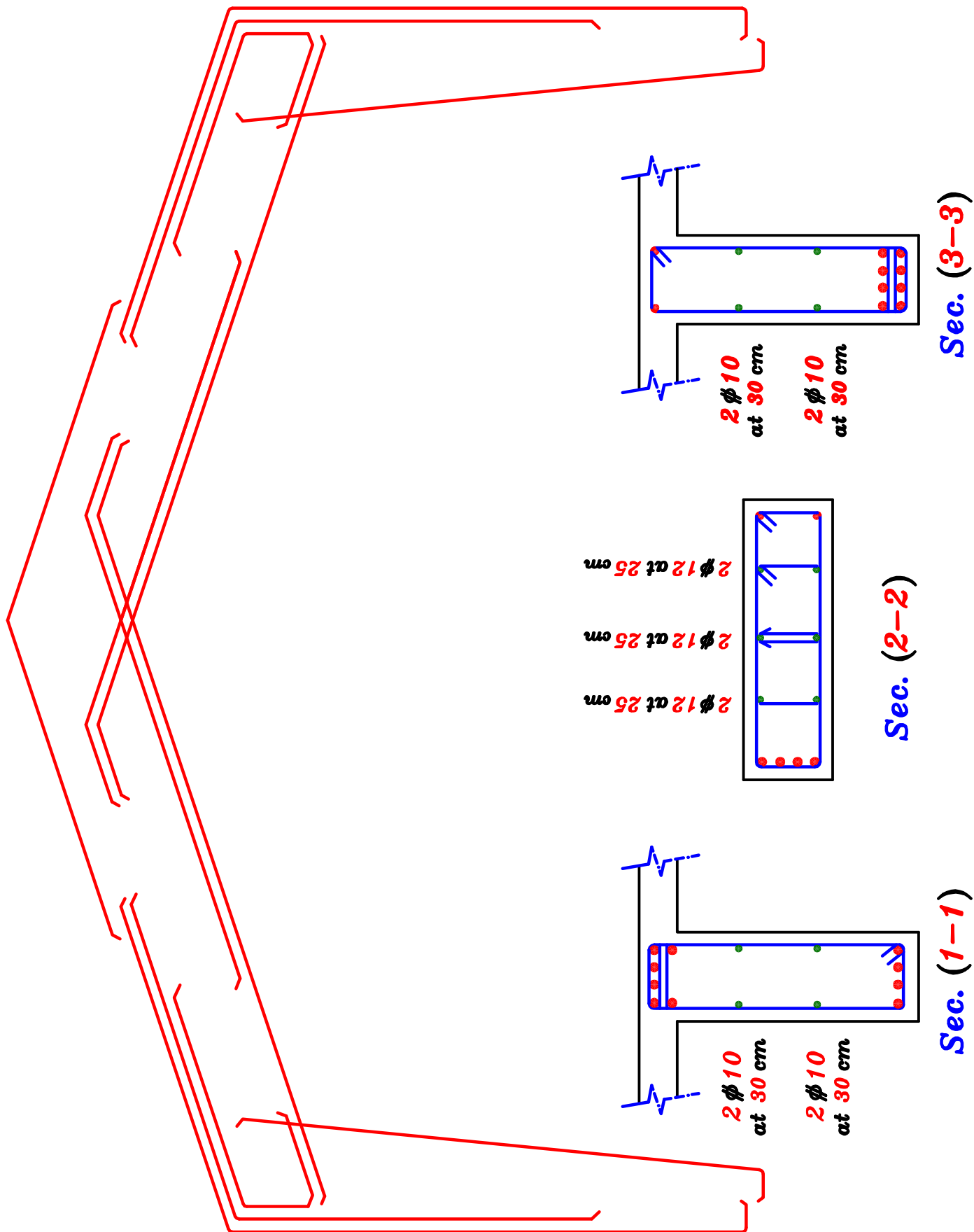
Take the moment at Point $\alpha = \text{Zero}$

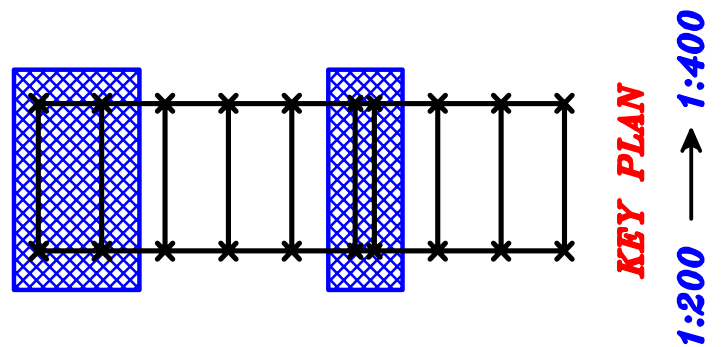
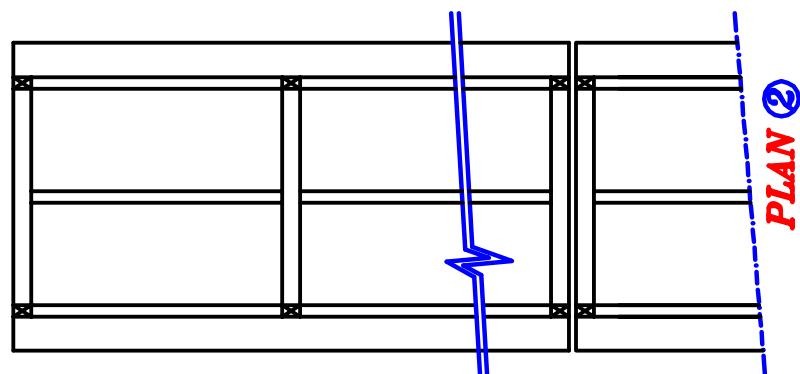
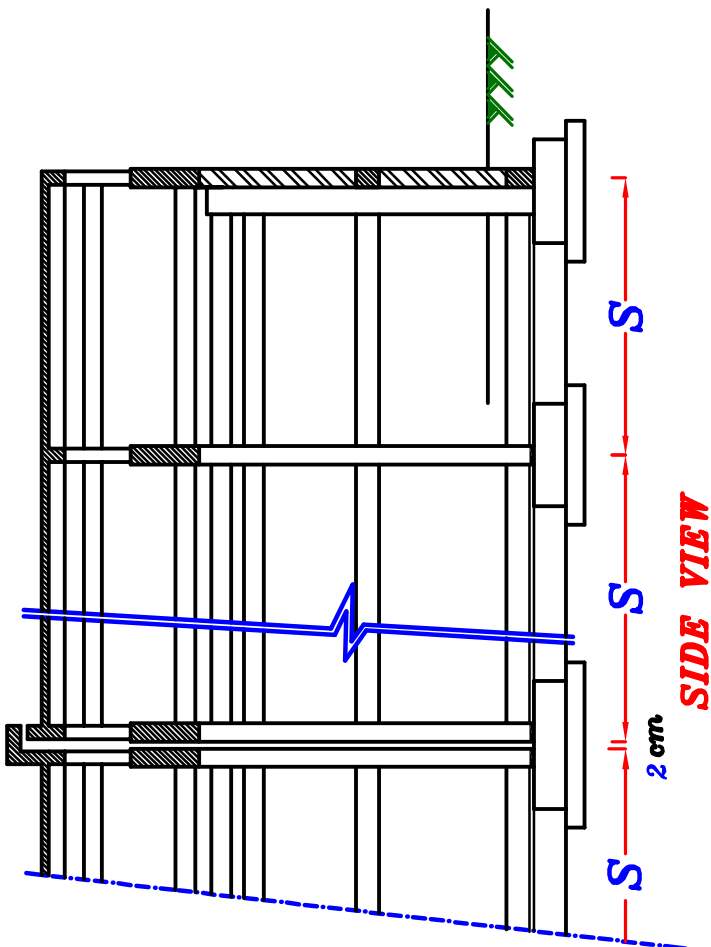
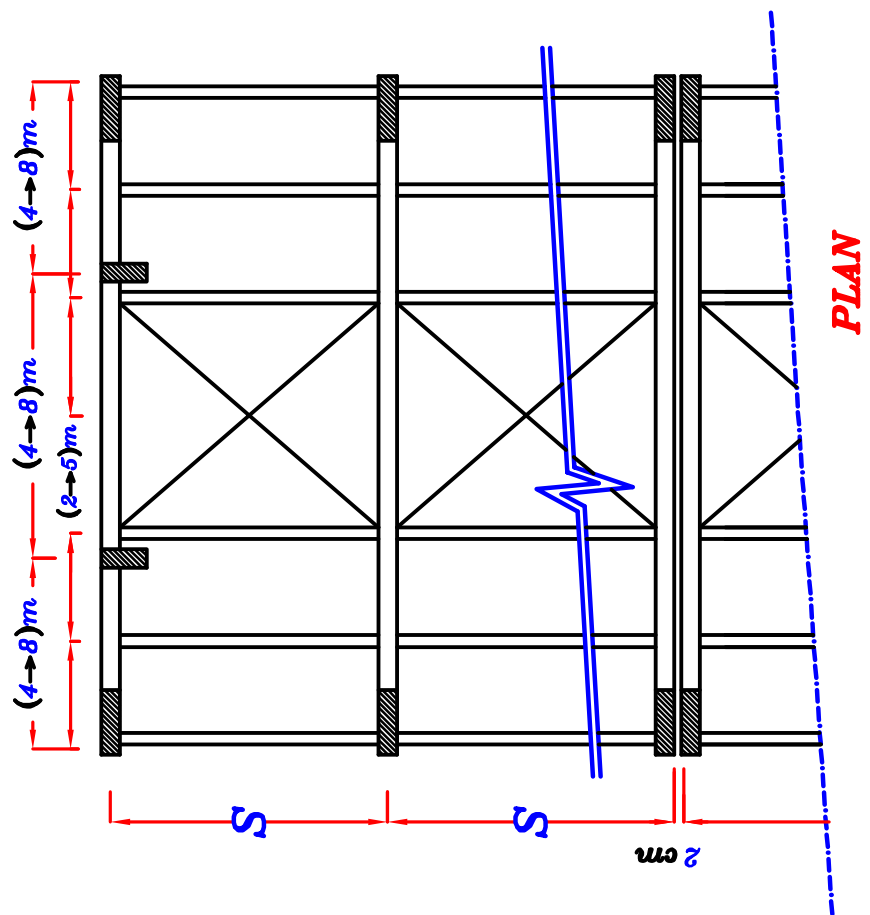
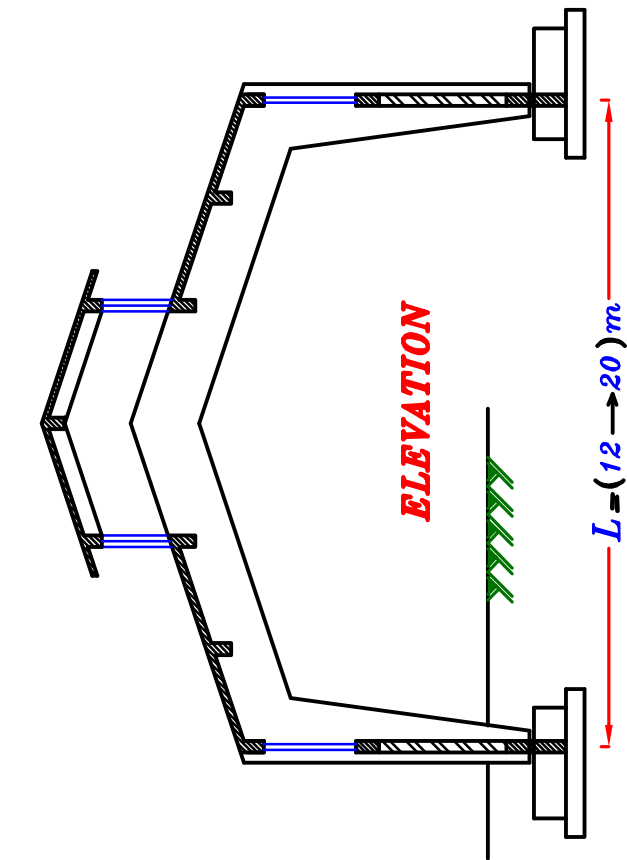
Then Draw Internal Forces Diagrams.

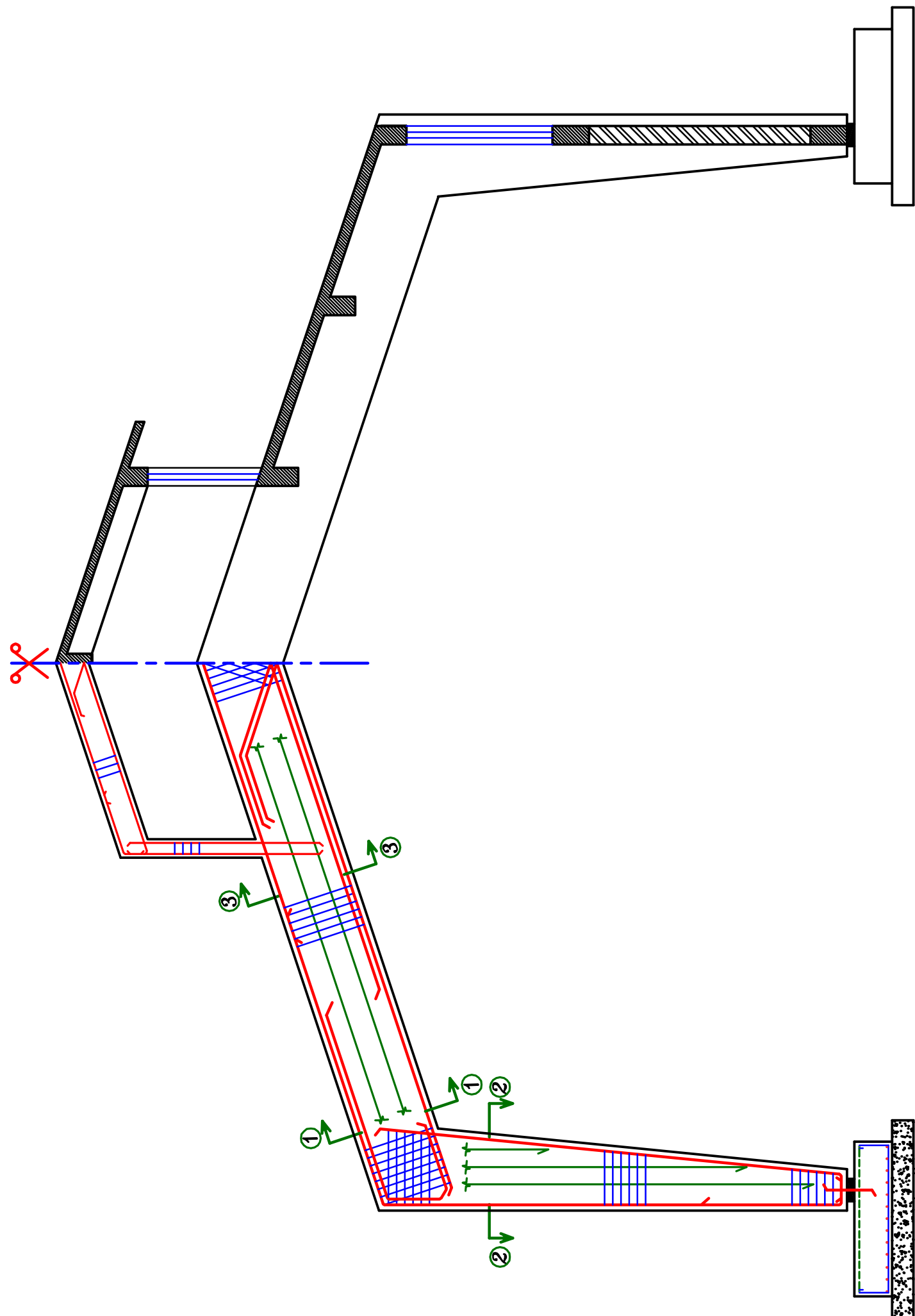
ملحوظه هامه

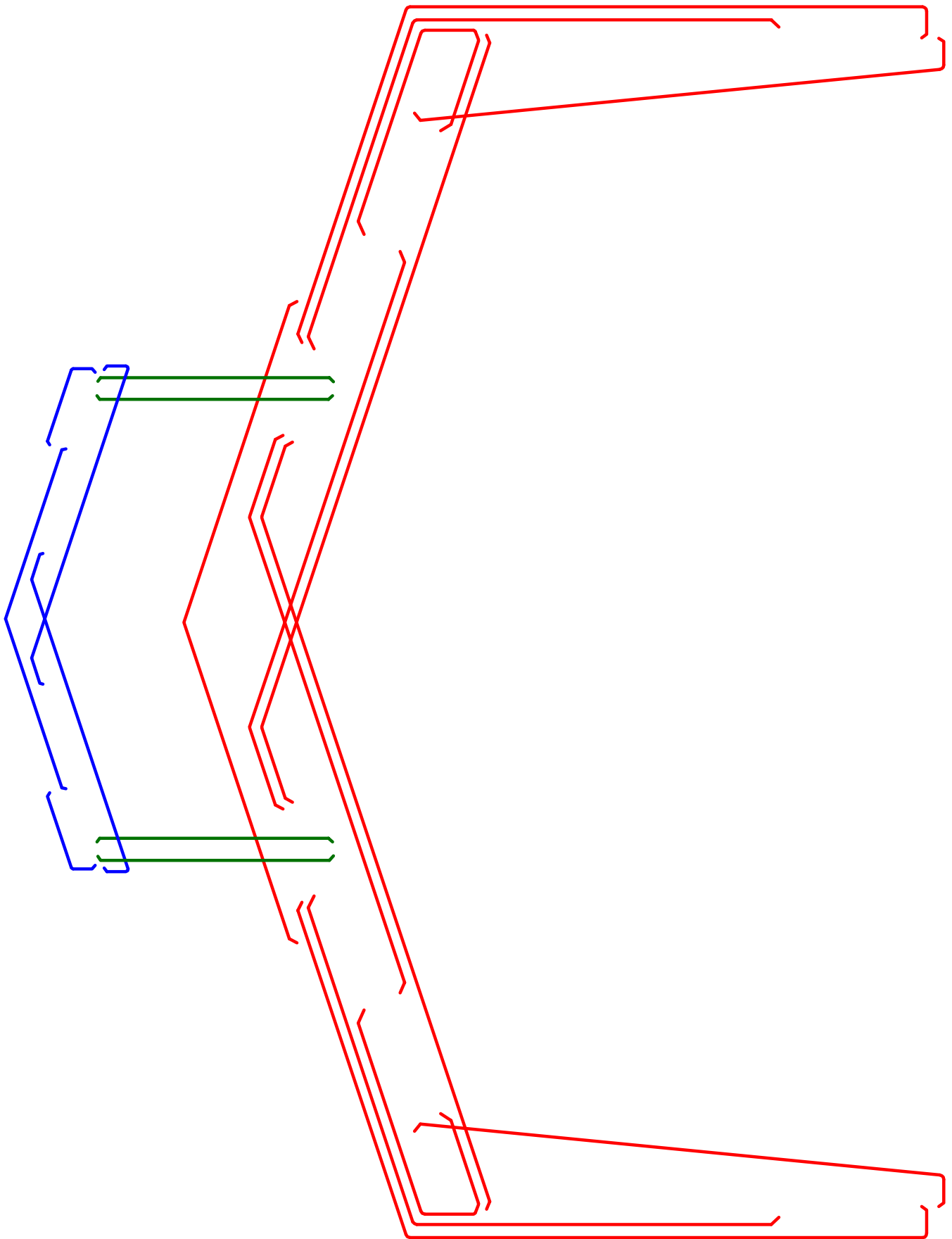
هذا الحل حل تقريبي جدا و غير دقيق ، لذا لن نستخدم هذا الحل
الا مع تعذر الوقت في الامتحان



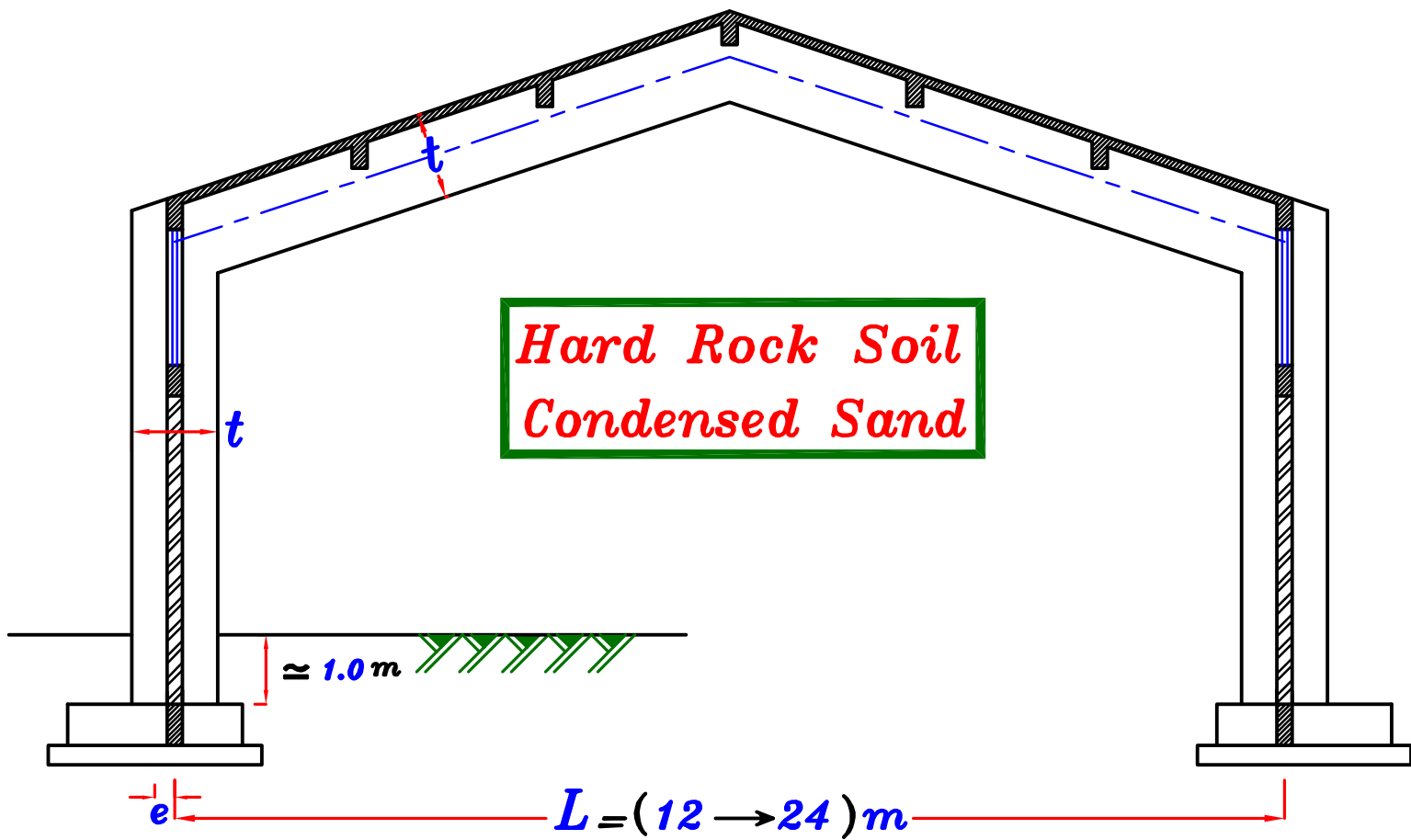






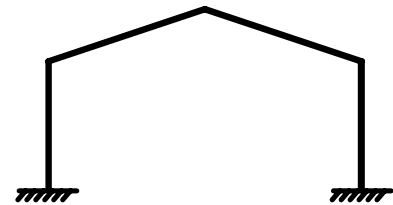


Inclined Fixed Frame.



– Statical System

The Fixed Frame is Two Times Statically indet. symmetric لانه



– Concrete Dimensions.

* $\text{Span } (L) = (12 \rightarrow 24) \text{ m}$

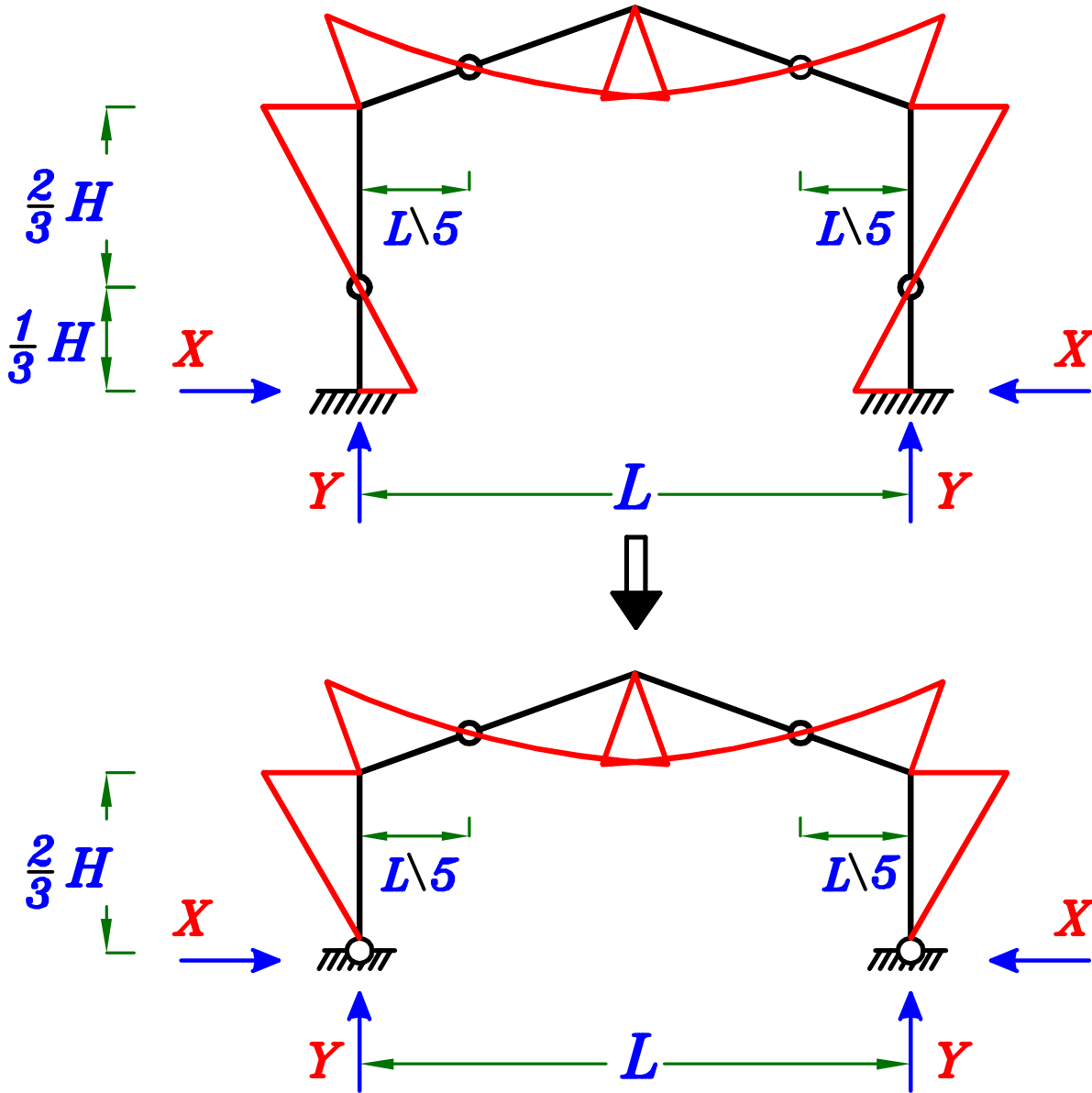
* $t \approx \frac{\hat{L}}{14 \rightarrow 16}$

* $b = \frac{0.30 \text{ m}}{\frac{\text{Spacing}}{20}}$ } الأكبر

Solving Inclined Fixed Frames.

لان ال **Fixed Inclined Frame** عليه **sway** فيكون حله بال **moment distribution** صعب جدا
ولانه **Twice statically indeterminate** فيكون حله بال **Virtual work** صعب جدا
لذا في الكليه سنضطر حله بـ **Approximate method** و هذا بالطبع حل تقريبي جدا .

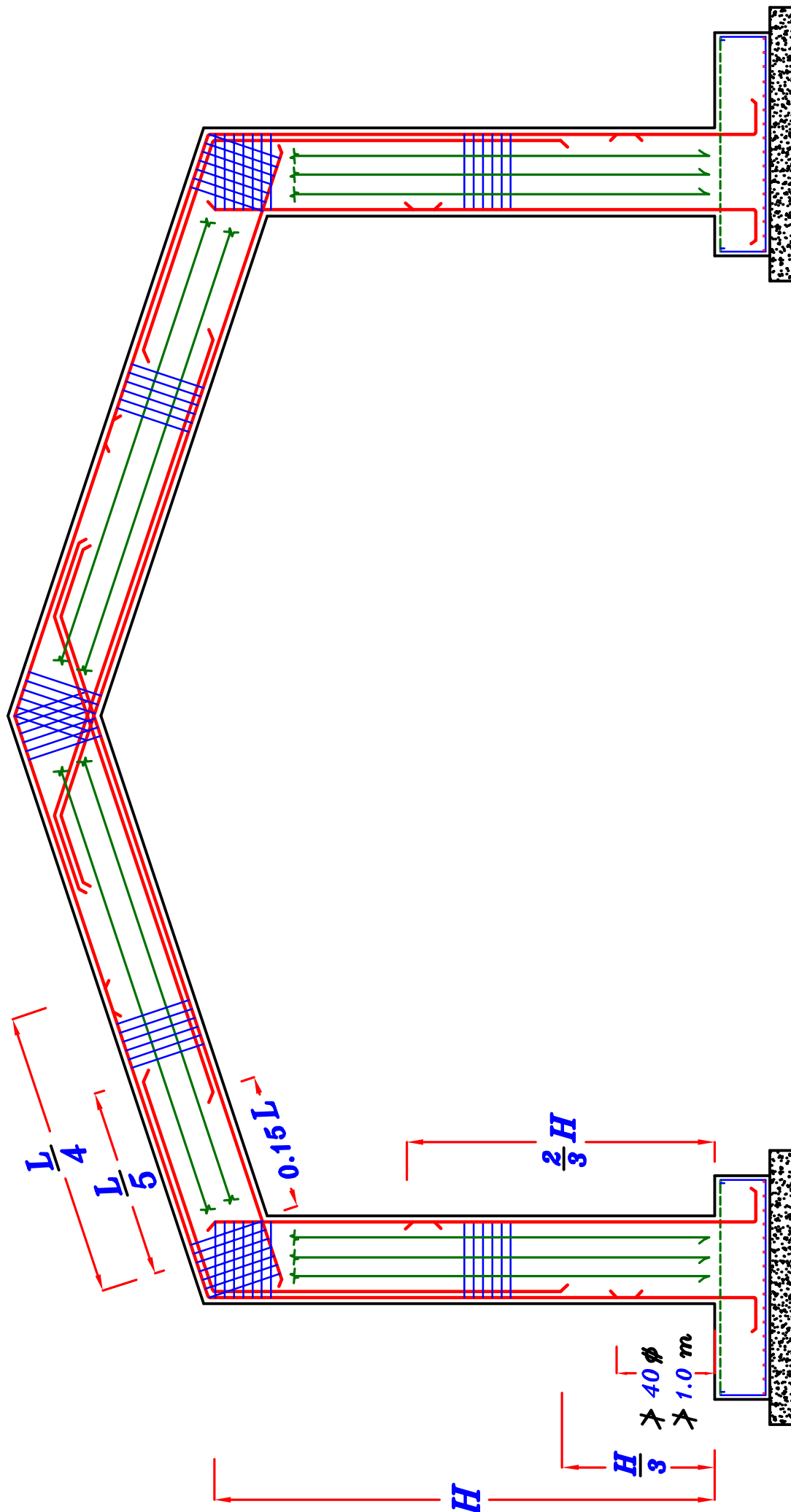
Approximate Method.

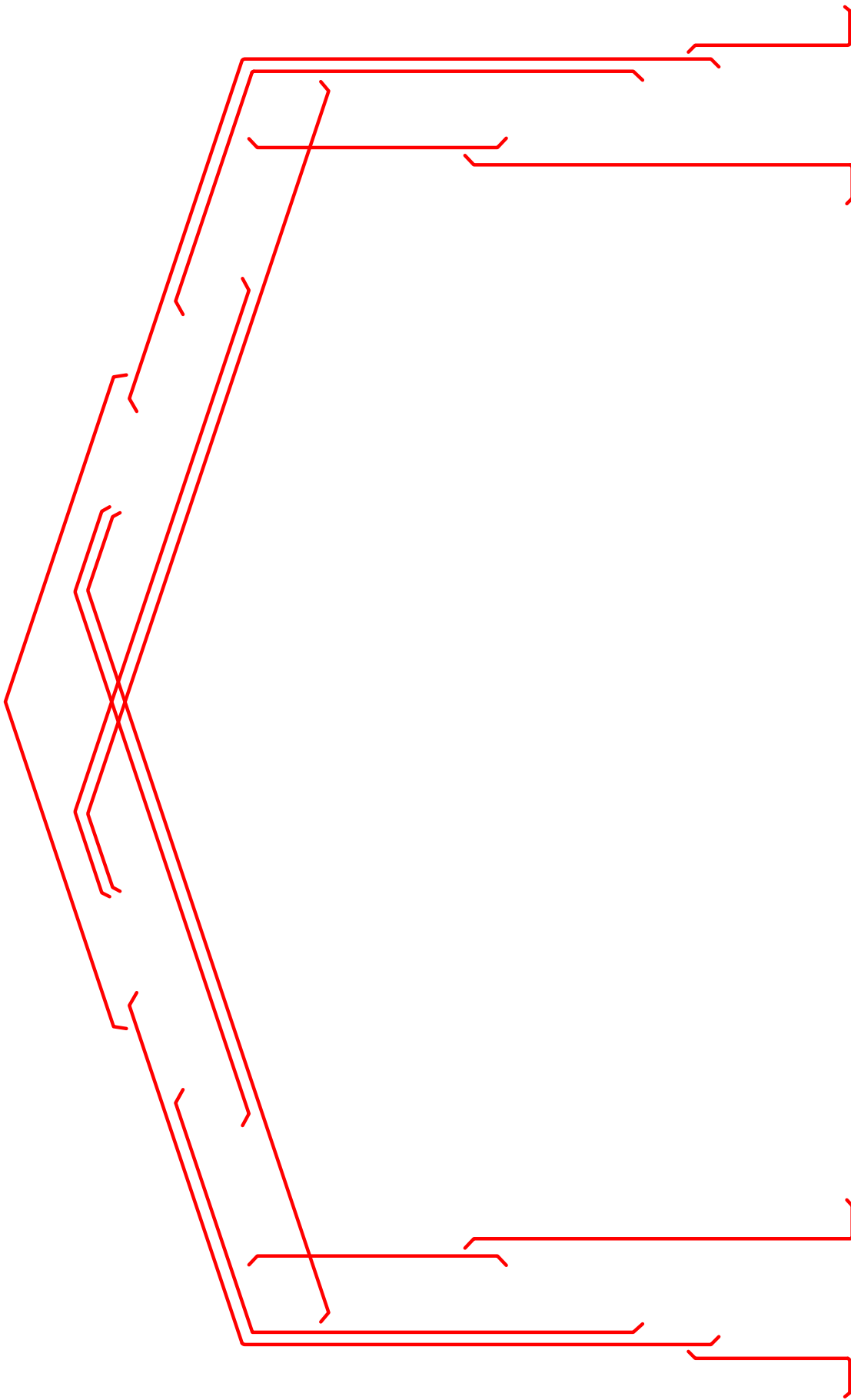


assume that in the column there is an intermediate hinge at $\frac{H}{3}$
so we can solve the Frame as Two hinged Frame but with height $\frac{2}{3}H$
assume that in the beam there is an intermediate hinge at $\frac{L}{5}$

$$Y = \frac{\sum \text{Loads}}{2}$$

To get the reactions **X** Take the moment at Point **a** = Zero





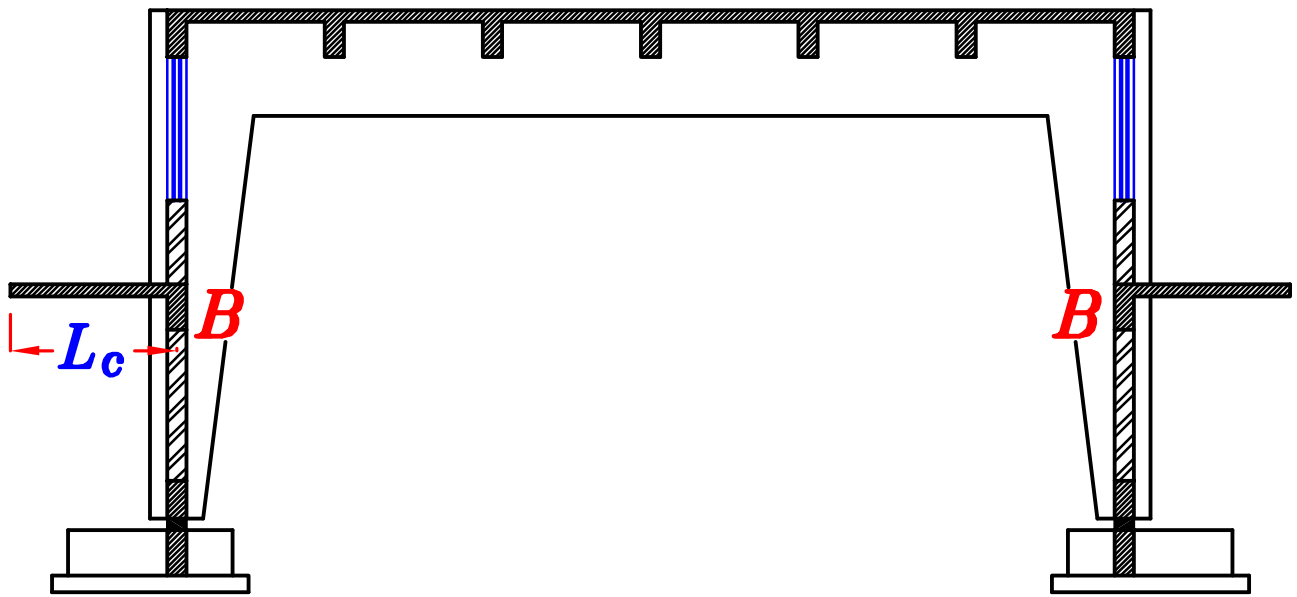
Special Case.



توجد حالتان :

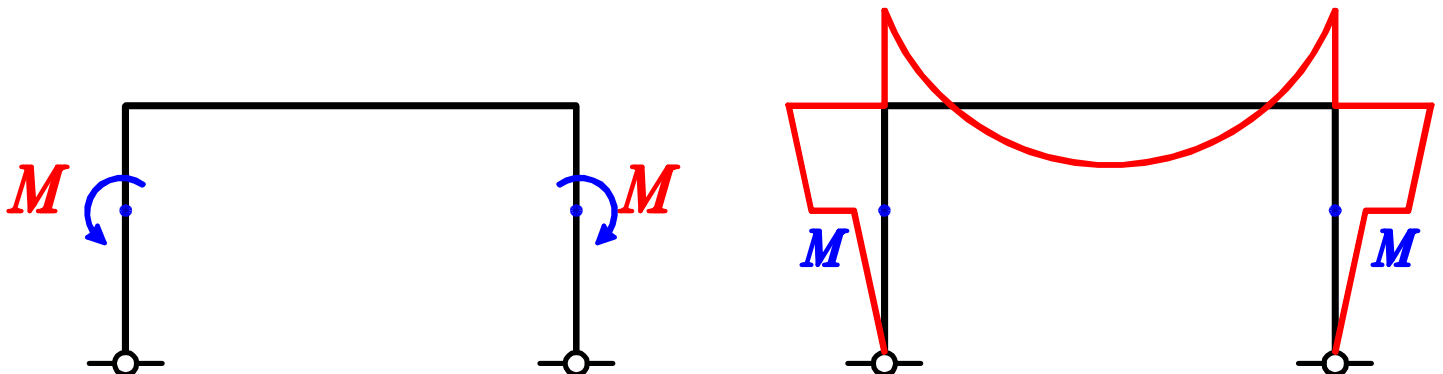
إذا وجد *cantilever* خارج من عمود ال *Frame*

$1 - IF L_c \leq 2.0 \xrightarrow{\text{Use}} \text{Cantilever Slab}$

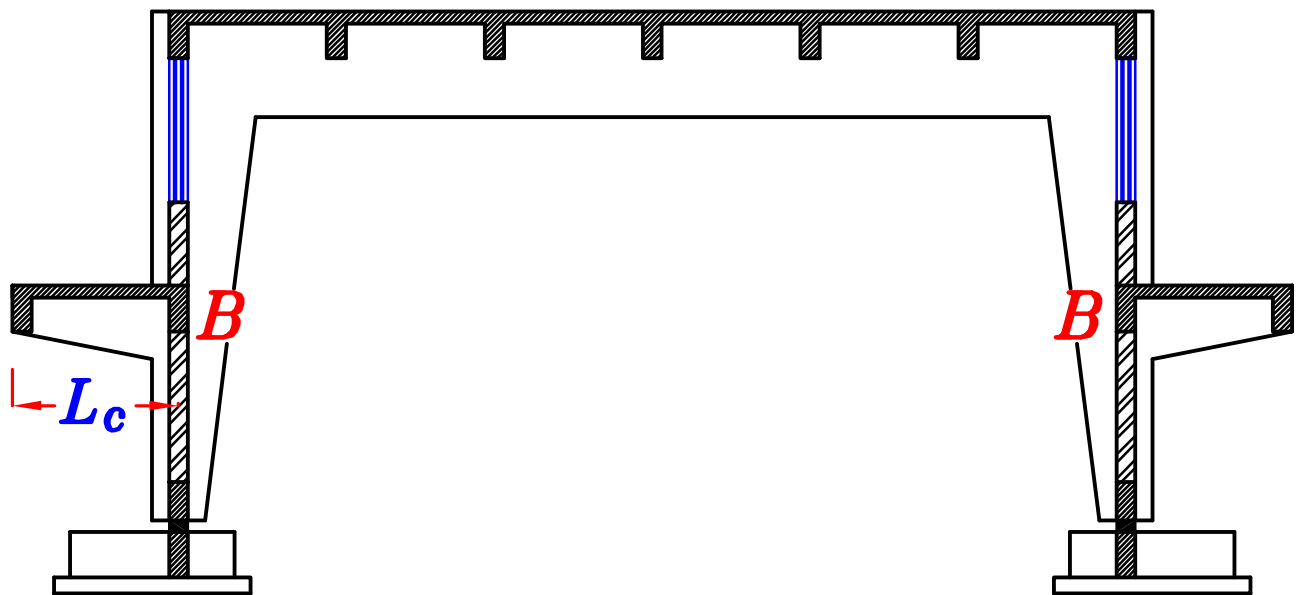


و في هذه الحالة يوجد *Torsion* على الكمره *B*
يتحول الى *Concentrated bending moment*

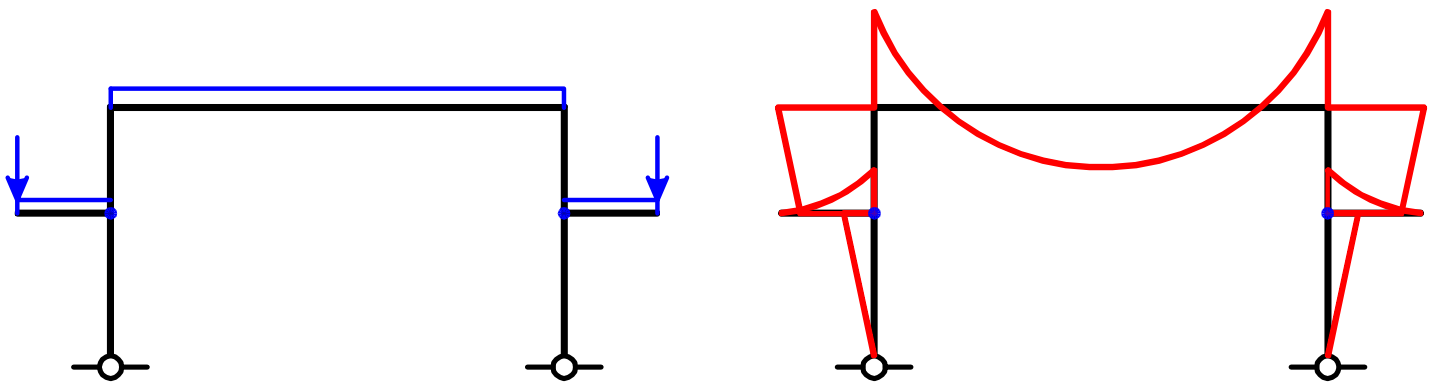
$$M = \left(\frac{w_s * L_c^2}{2} \right) * \text{Spacing} \quad \text{على عمود ال Frame}$$



$2 - IF L_c > 2.0 \xrightarrow{\text{Use}} \text{Cantilever Frame}$



و في هذه الحالة لا يوجد *Torsion* على الكمره *B*



في حالة وجود *Cantilever* سواء كان *Cantilever Slab* or *Cantilever Frame*

لن تنفع معادله *Moment distribution* $M = F.E.M. (Beam) * D.F. (Col.)$

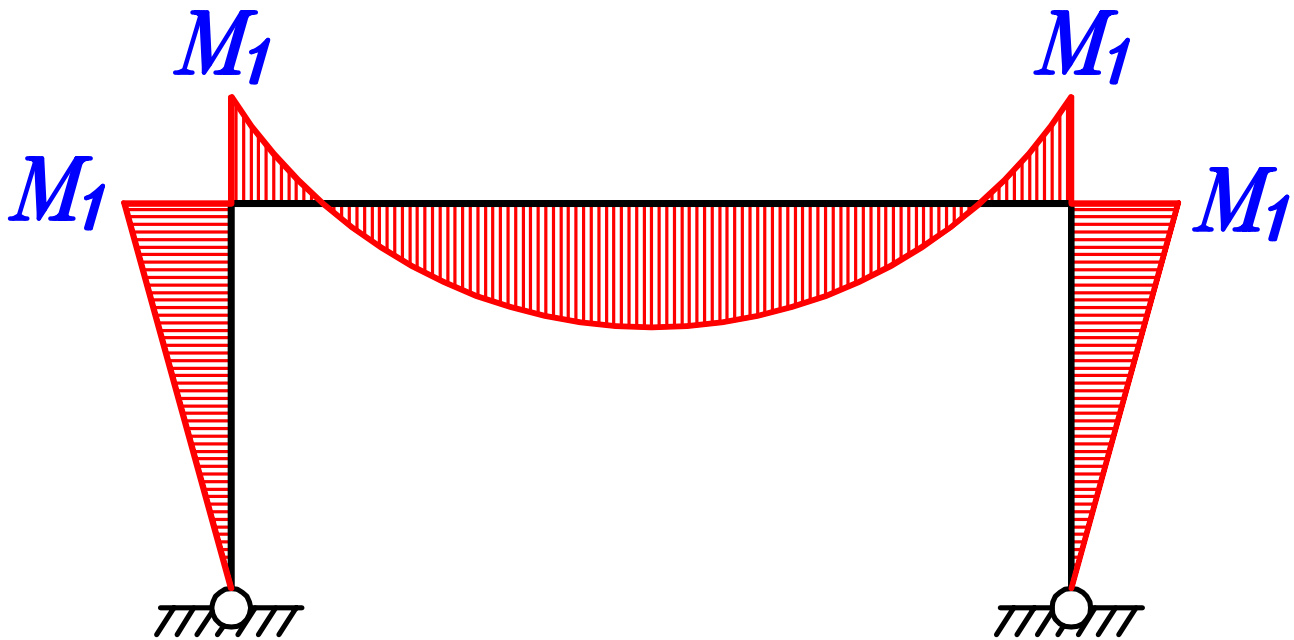
لذا سنضطر حل ال *Frame*

اما عن طريق *Moment distribution* لكن بجدول

او عن طريق *Virtual Work*

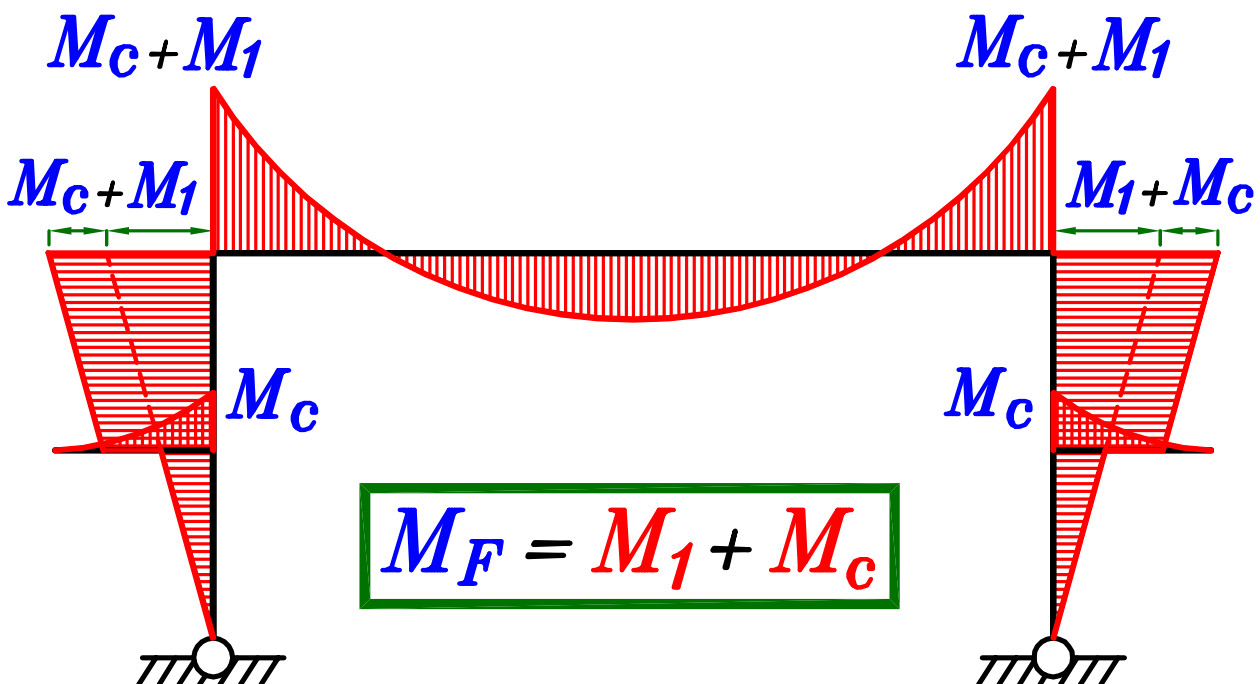
عند وجود *cantilever* خارج من ال *symetric Frame*

١- حل ال *Frame* بدون *cantilever*



$$M_1 = F.E.M. (beam) * D.F. (col.)$$

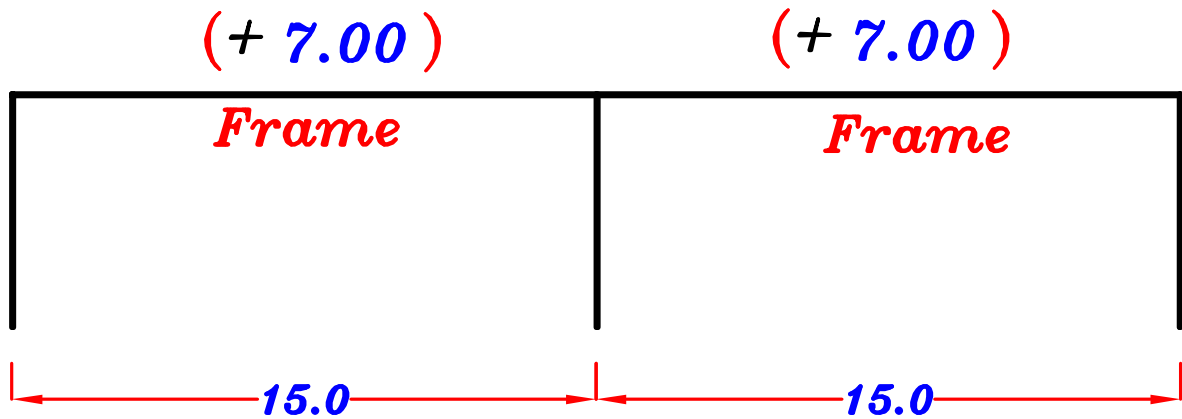
٢- حساب قيمه العزم النهاى $M_F = M_1 + M_c$



$$M_F = M_1 + M_c$$

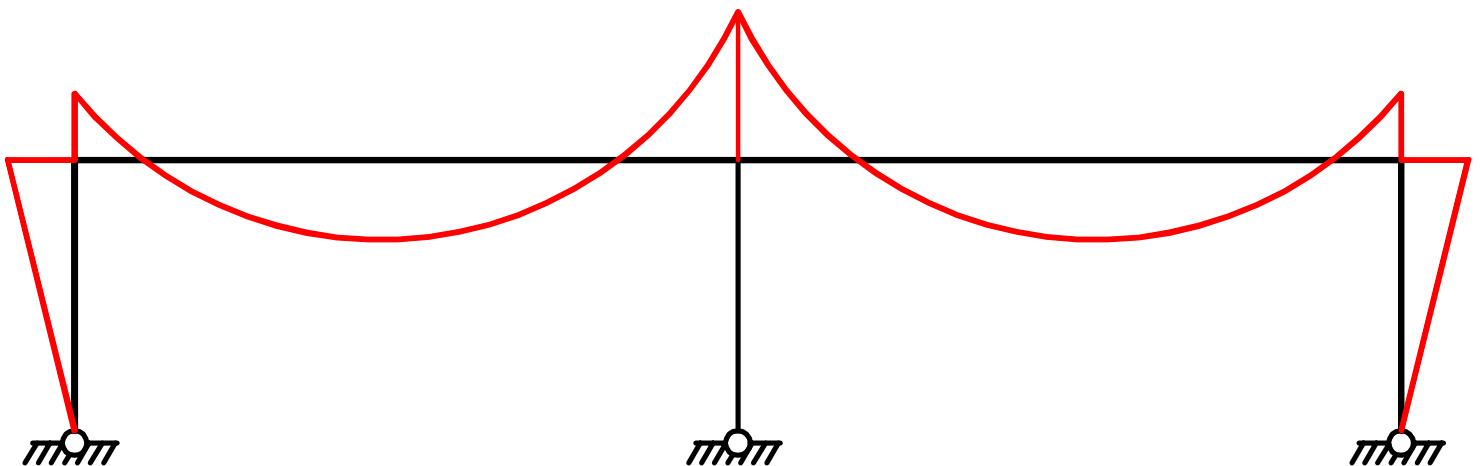
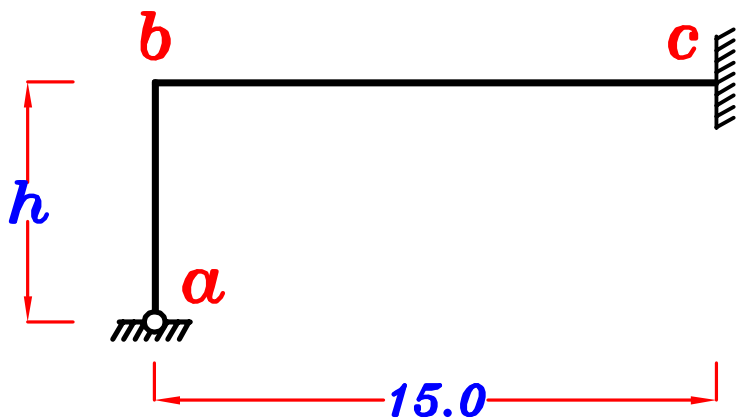
Applications Of Frames.

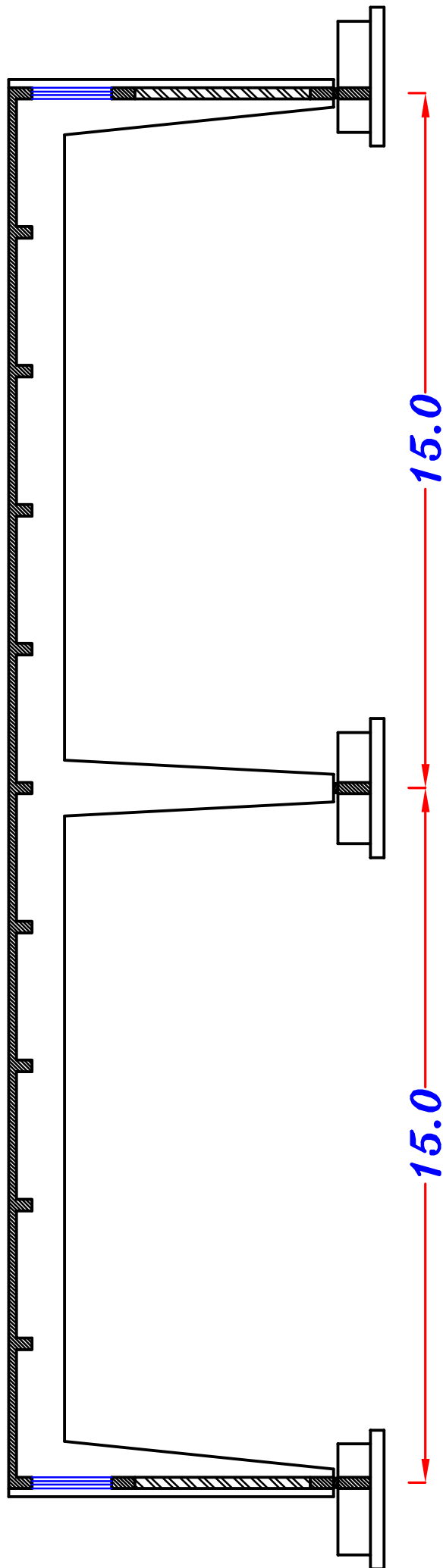
Continuous Frame.



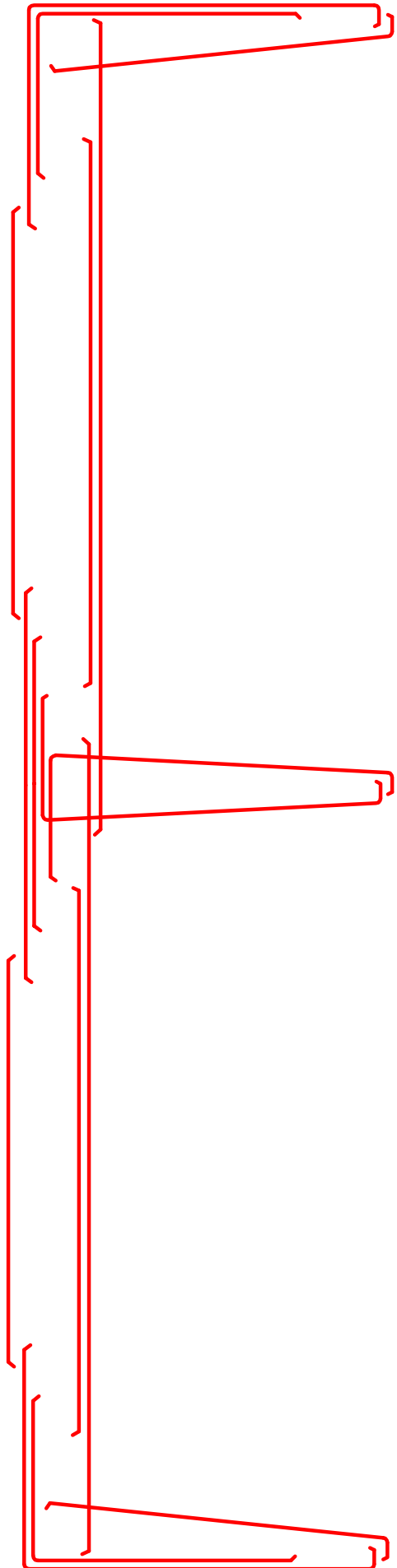
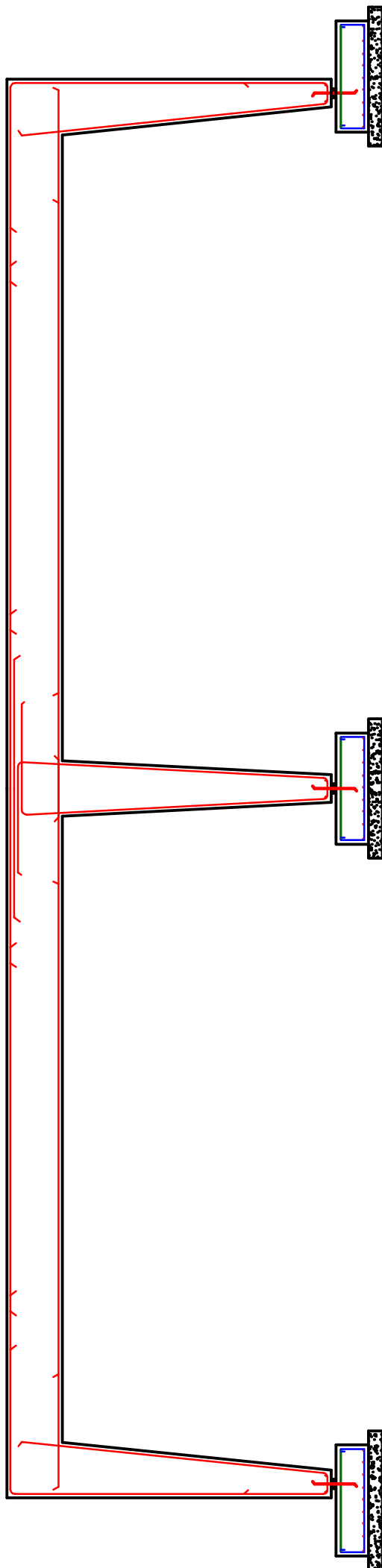
لکى نستطيع أن نحل هذا ال *Frame* بطريقه *moment distribution*
يجب أن يكون *symmetric Frame*

Joints	<i>b</i>		<i>c</i>
members	<i>b-a</i>	<i>b-c</i>	<i>c-b</i>
<i>D.F.</i>	✓	✓	—
<i>F.E.M.</i>	—	✓	✓
<i>B.M.</i>	✓	✓	—
<i>C.O.M</i>	—	—	✓
<i>B.M.</i>	—	—	—
<i>M_F</i>	✓	✓	✓





Continuous Hinged Frame



Example.

Figure (1) shows the plan of a roof covering a bus shed (**20 m * 9 m**). Four columns only are allowed and marked by **X**. Live Load plus roof Finish (**L.L. + F.C.**) = **3.0 kN/m²**

Concrete Characteristic strength is **25 MPa**

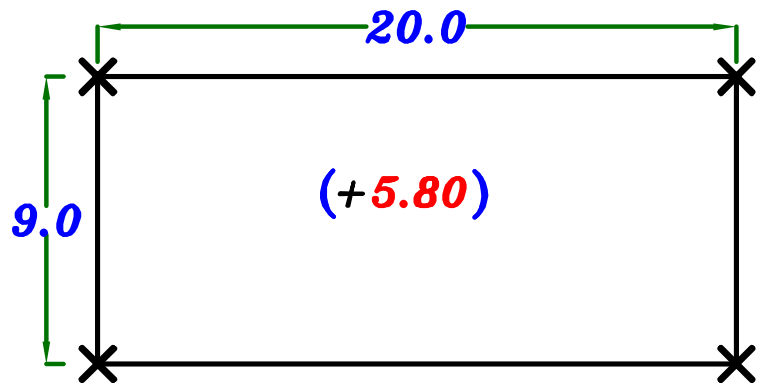
Steel grade is **400/600** For main RFT.

Steel grade is **240/350** For stirrups.

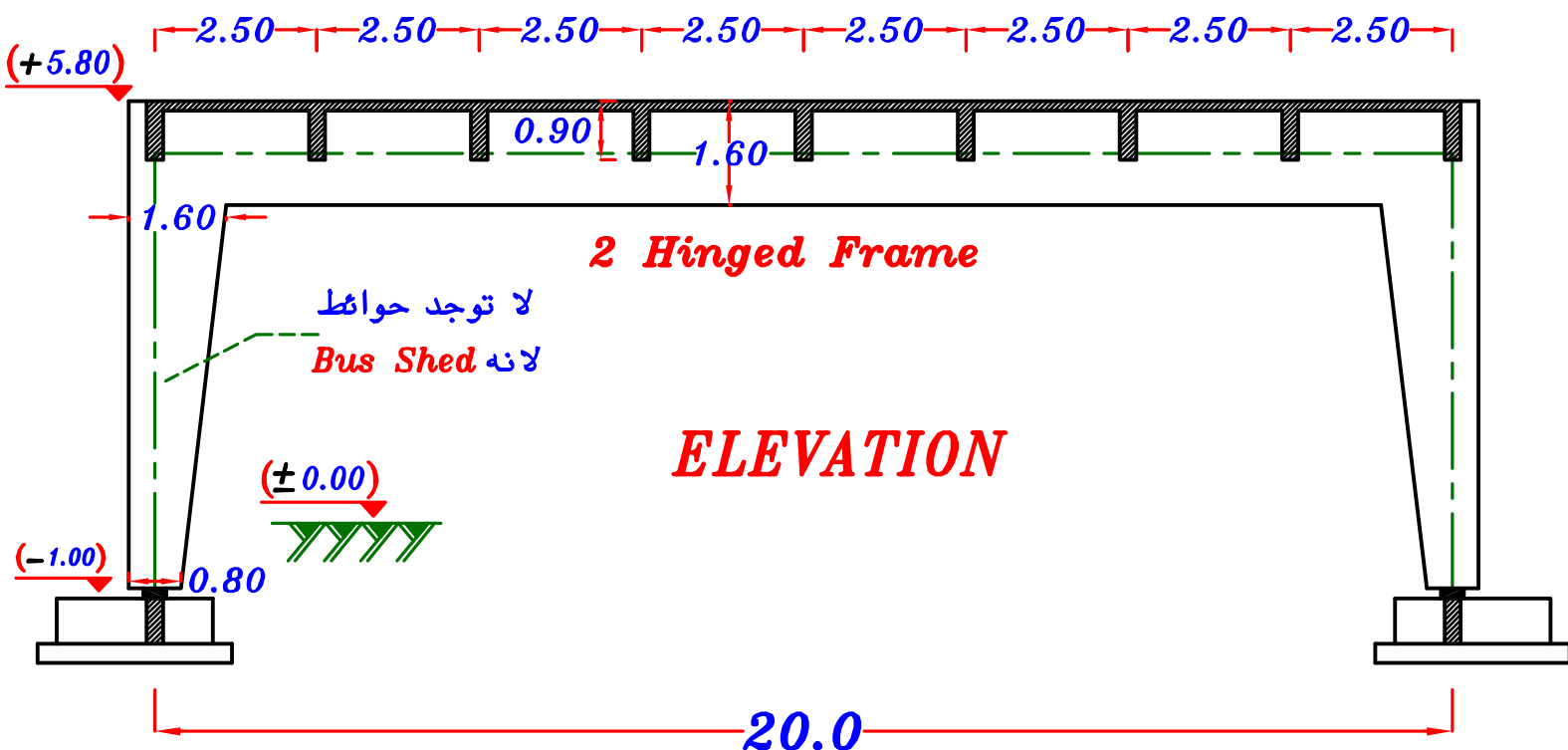
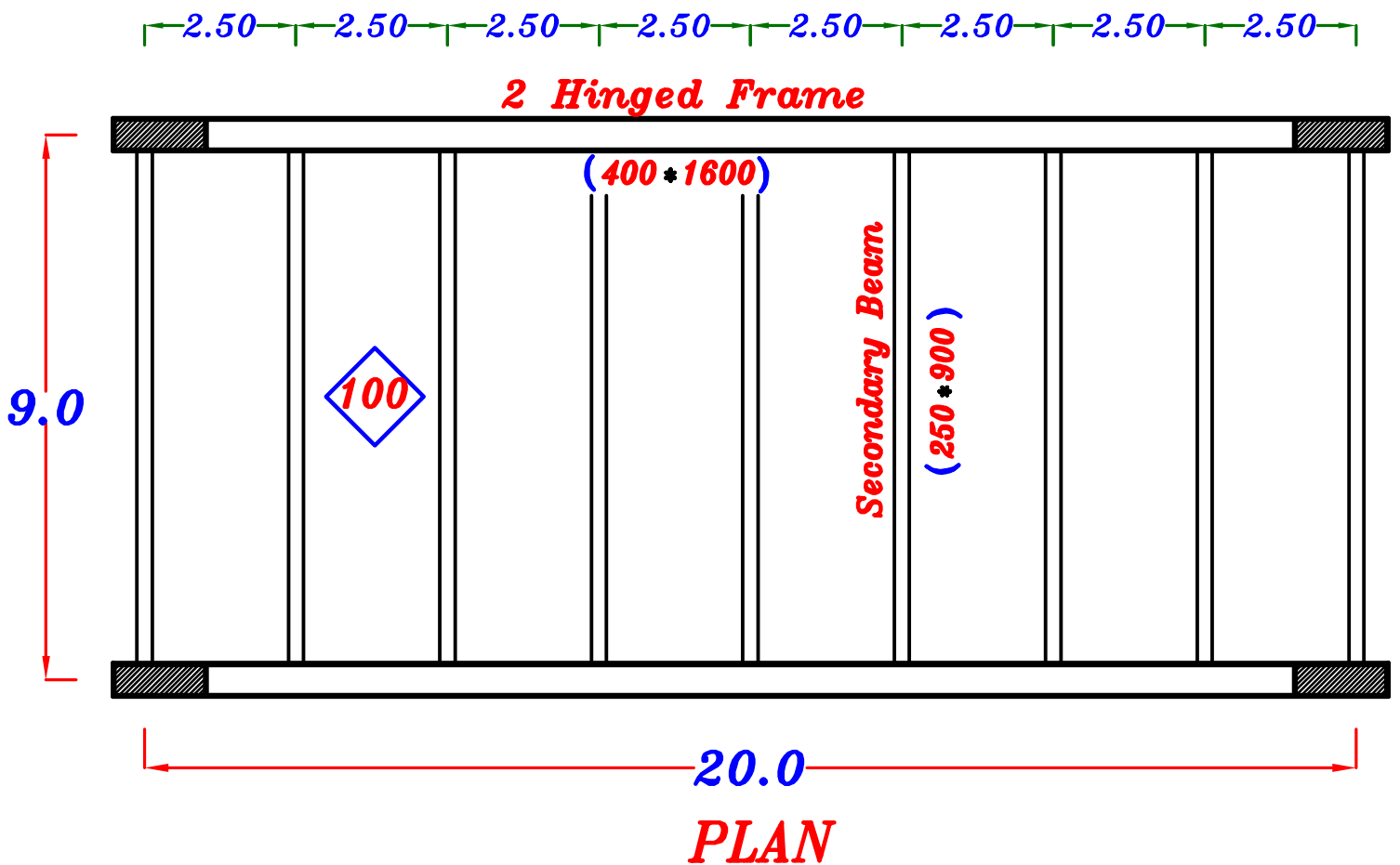
Required :

- 1** – Draw plan and elevation showing the concrete dimensions of the slabs, beams and the main supporting elements.
- 2** – Design the main supporting element.
- 3** – Draw details of RFT. For main supporting element in elevation to scale **1:50** and cross sections to scale **1:10**

Figure (1)



1 – Draw plan and elevation showing the concrete dimensions of the slabs, beams and the main supporting elements.

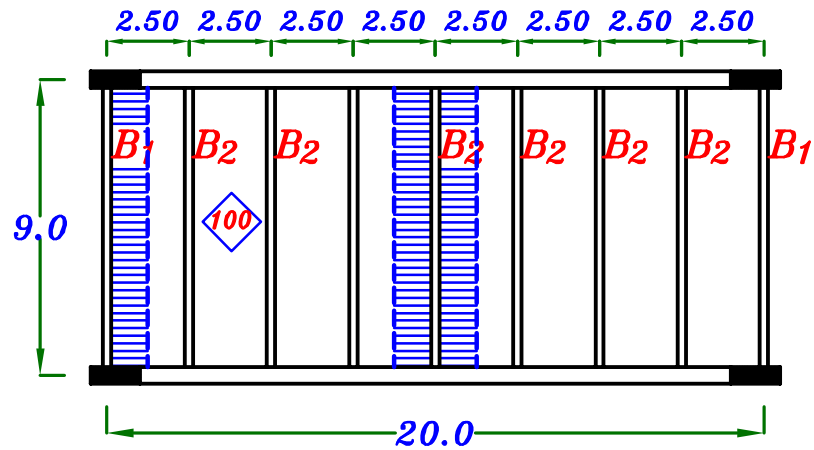


2 - Design the main supporting element.

Load Distribution.

$$t_s = \frac{2500}{30} = 83.33 \text{ mm}$$

Take $t_s = 100 \text{ mm}$



$$w_s = 1.5 (0.10 * 25 + 3.0) = 8.25 \text{ kN/m}^2$$

$$o.w. (Beam) = 1.4 b t \gamma_c = 1.4 (0.25) (0.9) (25) = 7.90 \text{ kN/m}$$

$$\underline{B_1} w_a = o.w. + w_s \frac{L_s}{2} = 7.90 + (8.25) \left(\frac{2.5}{2}\right) = 18.2 \text{ kN/m}$$

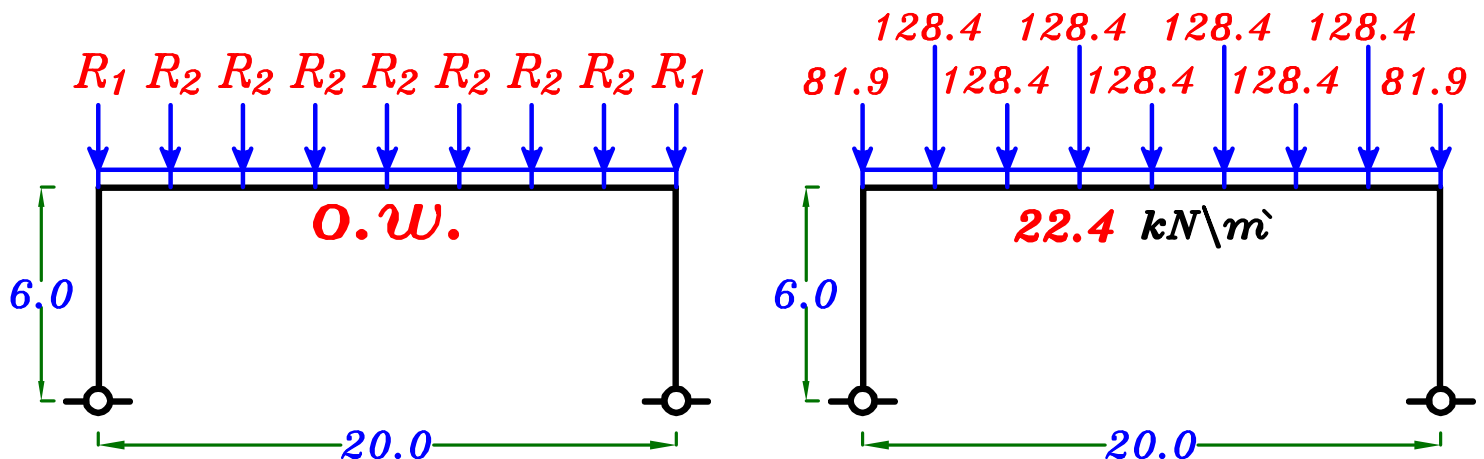
$$R_1 = 18.2 * \frac{9.0}{2} = 84.9 \text{ kN} \quad \boxed{R_1 = 81.9 \text{ kN}}$$

$$\underline{B_2} w_a = o.w. + 2 w_s \frac{L_s}{2} = 7.90 + 2 (8.25) \left(\frac{2.5}{2}\right) = 28.52 \text{ kN/m}$$

$$R_2 = 28.52 * \frac{9.0}{2} = 128.4 \text{ kN} \quad \boxed{R_2 = 128.4 \text{ kN}}$$

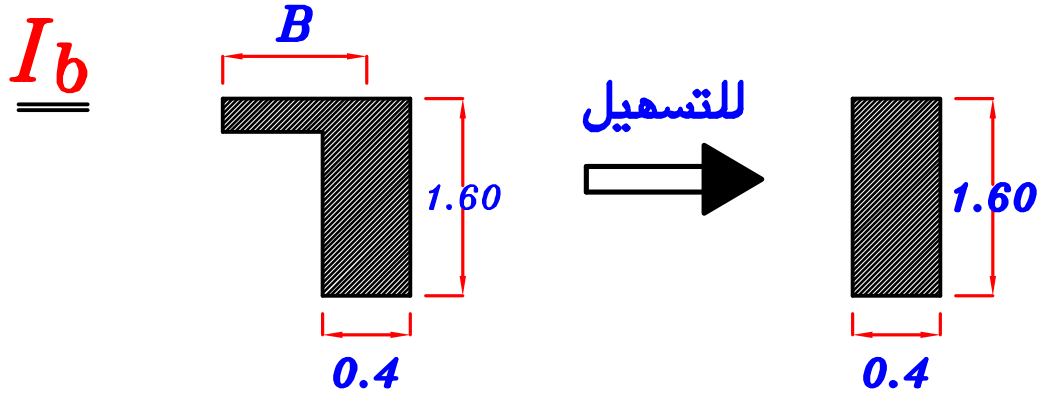
Loads on Frame.

$$o.w. (Beam) = 1.4 b t \gamma_c = 1.4 (0.40) (0.16) (25) = 22.4 \text{ kN/m}$$



Using Moment Distribution.

$$I_c = \frac{b \left(\frac{5}{6}t\right)^3}{12} = \frac{0.4 \left(\frac{5}{6} \cdot 1.60\right)^3}{12} = 0.079 \text{ m}^4$$



$$I_b = \frac{b t^3}{12} = \frac{0.4 (1.60)^3}{12} = 0.136 \text{ m}^4$$

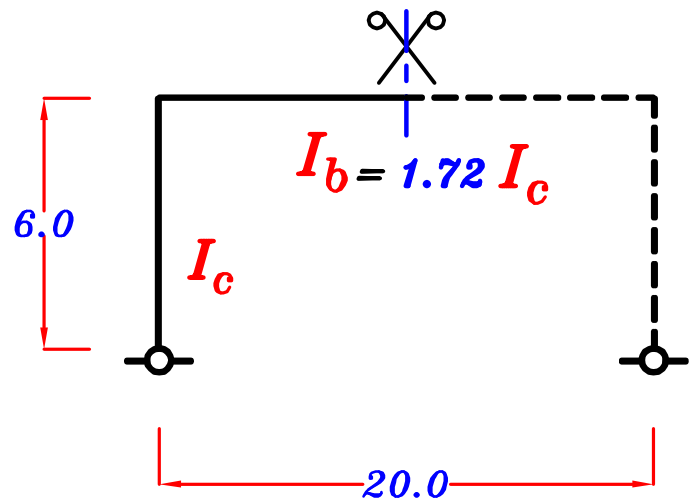
$$I_b = 1.72 I_c$$

D.F.

$$K_c = \frac{3}{4} \frac{I_c}{h} = \frac{3}{4} \cdot \frac{I_c}{6.0} = 0.125 I_c$$

$$K_b = \frac{1}{2} \frac{I_b}{L} = \frac{1}{2} \cdot \frac{(1.72) I_c}{20.0} = 0.043 I_c$$

$$D.F._c = \frac{0.125}{0.125 + 0.043} = 0.744$$



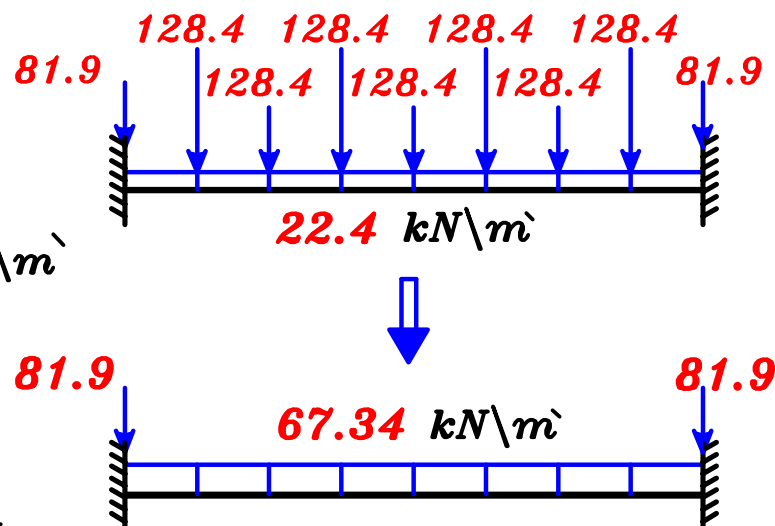
F.E.M.

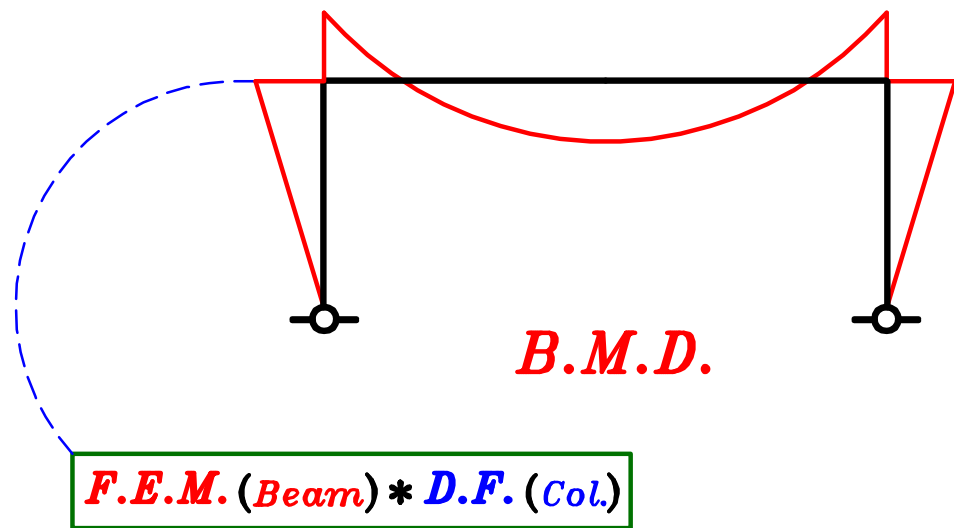
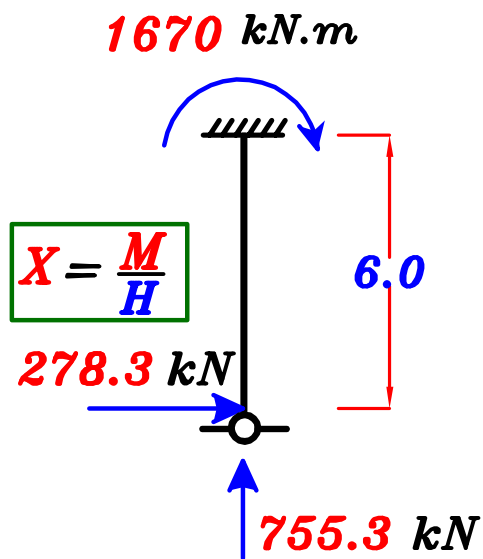
$$w = o.w. + \frac{\sum P}{\text{span}}$$

$$= 22.4 + \frac{7 (128.4)}{20.0} = 67.34 \text{ kN/m}$$

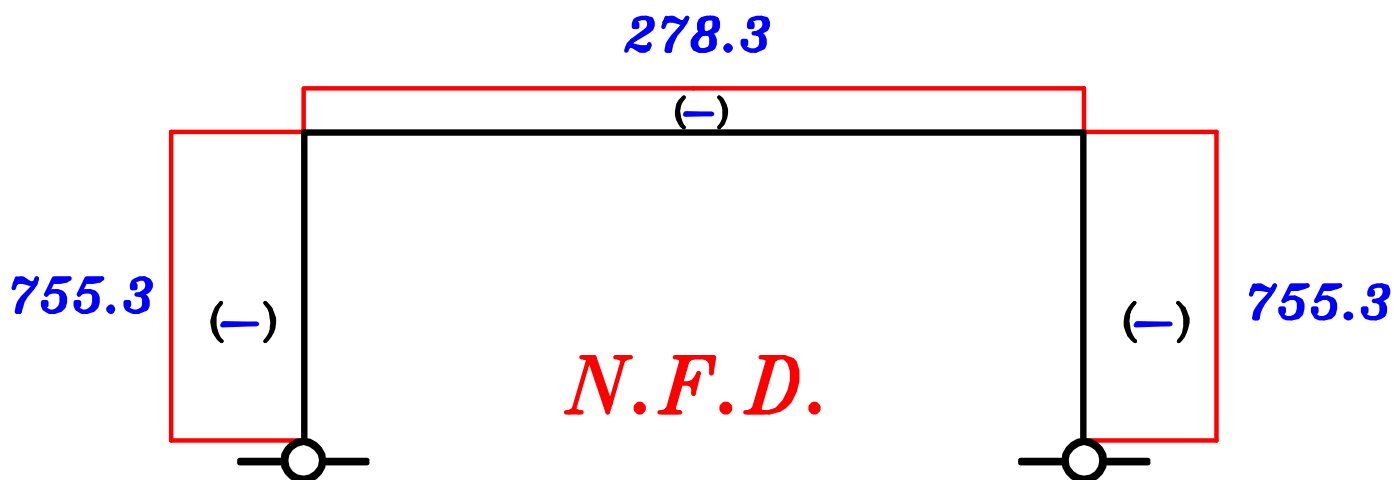
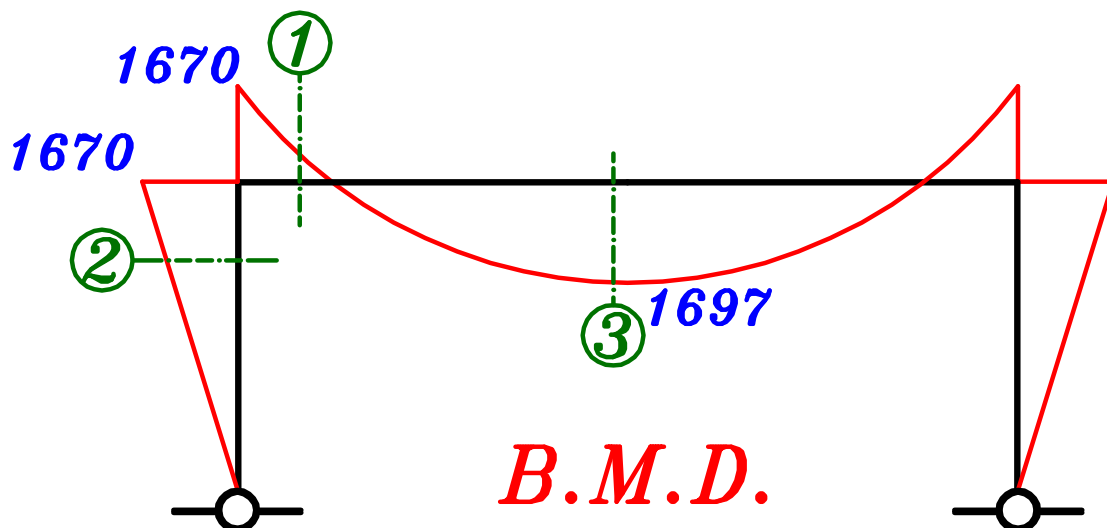
F.E.M. =

$$\frac{w L^2}{12} = \frac{67.34 \cdot (20.0)^2}{12} = 2244.6 \text{ kN.m}$$





$$2244.6 * 0.744 = 1670$$



Design of Sections.

Sec. ① R-Sec.

$$M = 1670 \text{ kN.m} , P = 278.3 \text{ kN} , b = 400 \text{ mm} , t = 1600 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{278.3 * 10^3}{25 * 400 * 1600} = 0.017 < 0.04 \text{ (neglect } P \text{)}$$

$$\therefore 1500 = C_1 \sqrt{\frac{1670 * 10^6}{25 * 400}} \rightarrow C_1 = 3.67 \rightarrow J = 0.788$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1670 * 10^6}{0.788 * 400 * 1500} = 3532.1 \text{ mm}^2$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 3532.1 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{400} \right) 400 * 1500 = 1687.5 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 3532.1 \text{ mm}^2 \quad (8 \Phi 25)$$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.0 \text{ bars}$$

Sec. ② R-Sec. Neglect Effect of Buckling.

$$M = 1670 \text{ kN.m} , P = 755.3 \text{ kN}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{755.3 * 10^3}{25 * 400 * 1600} = 0.0472 > 0.04 \text{ (Don't neglect } P \text{)}$$

$$e = \frac{M}{P} = \frac{1670}{755.3} = 2.21 \text{ m} \therefore \frac{e}{t} = \frac{2.21}{1.60} = 1.37 > 0.5 \xrightarrow{\text{use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 2.21 + \frac{1.6}{2} - 0.1 = 2.91 \text{ m}$$

$$M_s = P * e_s = 755.3 * 2.91 = 2197.92 \text{ kN.m}$$

$$\therefore 1500 = C_1 \sqrt{\frac{2197.92 * 10^6}{25 * 400}} \rightarrow C_1 = 3.20 \rightarrow J = 0.760$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \delta_s)} = \frac{2197.92 * 10^6}{0.760 * 400 * 1500} - \frac{755.3 * 10^3}{(400 \setminus 1.15)}$$

$$\text{Check } A_{s \min.} \quad A_{s \text{ req.}} = 2648.5 \text{ mm}^2 = 2648.5 \text{ mm}^2$$

$$\mu_{\min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{400} \right) 400 * 1500 = 1687.5 \text{ mm}^2$$

$$\therefore A_{s \text{ req.}} > \mu_{\min.} b d \therefore \text{Take } A_s = A_{s \text{ req.}} = 2648.5 \text{ mm}^2 \quad \textcircled{6 \Phi 25}$$

Sec. ③ L-Sec.

$$M = 1697 \text{ kN.m} , P = 278.3 \text{ kN} , b = 400 \text{ mm} , t = 1600 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{278.3 * 10^3}{25 * 400 * 1600} = 0.017 < 0.04 \text{ (neglect } P \text{)}$$

$$B = \left\{ \begin{array}{l} C.L. - C.L. = 4.50 \text{ m} = 4500 \text{ mm} \\ 6 t_s + b = 6 * 100 + 400 = 1000 \text{ mm} \\ K \frac{L}{10} + b = 0.7 * \frac{20000}{10} + 400 = 1800 \text{ mm} \end{array} \right\} \quad \textcircled{B = 1000 \text{ mm}}$$

$$\therefore 1500 = C_1 \sqrt{\frac{1697 * 10^6}{25 * 1000}} \rightarrow C_1 = 5.75 \rightarrow J = 0.826$$

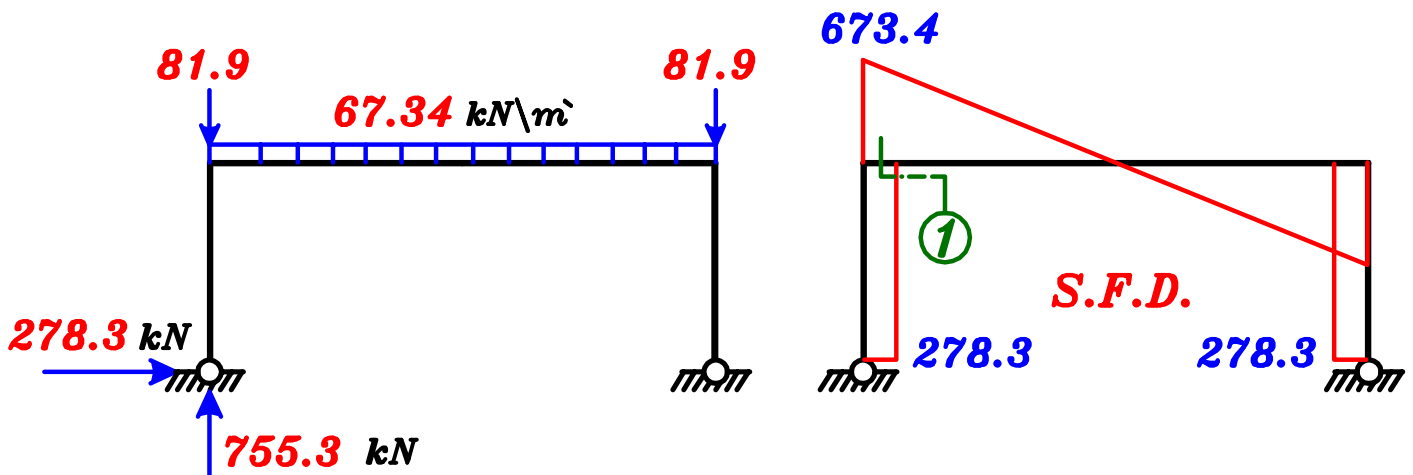
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1697 * 10^6}{0.826 * 400 * 1500} = 3424.1 \text{ mm}^2$$

$$\text{Check } A_{s \min.} \quad A_{s \text{ req.}} = 3424.1 \text{ mm}^2$$

$$\mu_{\min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{400} \right) 400 * 1500 = 1687.5 \text{ mm}^2$$

$$\therefore A_{s \text{ req.}} > \mu_{\min.} b d \therefore \text{Take } A_s = A_{s \text{ req.}} = 3424.1 \text{ mm}^2 \quad \textcircled{7 \Phi 25}$$

Check Shear.



Sec. ① $q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$

$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$

$q_u = \frac{Q_{max}}{b d} = \frac{673.4 * 10^3}{400 * 1500} = 1.12 \text{ N/mm}^2$

$\therefore q_{cu} < q_u < q_{max} \therefore$ We need Stirrups more Than $5 \phi 8 \text{ m}$

\therefore Use $q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \delta_s)}{b S}$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

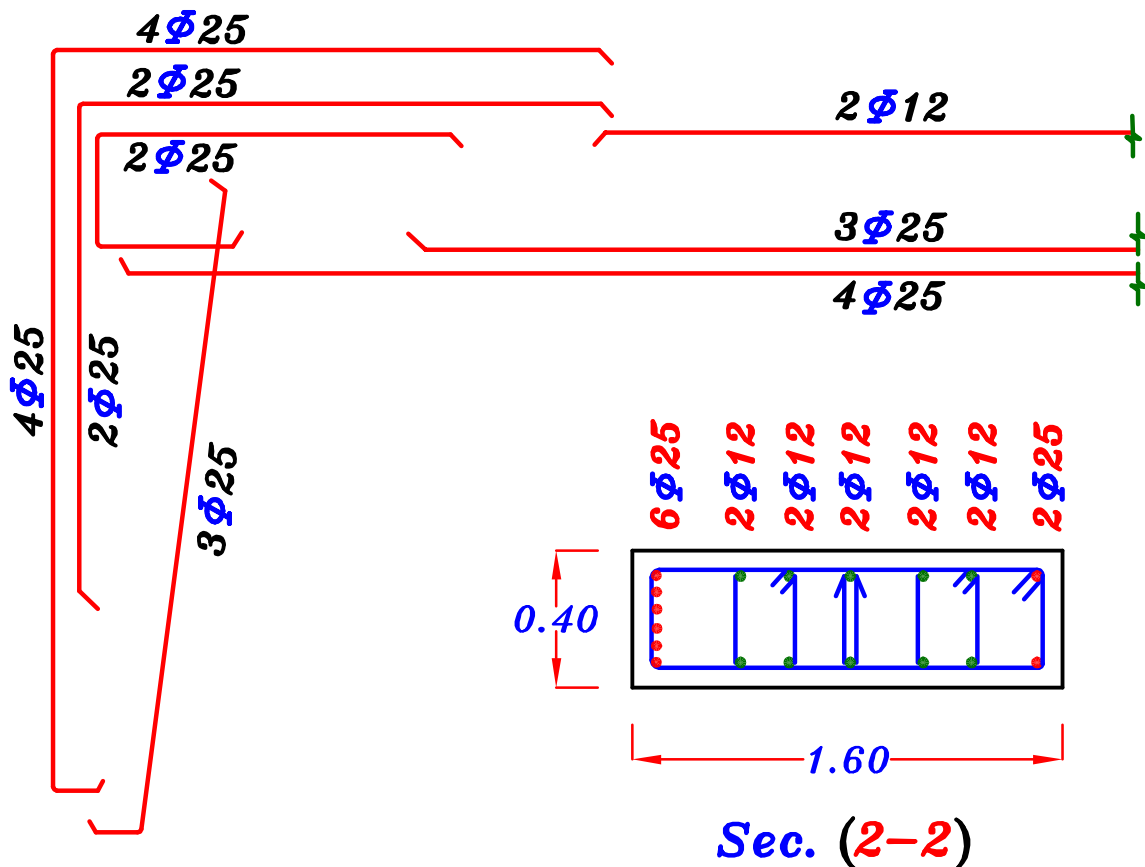
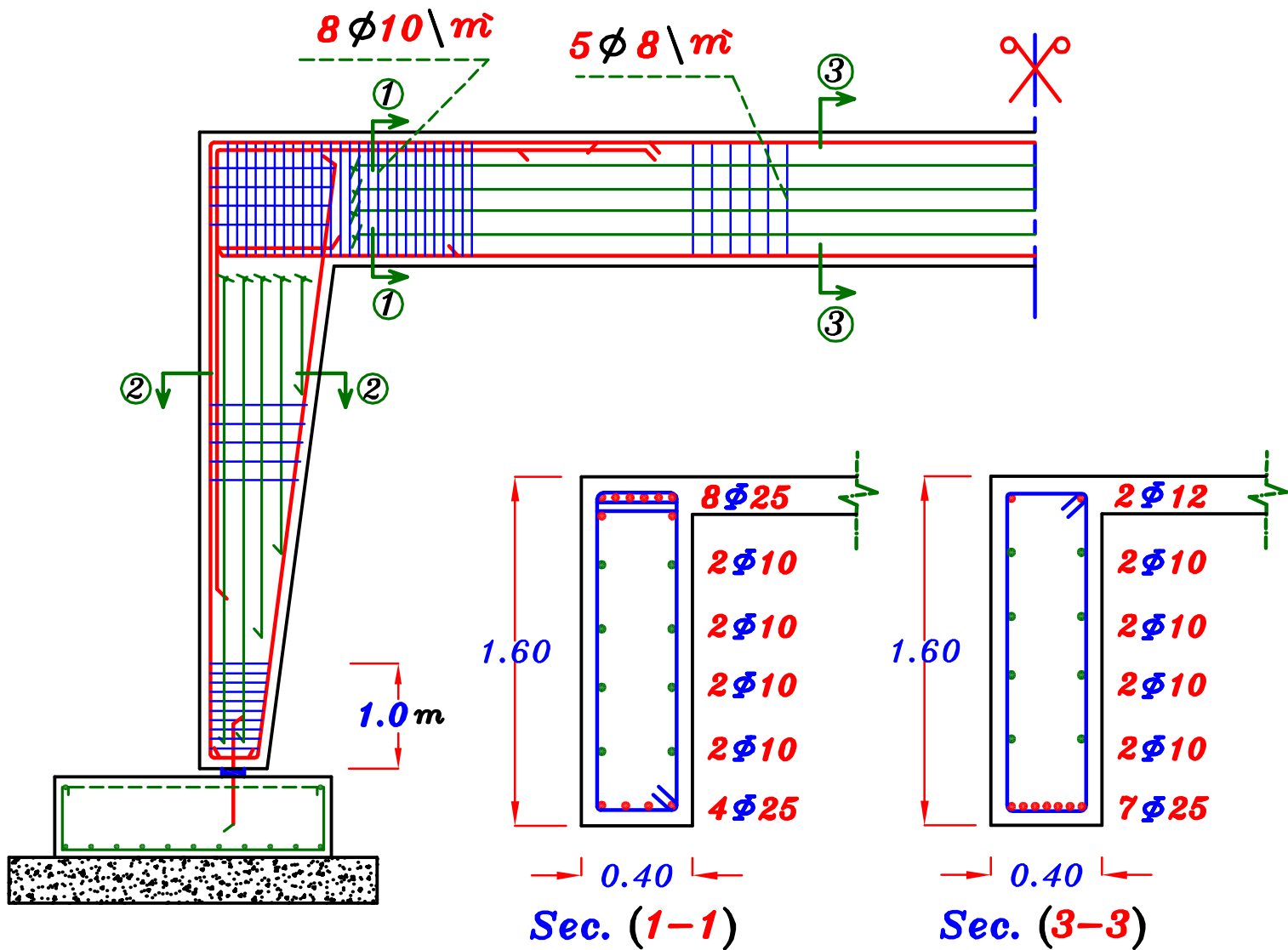
$1.12 - \frac{0.98}{2} = \frac{2 * 50.3 (240 \delta_s)}{400 * S} \rightarrow S = 83.3 \text{ mm} < 100 \text{ mm}$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

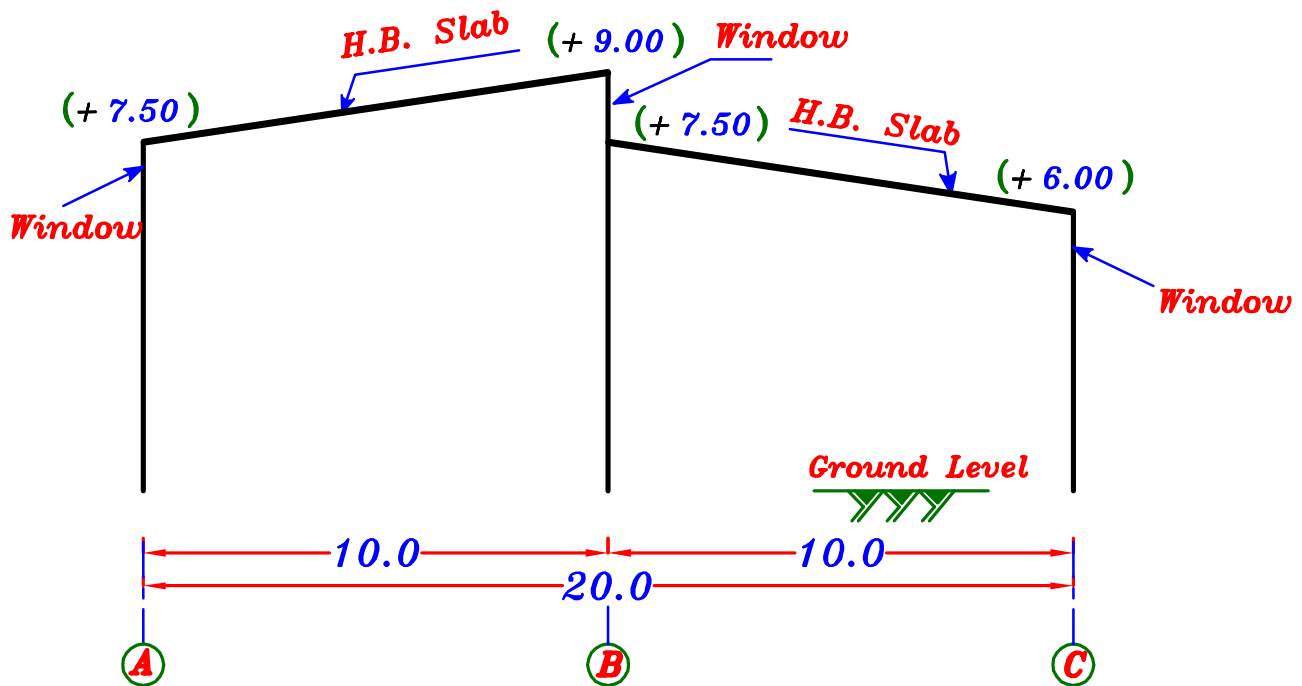
$1.12 - \frac{0.98}{2} = \frac{2 * 78.5 (240 \delta_s)}{400 * S} \rightarrow S = 130.0 \text{ mm} > 100 \text{ mm} \therefore \text{o.k.}$

\therefore No. of stirrups $\text{m} = \frac{1000}{S} = \frac{1000}{130.0} = 7.69 = 8 \text{ m}$

\therefore Use Stirrups $8 \phi 10 \text{ m}$ 2 branches



Example.



The Figure shows the cross sectional elevation of a R.C. Factory with dimensions 20.0×20.0 meters. Columns are allowed on axes **A, B & C** as shown and spaced every **5.0 m**. Covering slabs are one way Hollow-Block Slab of **5.0 m** span supported on the main supporting elements of the Factory.

$$F_{cu} = 25 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

Question 1:

Without any calculations but with reasonably concrete dimensions draw to scale **1:50** in elevation and part plan concrete dimensions of the main supporting elements of the Factory including columns & Foundations and show the arrangement of Hollow Blocks.

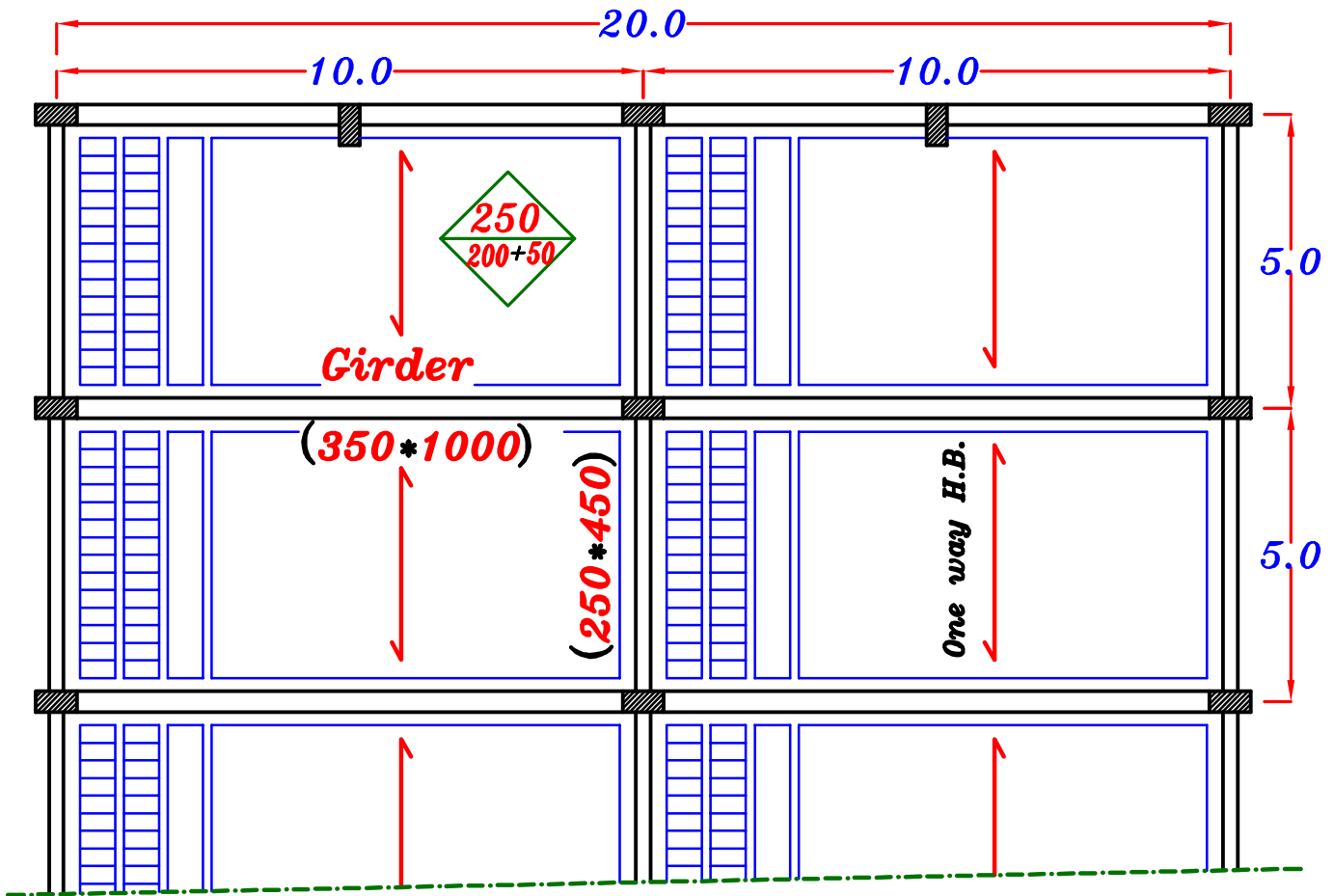
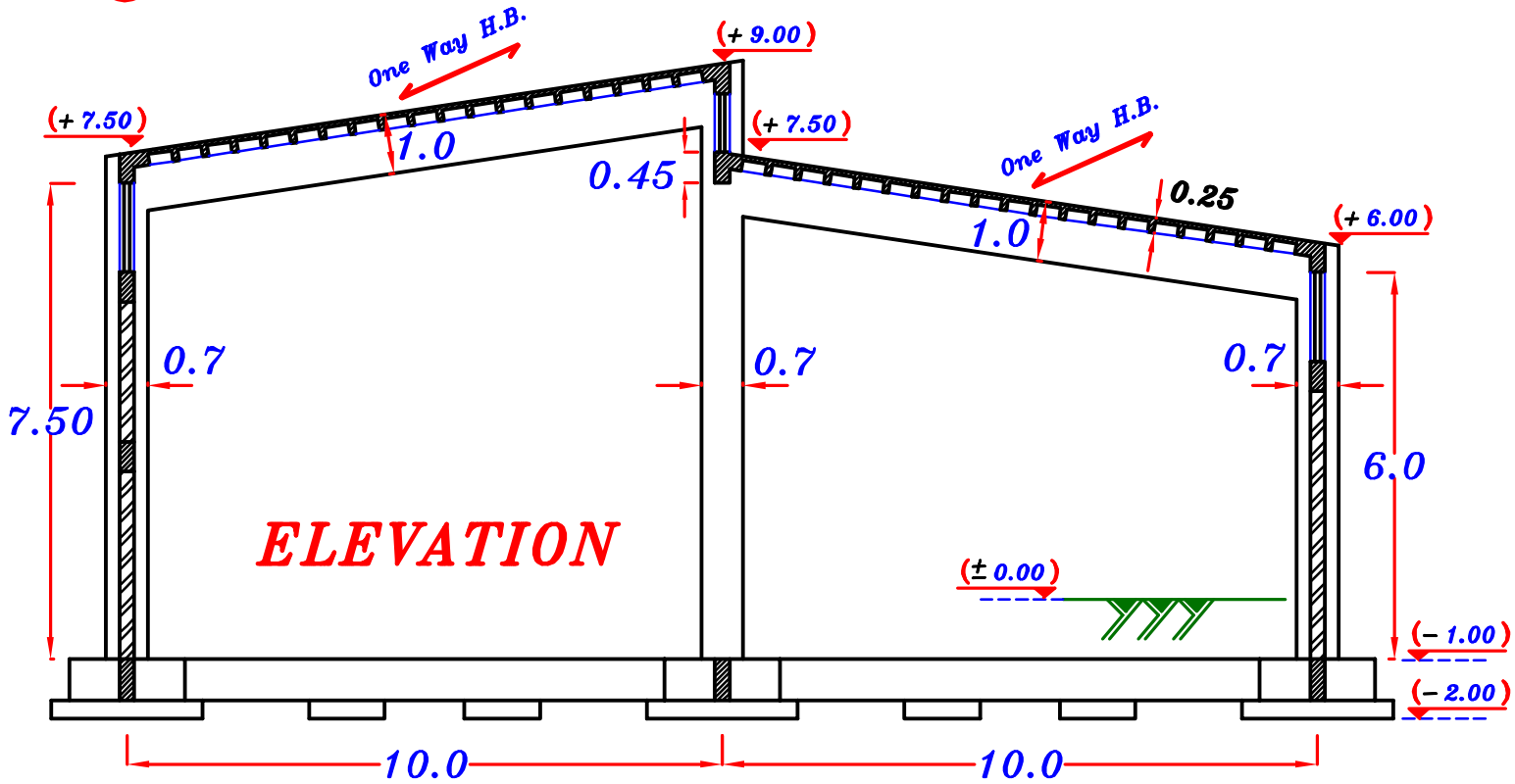
Question 2:

IF no internal columns are allowed in the Factory.

i.e. only columns at axes A & C

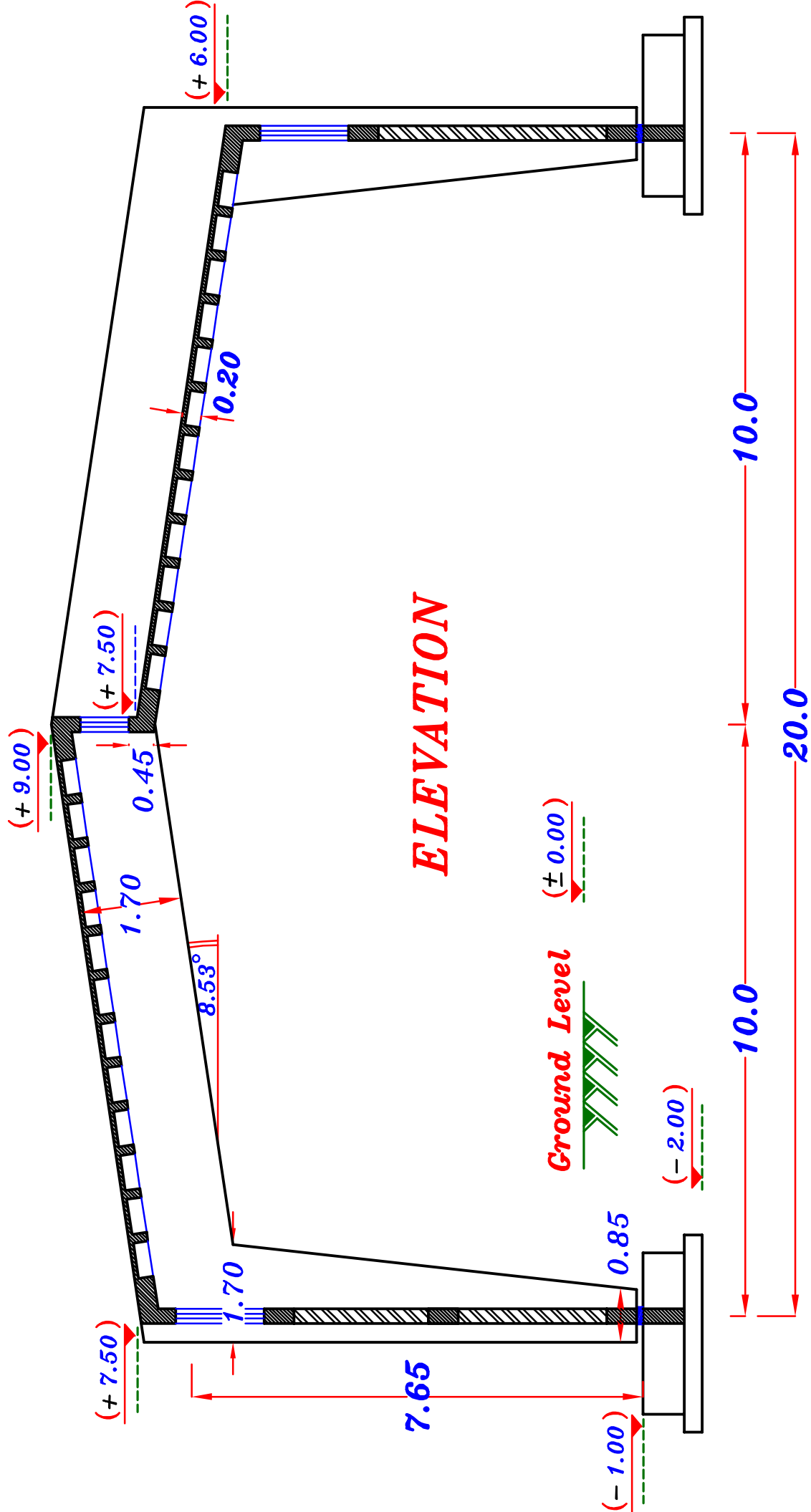
- 1- Without any calculation but with reasonably assumed concrete dimensions, draw to scale **1:50** in elevation only concrete dimensions of the main supporting element including Foundations.
- 2- Carry out load distribution and calculate the loads on the main element.
- 3- Design all sections of the main element.
- 4- Draw to scale **1:50** details of reinforcement of the main supporting element in elevation and draw the necessary cross sections to scale **1:10**
- 5- IF the slab at levels **7.50 & 9.00** become at levels **9.00 & 10.50**
Draw a new concrete dimensions in elevation.

①



② ①

Use Two Hinged Inclined Frame



② ② Loads From Slabs. (Using one way H.B. slab at 5.0 m)

∴ The Roof is inclined Take $F.C. = 0.50 \text{ kN/m}^2$, $L.L. = 0.50 \text{ kN/m}^2$

$$t = \frac{5000}{25} = 200 \text{ mm}$$

$$t = 200 \text{ mm}$$

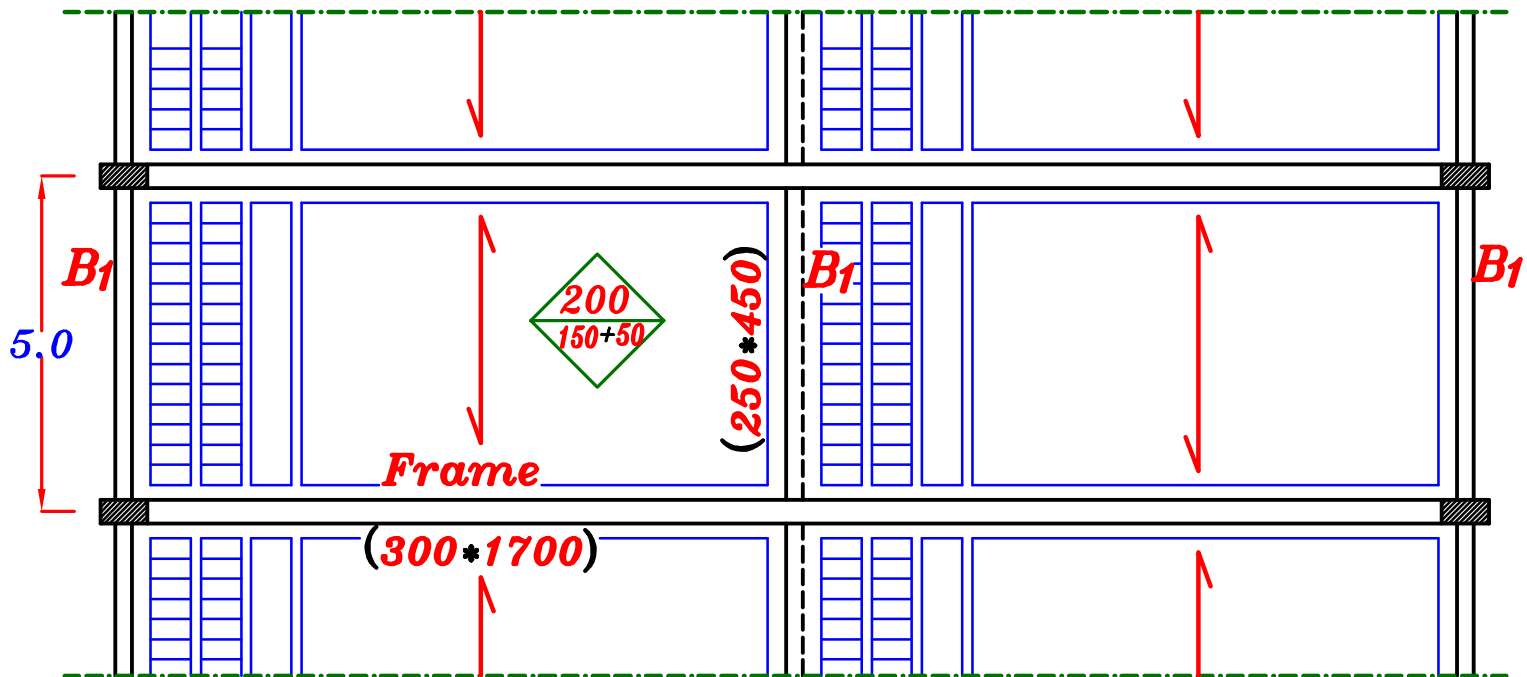
$$t_s = 50 \text{ mm}$$

$$h = 150 \text{ mm}$$

Weight of Block = 100 N , $S = e + b = 0.4 + 0.1 = 0.5 \text{ m}$

$$W_{ribi} = [1.4(t_s \delta_c + F.C.) + 1.6(L.L.) \cos \theta] (S * 1.0) + 1.4(b h * 1.0 \text{ m} * \delta_c) + 1.4 * (\text{Block وزن}) \left(\frac{1.0}{a}\right)$$

$$\therefore W_{ribi} = [1.4(0.05 * 25 + 0.5) + 1.6(0.5) \cos 8.53^\circ] (0.50 * 1.0) + 1.4(0.10 * 0.15 * 1.0 * 25) + 1.4\left(\frac{100}{1000}\right)\left(\frac{1.0}{0.2}\right) = 2.84$$



Loads on Beam B1

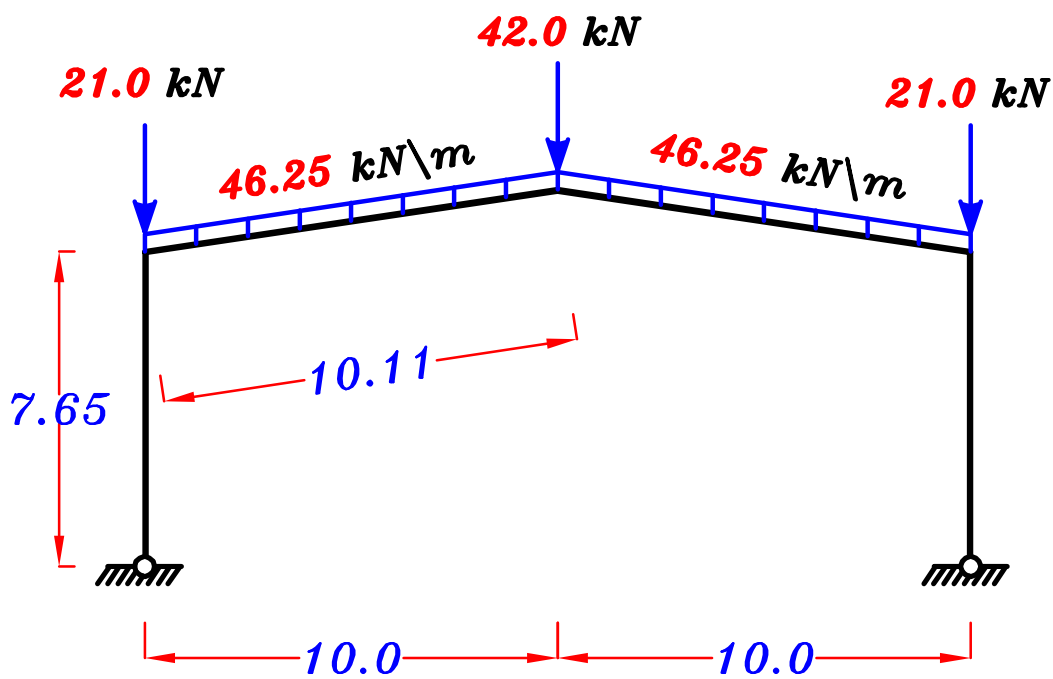
$$w = o.w. = 1.4 * 3.0 = 4.20 \text{ kN/m}$$

$$R_1 = w * S = 4.20 * 5.0 = 21.0 \text{ kN}$$

Loads on Frame F

$$o.w.(\text{Frame}) = 1.4(0.30 * 1.70 * 25) = 17.85 \text{ kN/m}$$

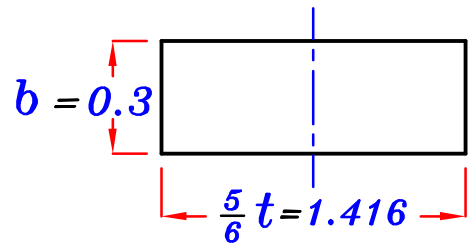
$$w = o.w. + \frac{W_{ribi}}{S} * L_s = 17.85 + \frac{2.84}{0.5} * 5.0 = 46.25 \text{ kN/m}$$



$$\underline{\underline{I_c}}$$

$$I_c = \frac{b \left(\frac{5}{6} t \right)^3}{12} = \frac{0.3 \left(\frac{5}{6} \cdot 1.70 \right)^3}{12}$$

$$= 0.071 \text{ m}^4$$



$$\underline{\underline{I_b}}$$

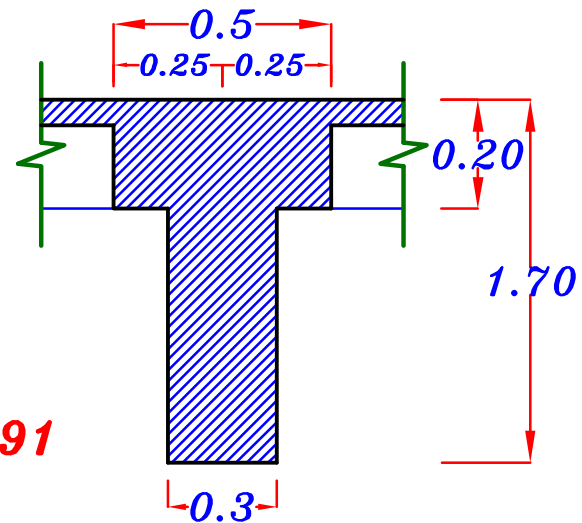
$$I_1 = (\mu \cdot 10^{-4}) B t^3$$

$$b = 0.30 \text{ m}, \quad t_s = 0.20 \text{ m}$$

$$B = 0.50 \text{ m}, \quad t = 1.70 \text{ m}$$

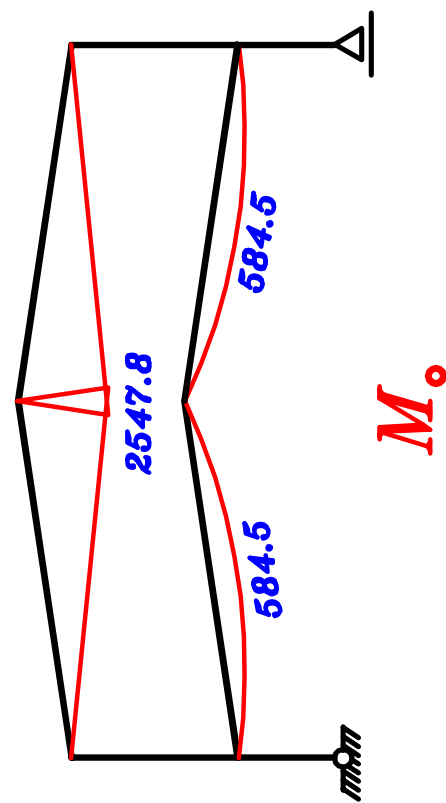
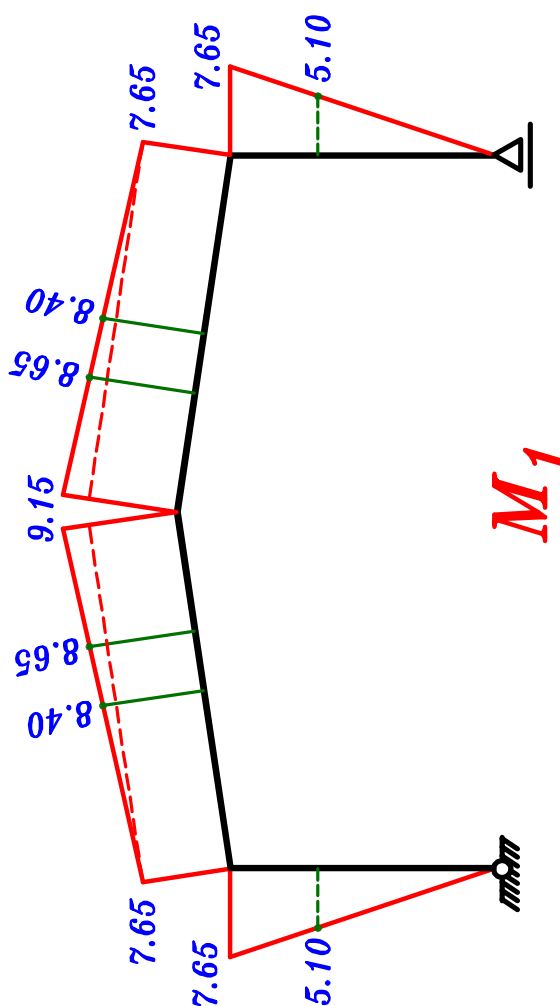
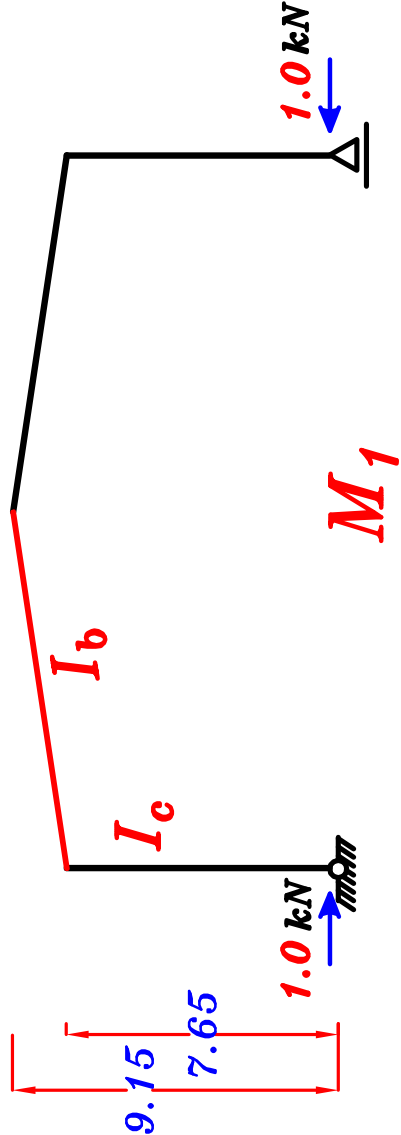
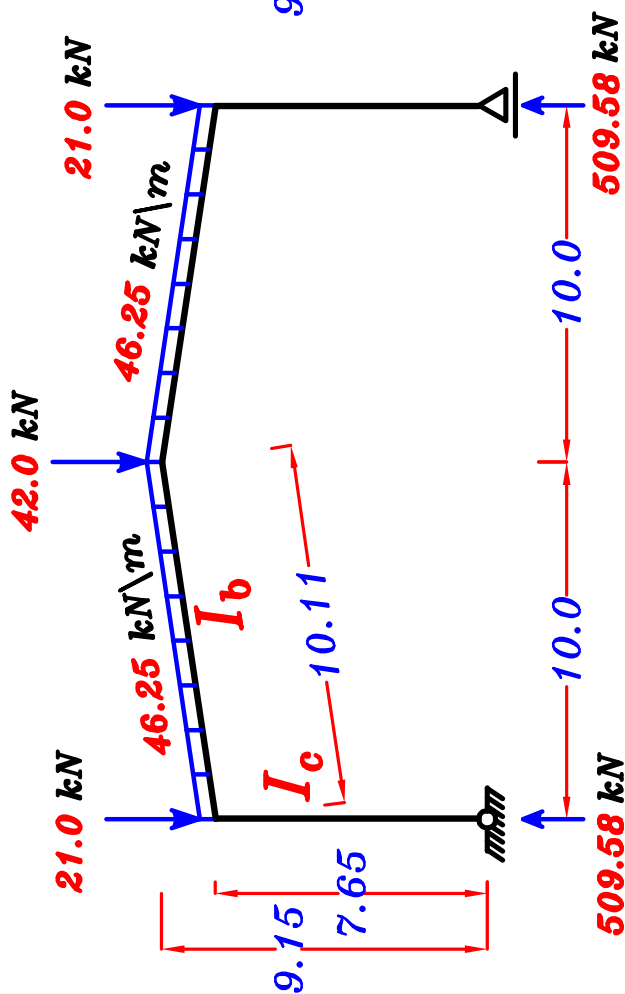
$$\frac{t_s}{t} = \frac{0.20}{1.70} = 0.117 \quad \left. \vphantom{\frac{t_s}{t}} \right\} \text{From Tables page 91}$$

$$\frac{b}{B} = \frac{0.30}{0.50} = 0.60 \quad \left. \vphantom{\frac{b}{B}} \right\} \mu = 606$$



$$I_b = (\mu \cdot 10^{-4}) B t^3 = (606 \cdot 10^{-4} \cdot 0.50 \cdot 1.70^3) = 0.149 \text{ m}^4$$

$$\therefore \boxed{I_b = 2.10 I_c}$$



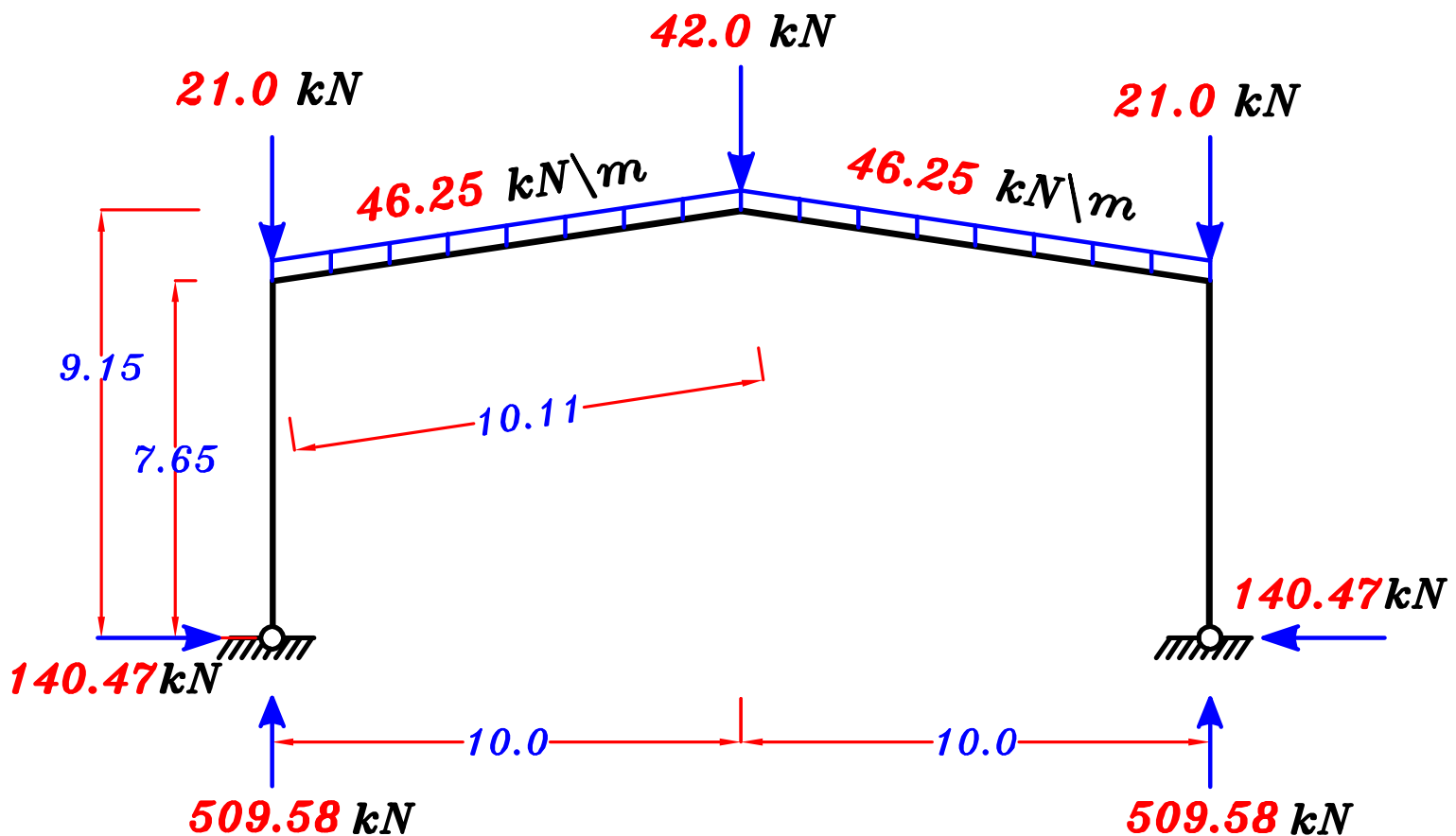
$$\delta_{10} = \frac{1}{E_c I_c} * (M_o * M_1) + \frac{1}{E_c I_b} * (M_o * M_1)$$

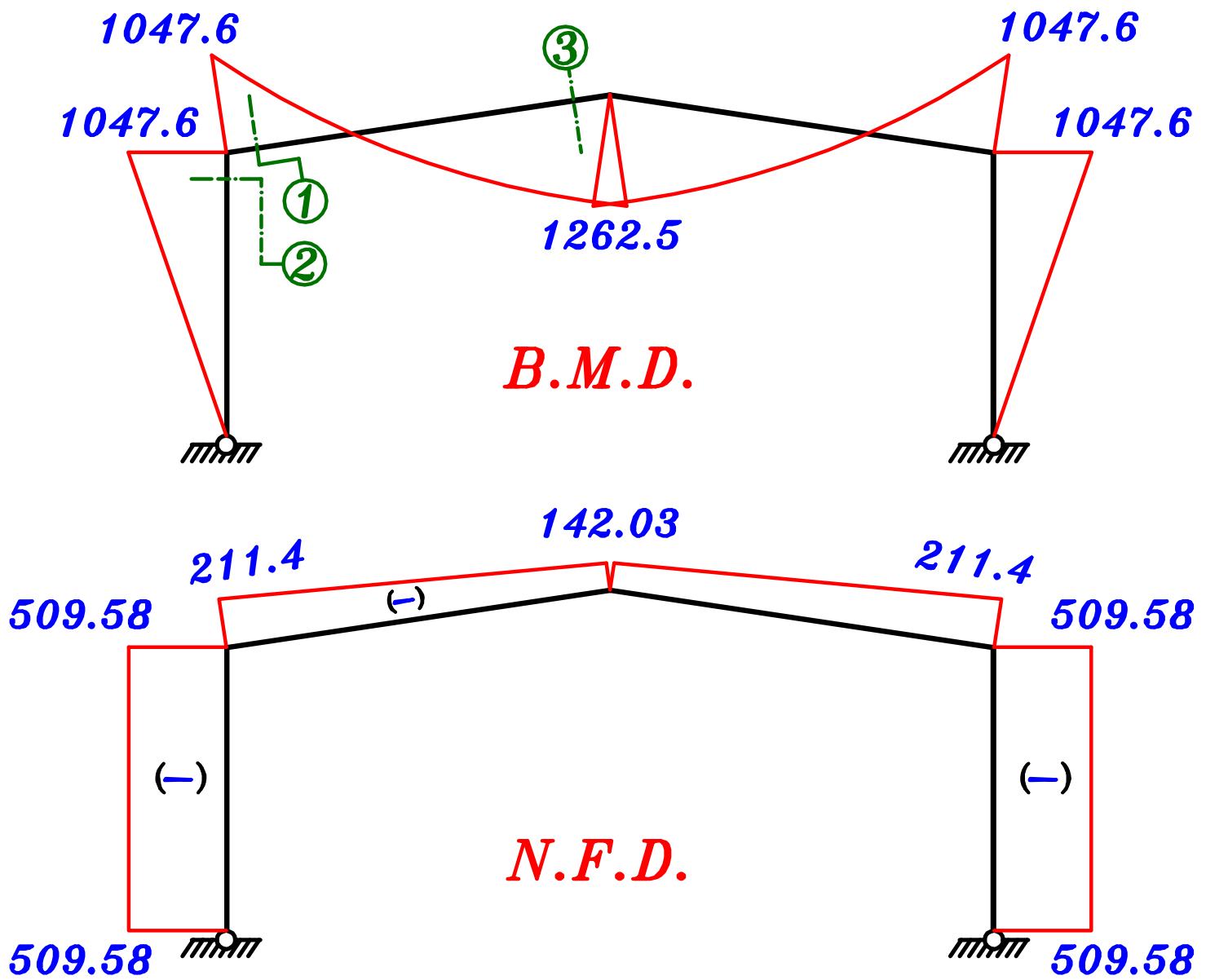
$$\delta_{10} = \text{zero} + \frac{2}{E_c (2.10) I_c} \left(-\frac{1}{2} (10.11) (2547.8) [8.65] - \frac{2}{3} (584.5) (10.11) [8.40] \right) = \frac{-137615.73}{E_c I_c}$$

$$\delta_{11} = \frac{1}{E_c I_c} * (M_1 * M_1) + \frac{1}{E_c I_b} * (M_1 * M_1) = \frac{2}{E_c I_c} \left(\frac{1}{2} (7.75) (7.75) [5.16] \right) + \frac{2}{E_c (2.10) I_c} \left((7.65) (10.11) [8.40] + \frac{1}{2} (10.11) (1.50) [8.65] \right) = \frac{979.66}{E_c I_c}$$

$$\therefore \delta_{10} + X \delta_{11} = \text{Zero}$$

$$\therefore \frac{-137615.73}{E_c I_c} + X * \frac{979.66}{E_c I_c} = \text{Zero} \rightarrow \boxed{X = 140.47 \text{ kN}}$$





Design of Sections.

Sec. ① R-Sec.

$$M = 1047.6 \text{ kN.m} , P = 211.4 \text{ kN} , b = 300 \text{ mm} , t = 1700 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{211.4 * 10^3}{25 * 300 * 1700} = 0.0166 < 0.04 \text{ (neglect } P \text{)}$$

$$\therefore 1600 = C_1 \sqrt{\frac{1047.6 * 10^6}{25 * 300}} \rightarrow C_1 = 4.23 \rightarrow J = 0.812$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1047.6 * 10^6}{0.812 * 360 * 1600} = 2297.57 \text{ mm}^2$$

Check $A_{s \min.}$ $A_{s_{req.}} = 2297.57 \text{ mm}^2$

$$\mu_{\min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 300 * 1600 = 1500 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{\min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2297.57 \text{ mm}^2$ **7 ϕ 22**

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{300 - 25}{22 + 25} = 5.85 = 5.0 \text{ bars}$$

Sec. ② R-Sec.

Neglect Effect of buckling

$M = 1047.6 \text{ kN.m}$, $P = 509.58 \text{ kN}$, $b = 300 \text{ mm}$, $t = 1700 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{509.58 * 10^3}{25 * 300 * 1700} = 0.039 < 0.04$ (Neglect P)

$$\therefore 1600 = C_1 \sqrt{\frac{1047.6 * 10^6}{25 * 300}} \rightarrow C_1 = 4.23 \rightarrow J = 0.812$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1047.6 * 10^6}{0.815 * 360 * 1600} = 2297.57 \text{ mm}^2$$

Check $A_{s \min.}$ $A_{s_{req.}} = 2297.57 \text{ mm}^2$

$$\mu_{\min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{25}}{360} \right) 300 * 1600 = 1500 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{\min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2297.57 \text{ mm}^2$ **7 ϕ 22**

Sec. ③ *R-Sec.* (Because the slab is H.B.)

$$M = 1262.5 \text{ kN.m}, P = 142.03 \text{ kN}, b = 300 \text{ mm}, t = 1700 \text{ mm}$$

Check $\frac{P}{F_{cu} b t} = \frac{142.03 \cdot 10^3}{25 \cdot 300 \cdot 1700} = 0.011 < 0.04$ (neglect P)

$$\therefore 1600 = C_1 \sqrt{\frac{1262.5 \cdot 10^6}{25 \cdot 300}} \rightarrow C_1 = 3.90 \rightarrow J = 0.80$$

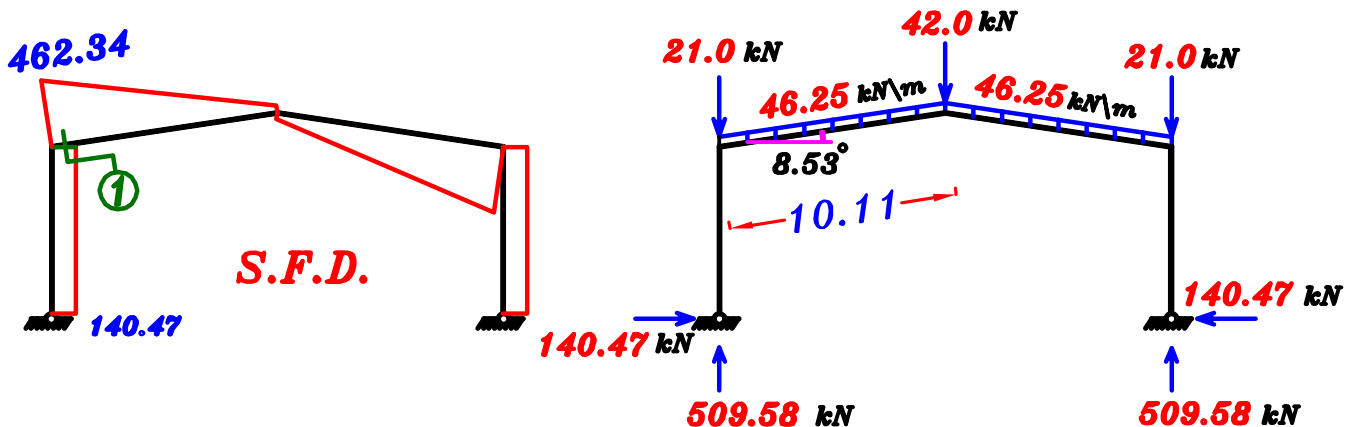
$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{1338.9 \cdot 10^6}{0.80 \cdot 360 \cdot 1600} = 2739.8 \text{ mm}^2$$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 2739.8 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 300 \cdot 1600 = 1500 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 2739.8 \text{ mm}^2 \quad \textcircled{8 \phi 22}$$

Check Shear.

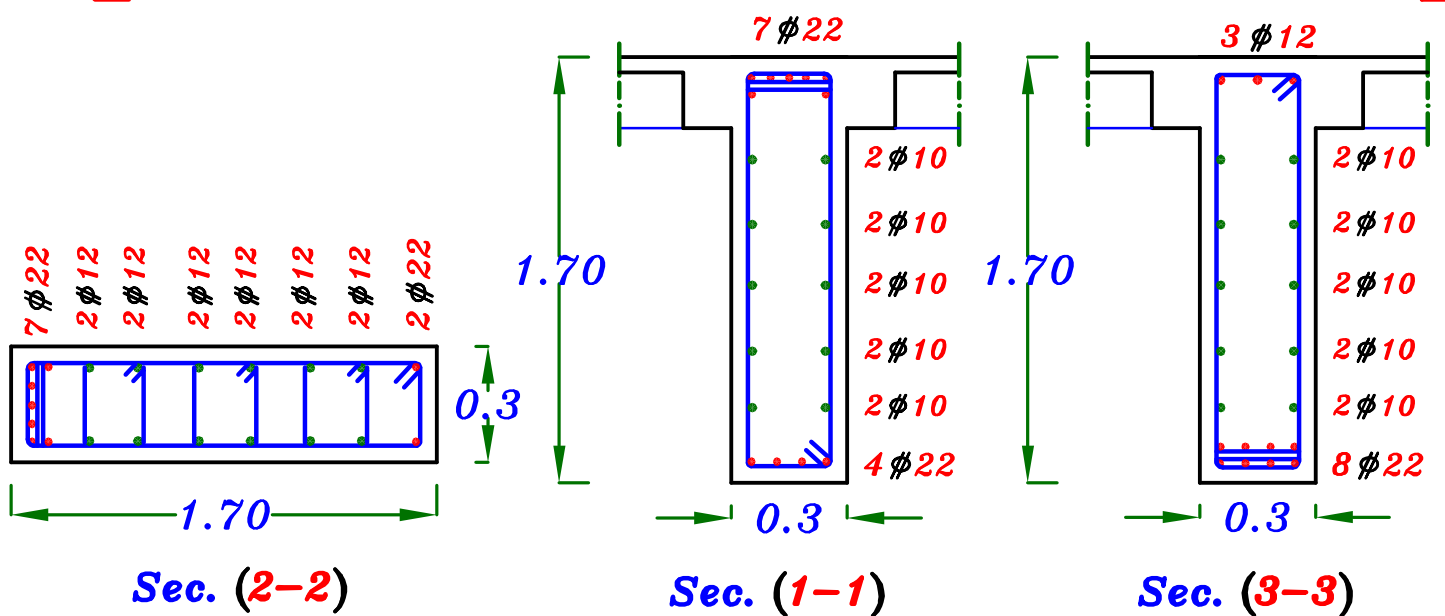
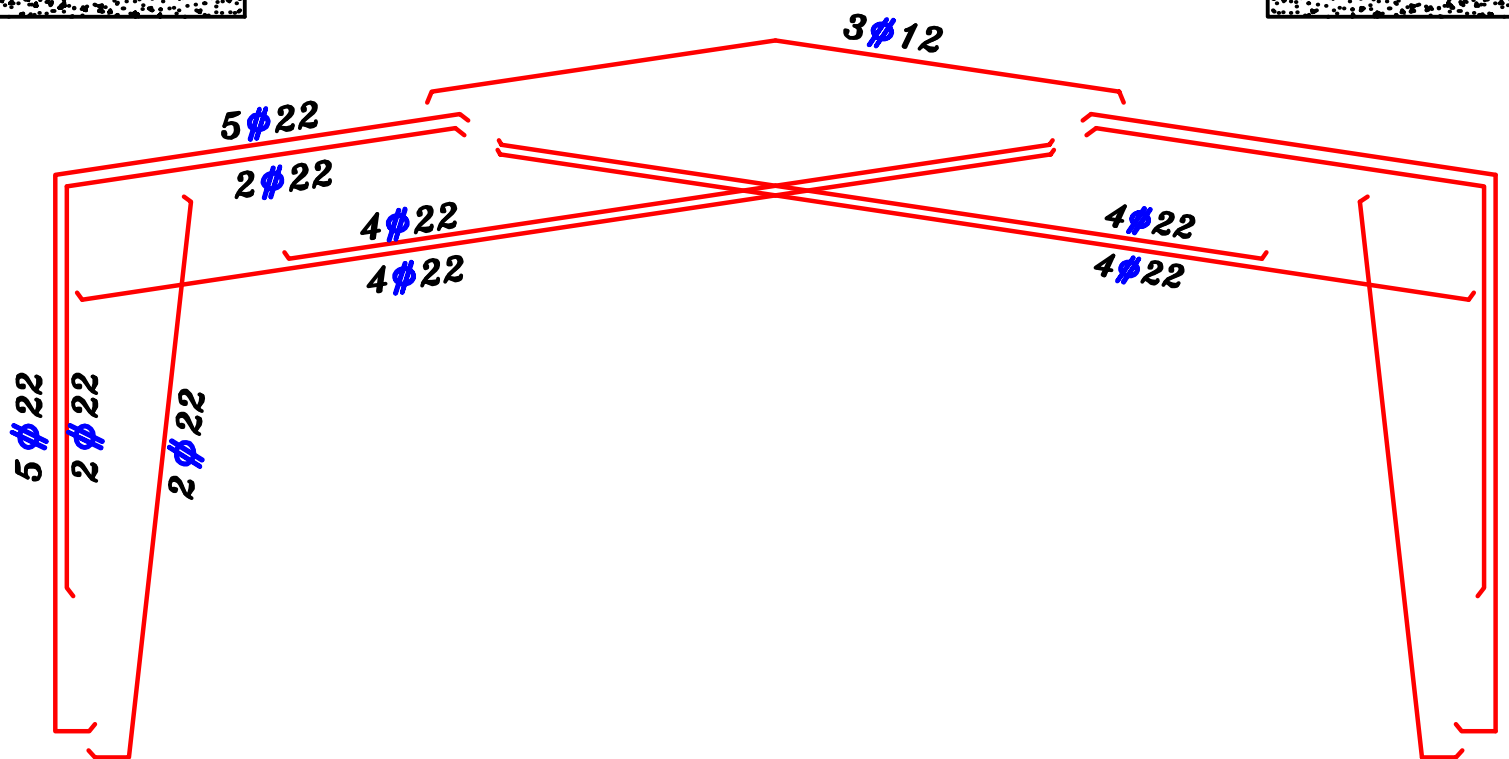
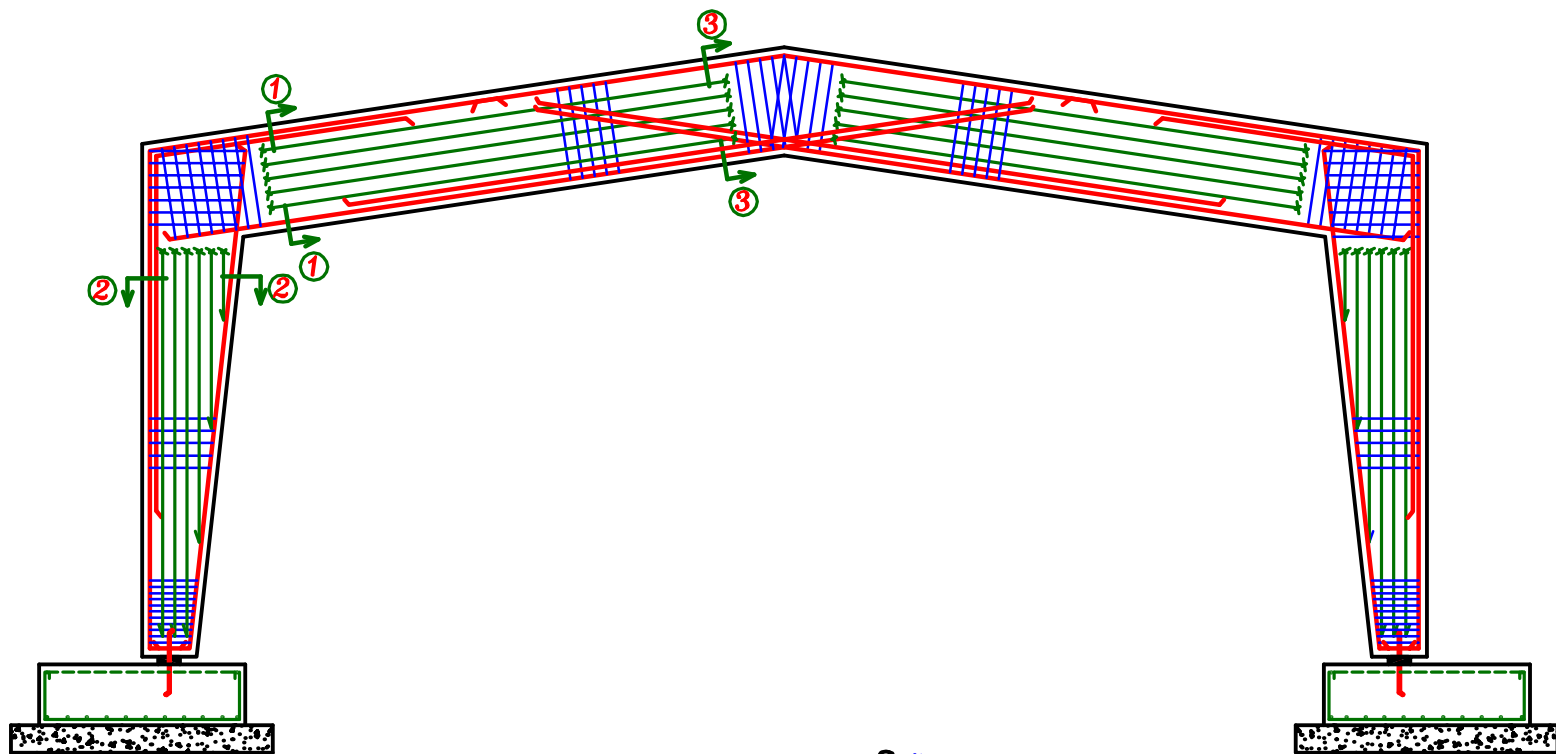


$$q_{cu} = (0.24) \sqrt{\frac{25}{1.50}} = 0.98 \text{ N/mm}^2$$

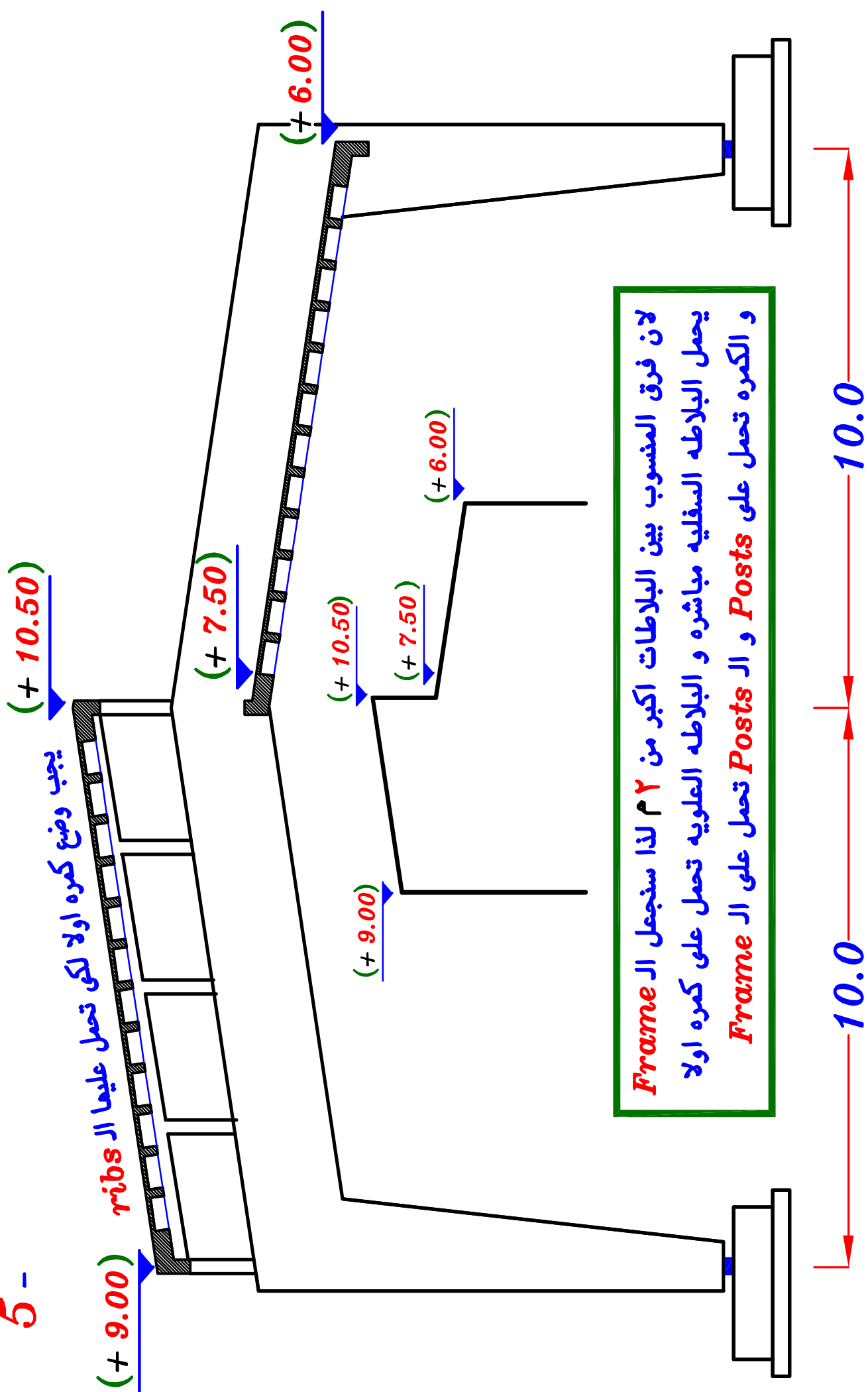
$$q_{u_{max}} = (0.70) \sqrt{\frac{25}{1.50}} = 2.85 \text{ N/mm}^2$$

Sec. ① $q_u = \frac{Q_{max}}{b d} = \frac{462.34 \cdot 10^3}{300 \cdot 1600} = 0.963 \text{ N/mm}^2 < q_{cu}$

\therefore Use Stirrups $5 \phi 8 \setminus m$ 2 branches



5 -



Example.

Figure (1) shows a sectional elevation For an Industrial building of overall plan dimensions $28.0\text{ m} \times 42.0\text{ m}$, with 24.0 m clear span without any intermediate columns. The covering system consists of set of horizontal and inclined slabs where shown in the Figure. The level of horizontal slabs is 7.0 m From ground level. Only two sets of windows are allowed where shown in the Figure.

It is required to:

- 1 – Choose a convenient main system For the main supporting element and draw a sectional elevation and structural plan (to scale $1:50$), showing all the structural elements with reasonably assumed concrete dimensions.
- 2 – Design the slab (a b c), then draw its details of reinforcement on the structural plan.
- 3 – Design the main supporting structural system, then draw its details of reinforcement in elevation (to scale $1:50$) and sections (to scale $1:20$).

Data:

$F_{cu} = 30\text{ MPa}$, st. 40/60 , Spacing between systems = 7.0 m

$F.C. = 1.0\text{ kN/m}^2$, $L.L. = 1.0\text{ kN/m}^2$

Foundations level = $(-1.50)\text{ m}$ From ground level.

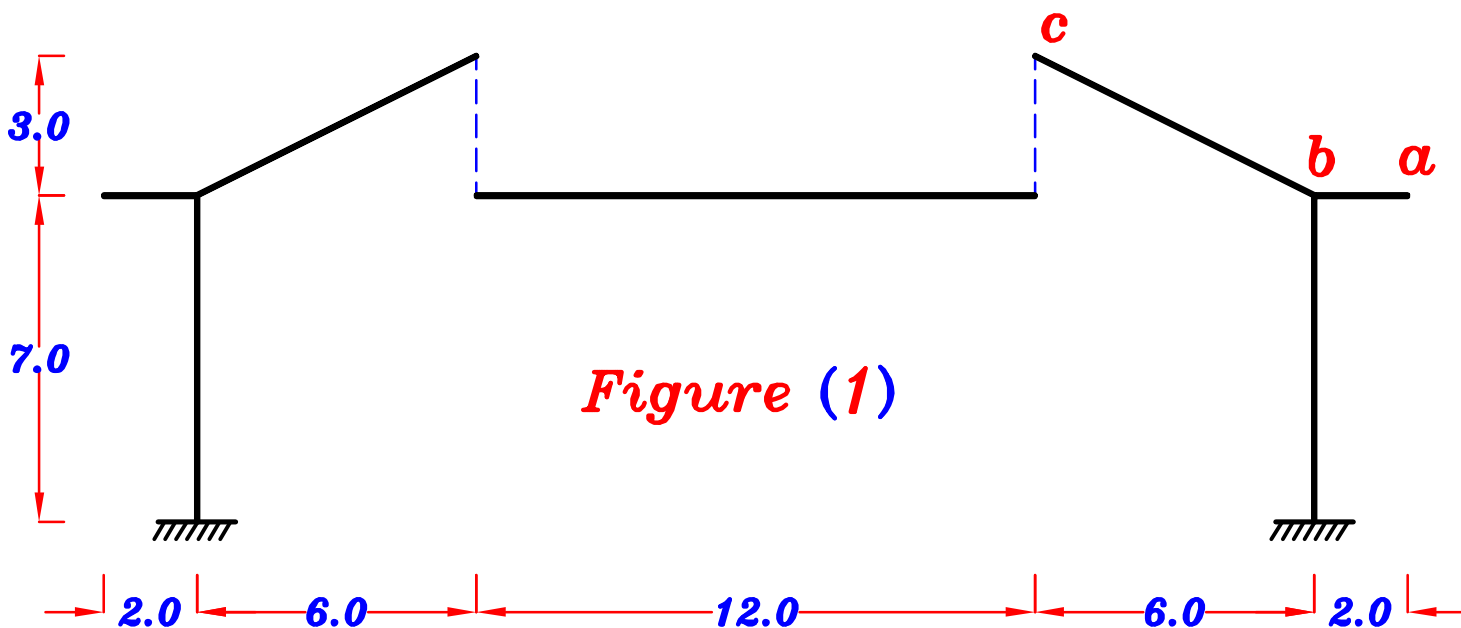
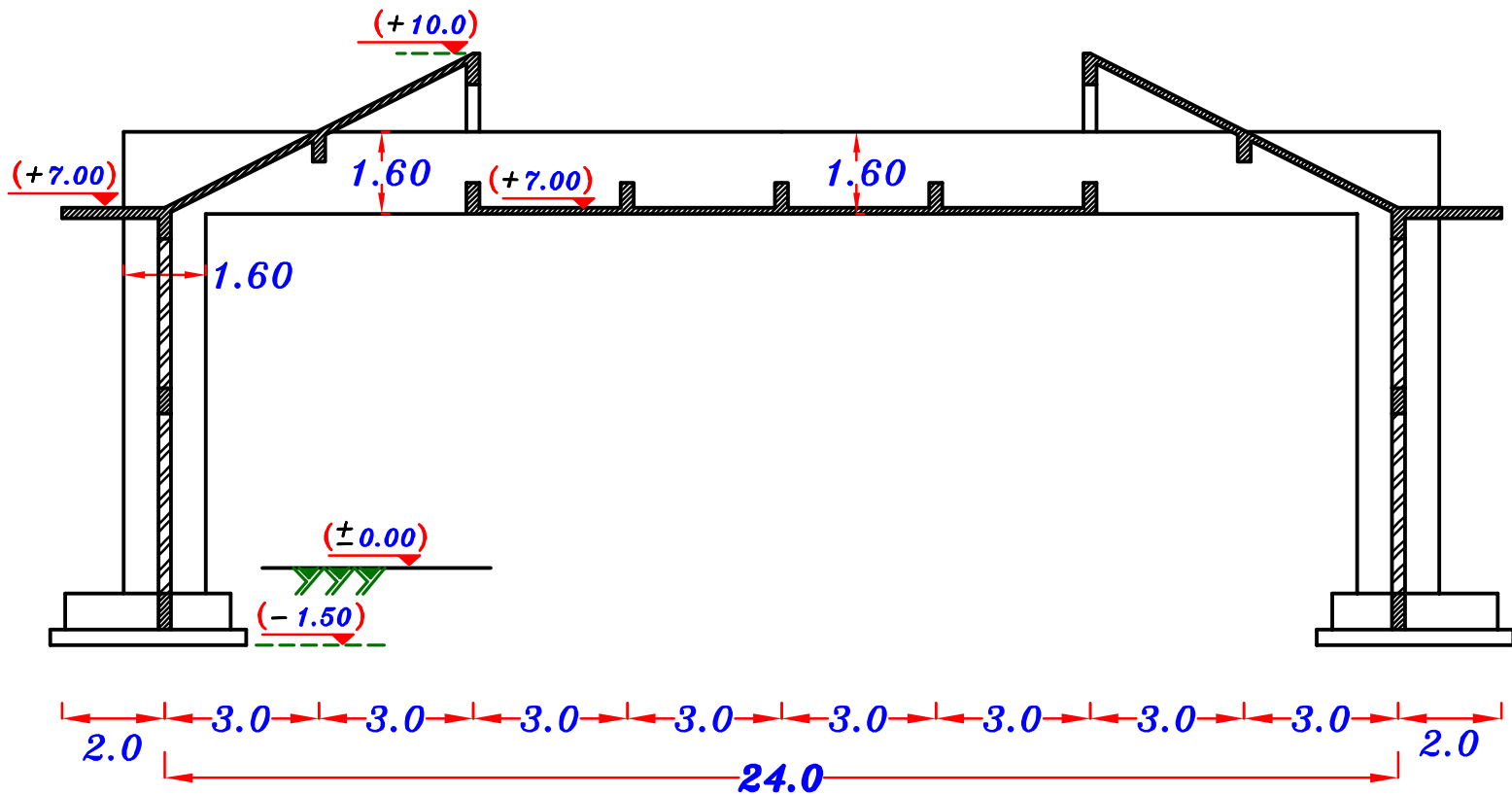


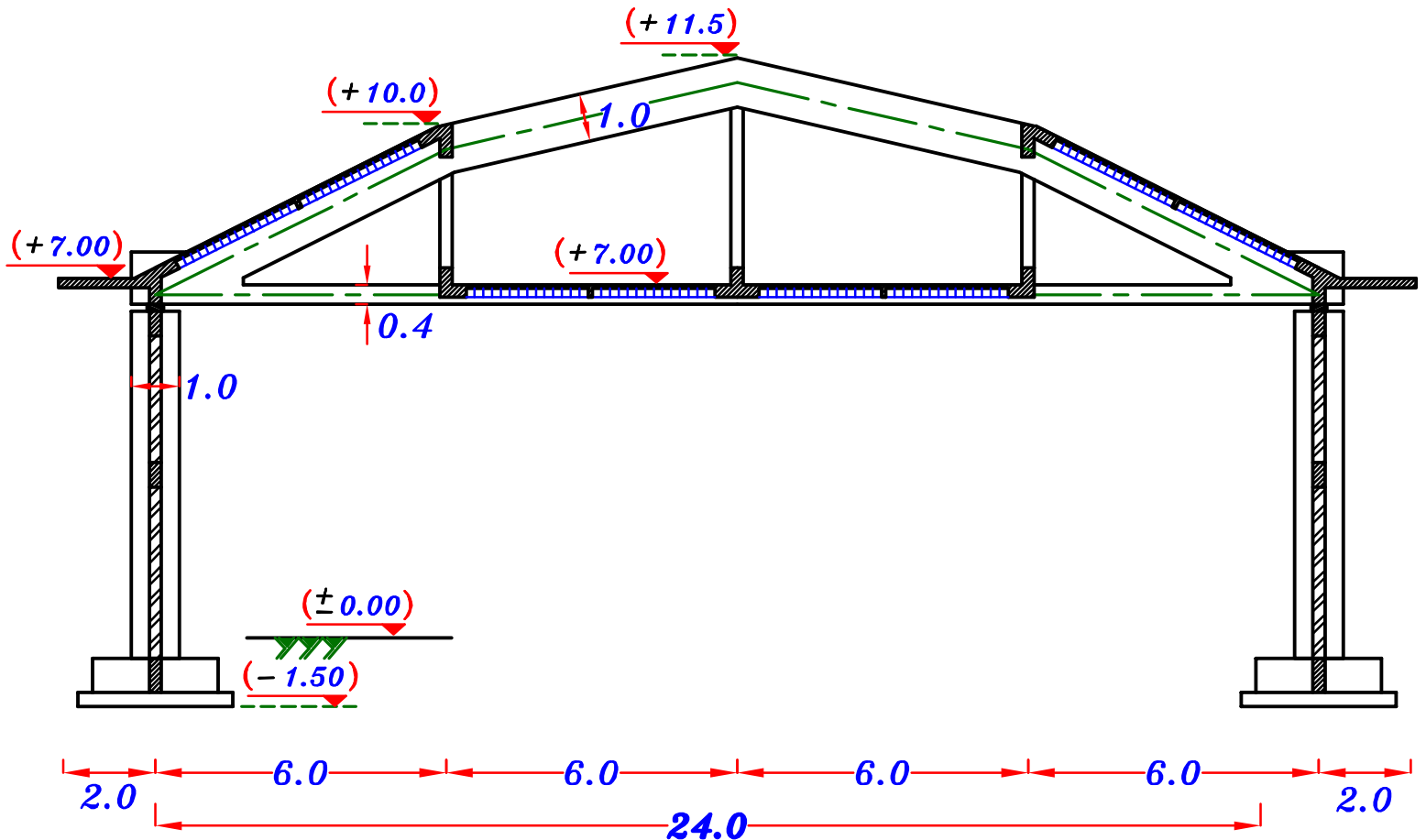
Figure (1)

1 – There are 2 Systems can be used to cover this area.

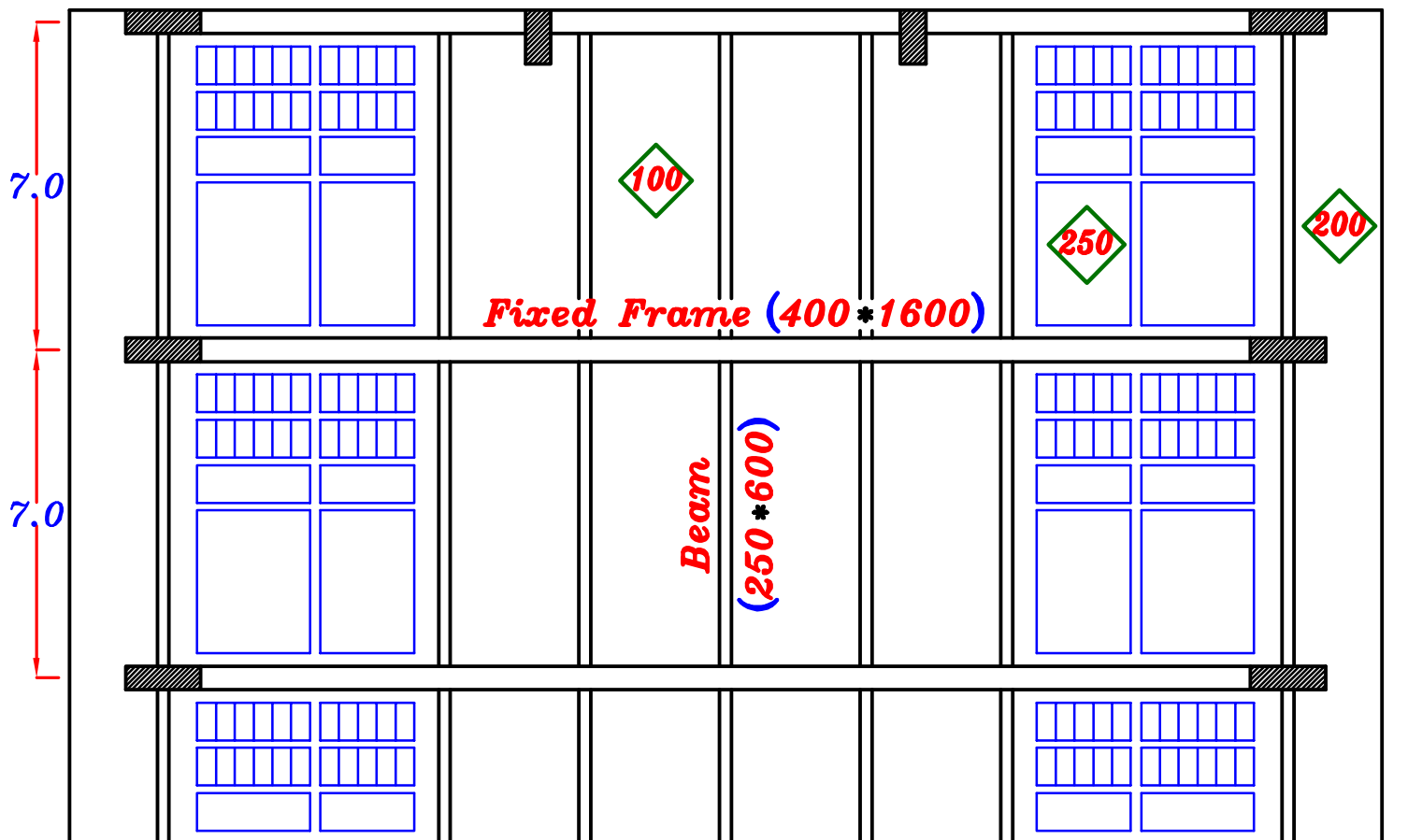
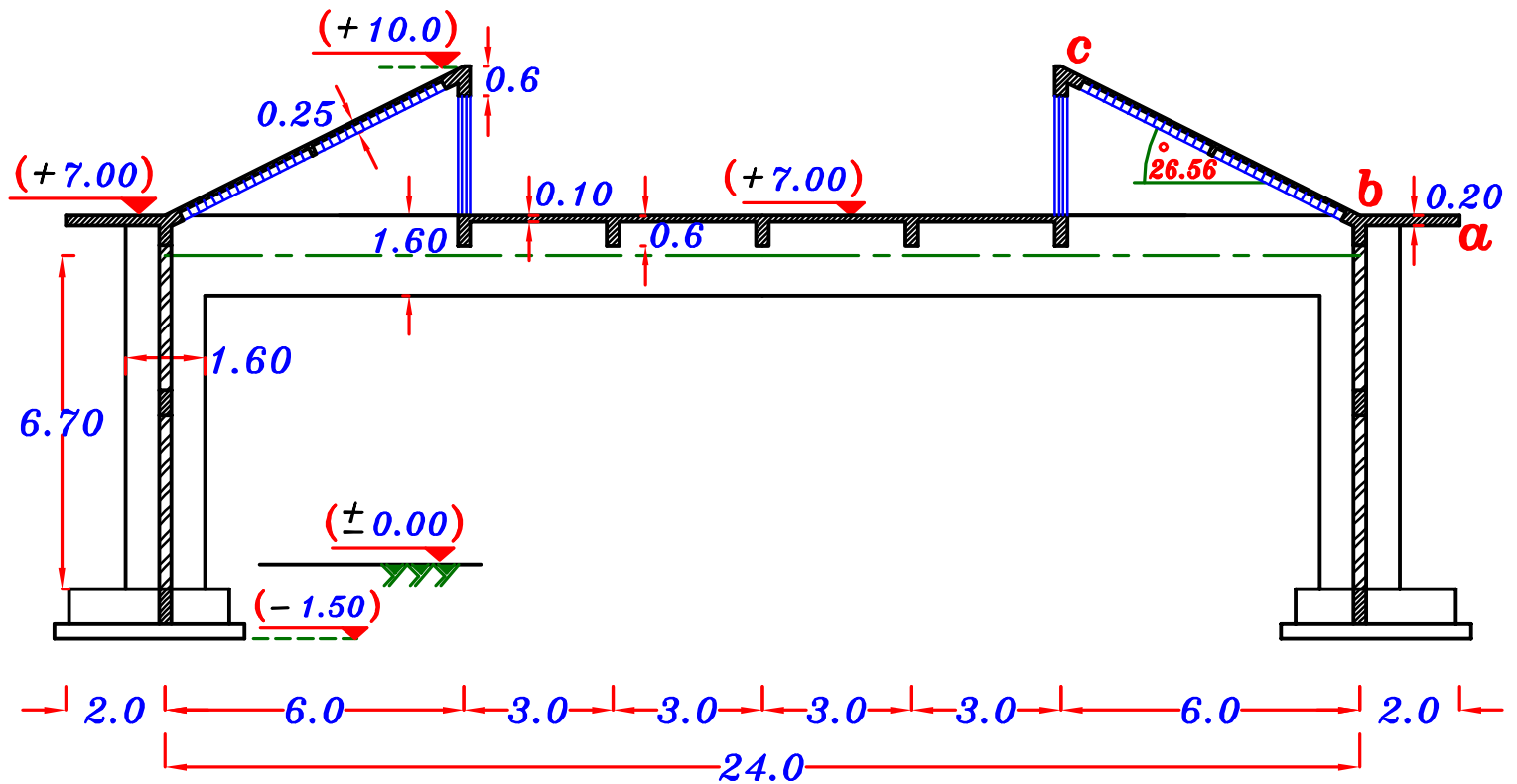
We can use **Fixed Frame**.



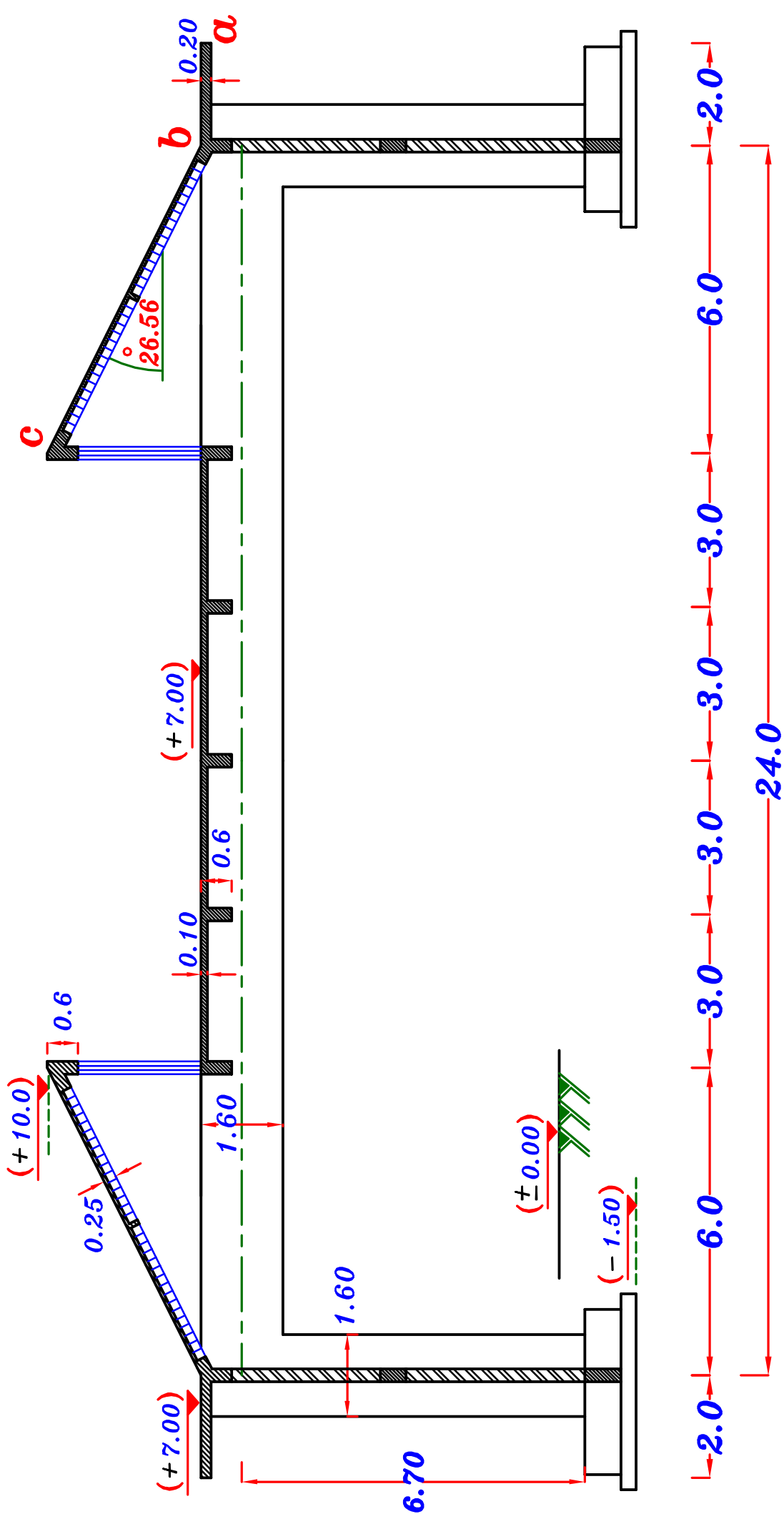
Or we can use **Arch Girder**.



Use Fixed Frame.



Fixed Frame.



2- Design the slab (**a b c**), then draw its details of reinforcement on the structural plan.

For cantilever Solid Slab. **a b**

$$t_s = \frac{2000}{10} = 200 \text{ mm}$$

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 (L.L.) \quad \text{kN/m}^2$$

$$w_s = 1.4 (0.20 * 25 + 1.0) + 1.6 (1.0) = 10.0 \quad \text{kN/m}^2$$

For Inclined H.B. Slab. **b c** Blocks (200*400*200)

$$a = 200 \text{ mm} , e = 400 \text{ mm} , h = 200 \text{ mm} , t_s = 50 \text{ mm}$$

$$t = h + t_s = 200 + 50 = 250 \text{ mm}$$

$$b = 100 \text{ mm} , S = e + b = 400 + 100 = 500 \text{ mm}$$

$$h = 200 \text{ mm} \longrightarrow \text{Weight of Block} = 150 \text{ N}$$

$$w_{ribi} = \left[1.4 (t_s \delta_c + F.C.) + 1.6 (L.L.) \cos \theta \right] (S * 1.0) \\ + 1.4 (b h * 1.0 \text{ m} * \delta_c) + 1.4 * (\text{Block weight}) \left(\frac{1.0}{a} \right)$$

$$\therefore w_{ribi} = \left[1.4 (0.05 * 25 + 1.0) + 1.6 (1.0) (\cos 26.56) \right] (0.50 * 1.0) \\ + 1.4 (0.10 * 0.20 * 1.0 * 25) + 1.4 \left(\frac{150}{1000} \right) \left(\frac{1.0}{0.2} \right) = 4.04 \quad \text{kN / (1.0 * 0.5) m}^2$$

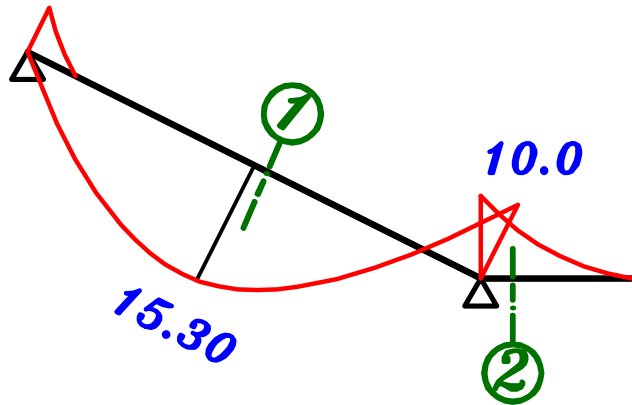
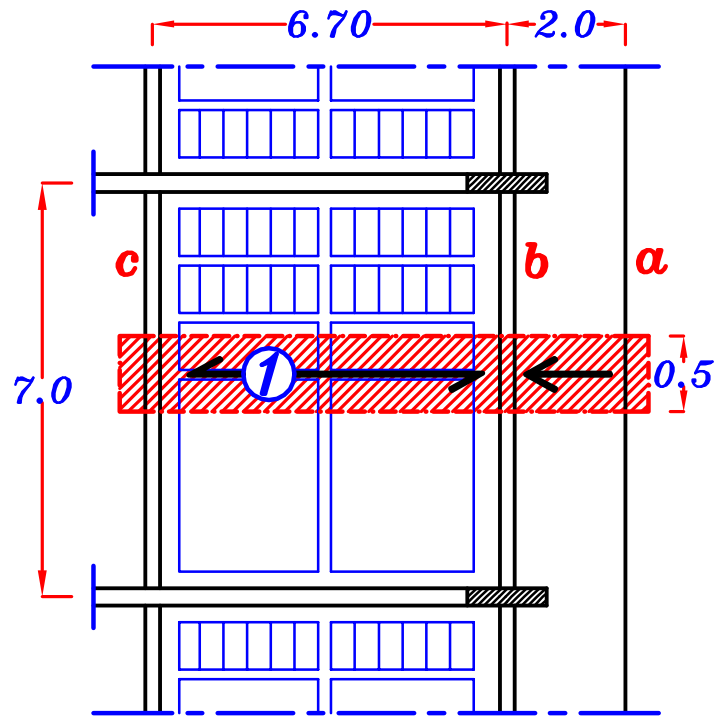
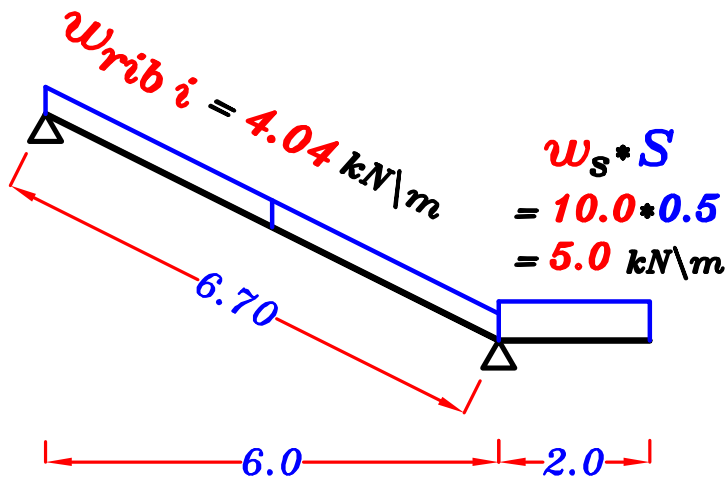
For the Horizontal Solid Slabs at the middle of the Frame.

$$\text{One way Solid slab } t_s = \frac{L_s}{30} = \frac{3000}{30} = 100 \text{ mm}$$

$$w_s = 1.4 (t_s \delta_c + F.C.) + 1.6 (L.L.) \quad \text{kN/m}^2$$

$$w_s = 1.4 (0.10 * 25 + 1.0) + 1.6 (1.0) = 6.50 \quad \text{kN/m}^2$$

Strip a b c



Sec. ① **H.B.** $M_{U.L.} = 15.30 \text{ kN.m/rib}$

$t = 250 \text{ mm}$, $d = 250 - 30 = 220 \text{ mm}$, $S = 500 \text{ mm}$ عرض الشريحة

$$220 = C_1 \sqrt{\frac{15.30 \cdot 10^6}{30 \cdot 500}} \longrightarrow C_1 = 6.88 \longrightarrow J = 0.826$$

$$A_s = \frac{15.30 \cdot 10^6}{0.826 \cdot 400 \cdot 220} = 210.5 \text{ mm}^2/\text{rib} \quad \textcircled{2\Phi 12 \text{ \textbackslash rib}}$$

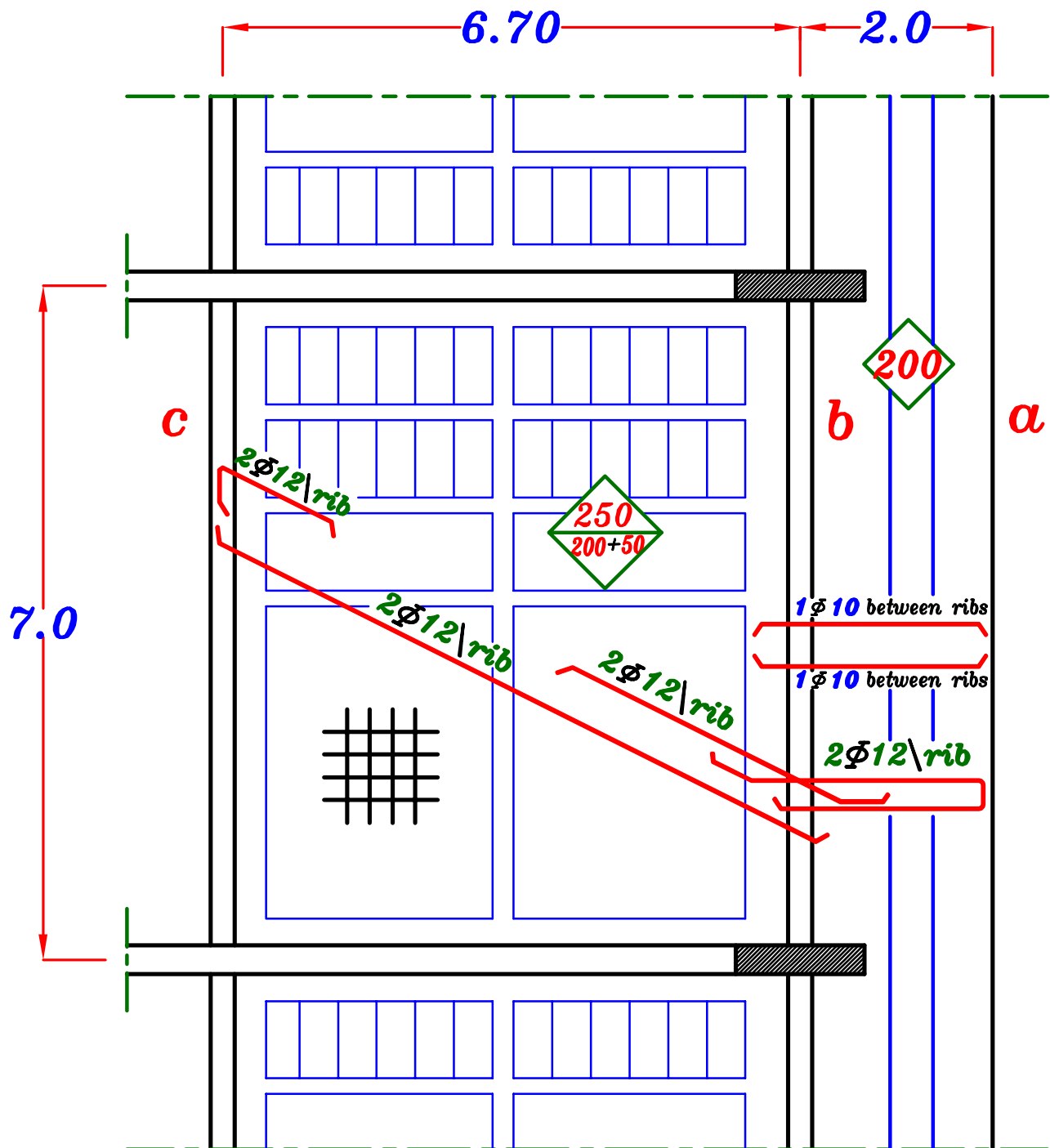
Sec. ② **S.S.** $M_{U.L.} = 10.0 \text{ kN.m/0.50 m}$

$t_s = 200 \text{ mm}$, $d = 200 - 20 = 180 \text{ mm}$, $S = 500 \text{ mm}$ عرض الشريحة

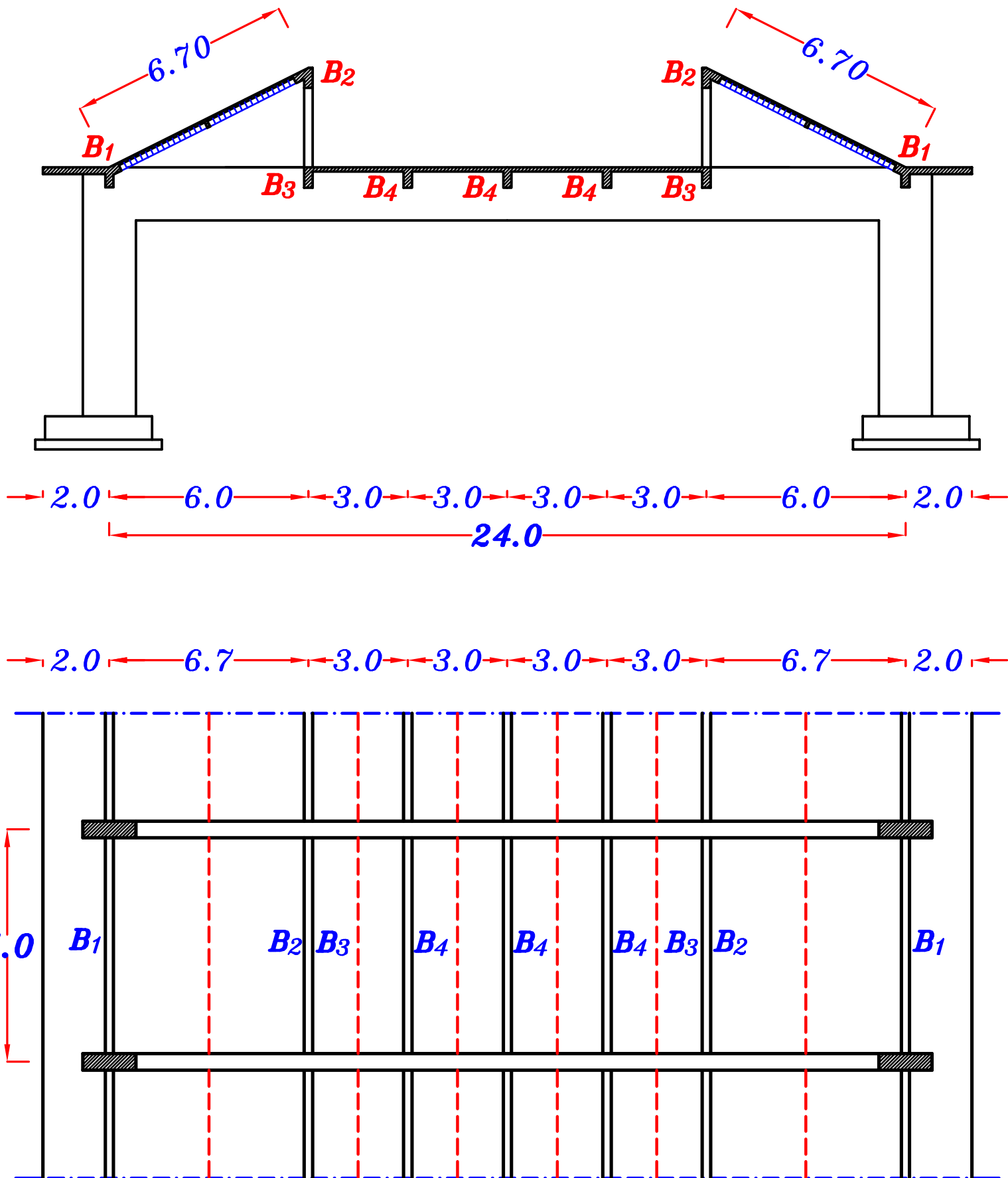
$$180 = C_1 \sqrt{\frac{10.0 \cdot 10^6}{30 \cdot 500}} \longrightarrow C_1 = 6.97 \longrightarrow J = 0.826$$

$$A_s = \frac{10.0 \cdot 10^6}{0.826 \cdot 400 \cdot 180} = 168.14 \text{ mm}^2/\text{rib} \quad \textcircled{2\Phi 12 \text{ \textbackslash rib}}$$

التسليح rib \ لأنه يوجد تداخل بين ال **S.S. & H.B.**



3 – Design the main supporting structural system, then draw its details of reinforcement in elevation (to scale **1:50**) and sections (to scale **1:20**).



Take all secondary Beams (250 * 600)

$$O.W.(Beams) = 1.4 * 0.25 * 0.60 * 25 = 5.25 \text{ kN/m}$$

Frame (400 * 1600)

$$O.W.(Frame) = 1.4 * 0.40 * 1.60 * 25 = 22.4 \text{ kN/m}$$

$$w_s = 10.0 \text{ kN/m}^2 \text{ For Cantilever solid Slab}$$

$$w_s = 6.50 \text{ kN/m}^2 \text{ For One way solid Slab}$$

$$w_{rib} = 4.04 \text{ kN/(1.0 * 0.5)} \text{ For One way H.B.}$$

Load Distribution.

$$\underline{B_1} \quad w = o.w. + w_s * L_c + \frac{w_{rib}}{S} * \frac{L_s}{2}$$

$$w = 5.25 + 10.0 * 2.0 + \frac{4.04}{0.5} * \frac{6.70}{2} = 52.32 \text{ kN/m}$$

$$R_1 = w * S = 52.32 * 7.0 = 366.24 \text{ kN}$$

$$\underline{B_2} \quad w = o.w. + \frac{w_{rib}}{S} * \frac{L_s}{2} = 5.25 + \frac{4.04}{0.5} * \frac{6.70}{2} = 32.32 \text{ kN/m}$$

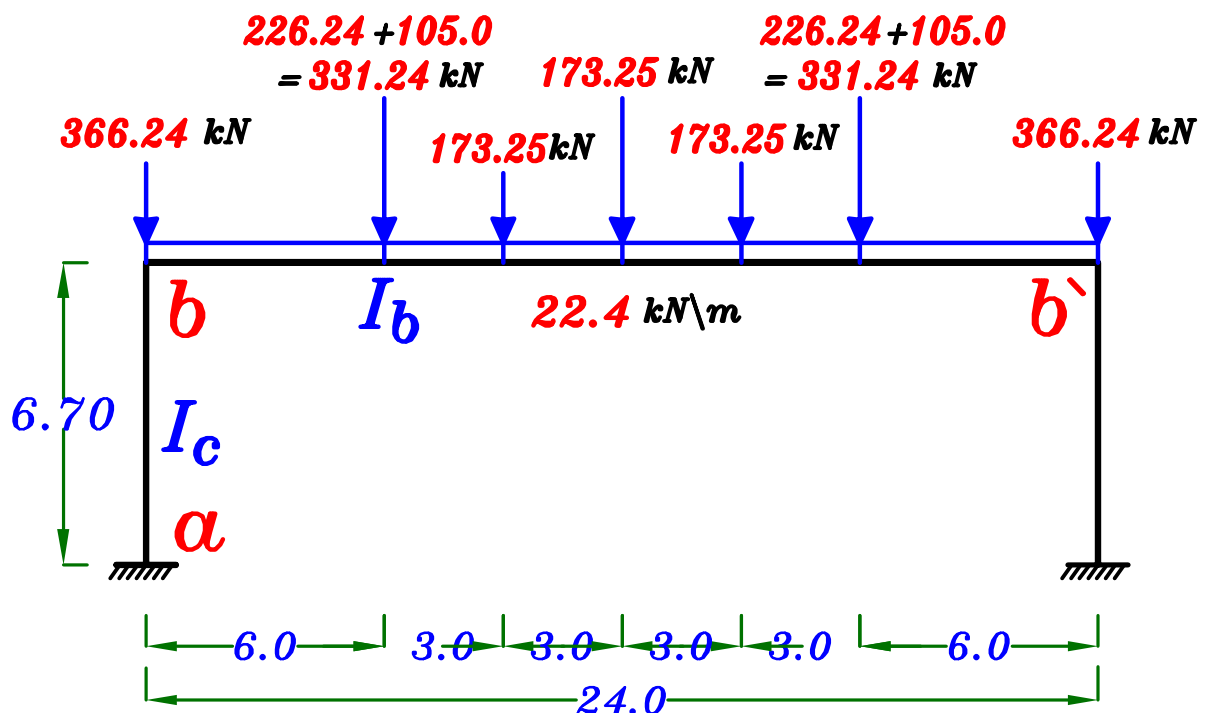
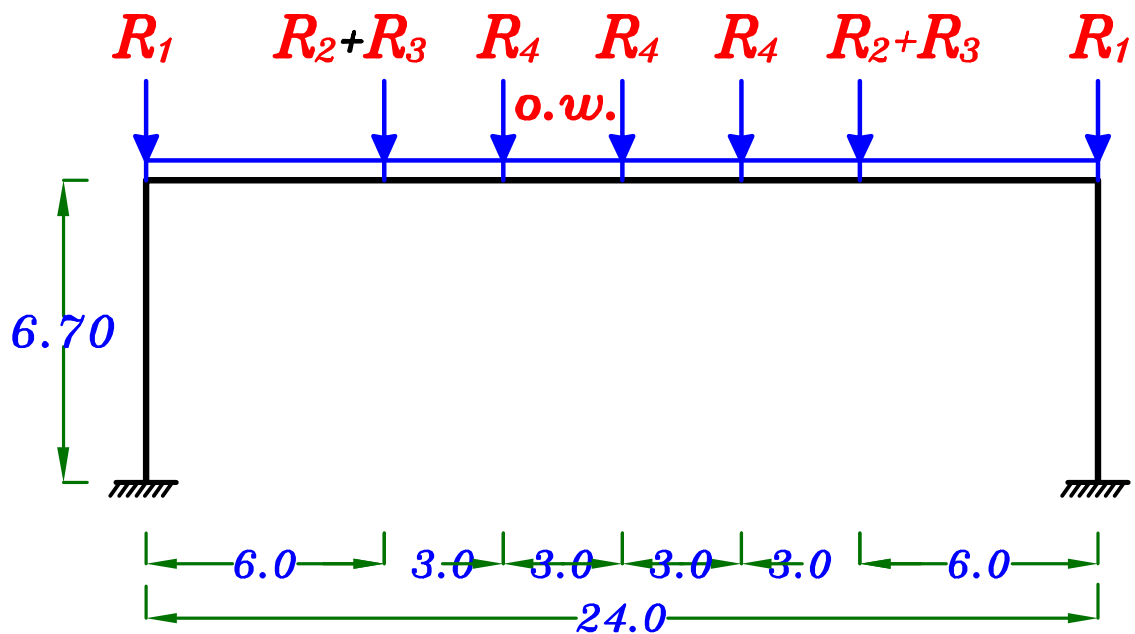
$$R_2 = w * S = 32.32 * 7.0 = 226.24 \text{ kN}$$

$$\underline{B_3} \quad w = o.w. + w_s * \frac{L_s}{2} = 5.25 + 6.50 * \frac{3.0}{2} = 15.0 \text{ kN/m}$$

$$R_3 = w * S = 15.0 * 7.0 = 105.0 \text{ kN}$$

$$\underline{B_4} \quad w = o.w. + 2 * w_s * \frac{L_s}{2} = 5.25 + 2 * 6.50 * \frac{3.0}{2} = 24.75 \text{ kN/m}$$

$$R_4 = w * S = 24.75 * 7.0 = 173.25 \text{ kN}$$



$$I_c = I_b = \frac{b(t)^3}{12} = \frac{0.4(1.60)^3}{12} = 0.136 \text{ m}^4$$

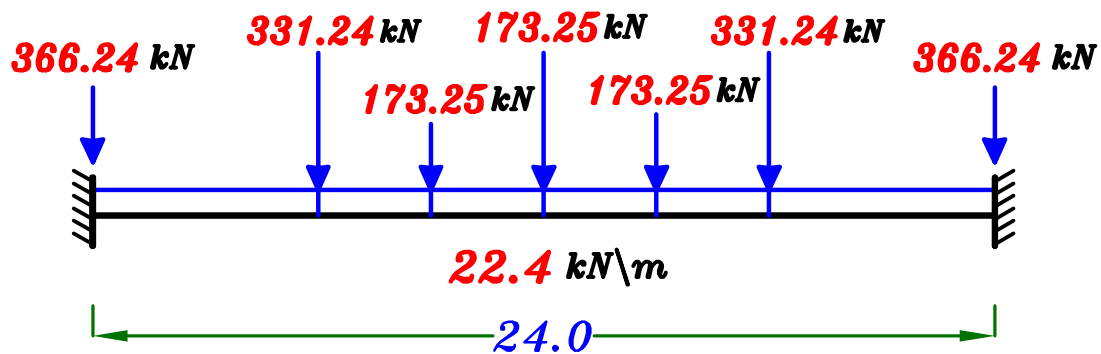
For Joint b

$$K_c = \frac{I_c}{h} = \frac{I_c}{6.70} = 0.149 I_c$$

$$K_b = \frac{1}{2} \frac{I_b}{L} = \frac{1}{2} * \frac{I_b}{24.0} = 0.0208 I_b = 0.0208 I_c$$

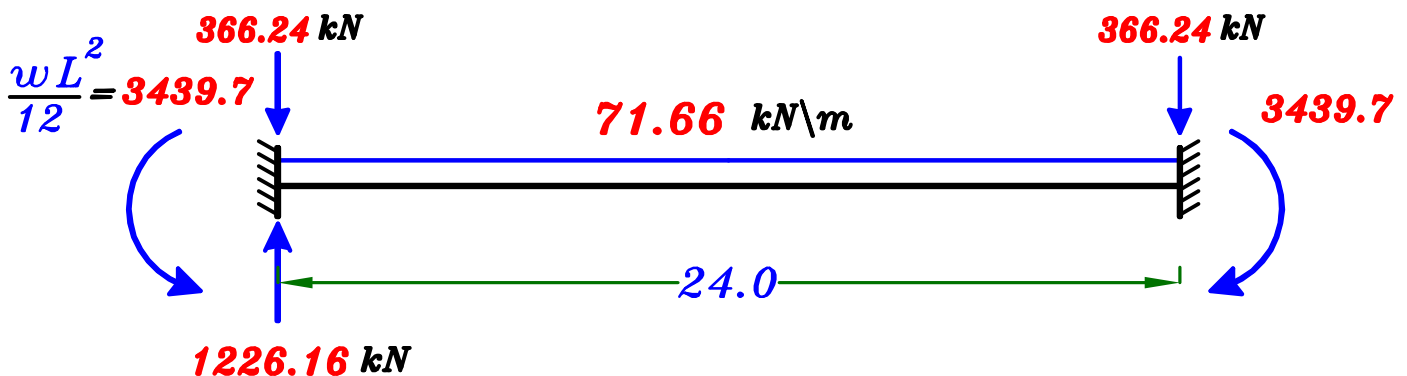
$$D.F. (c) = \frac{0.149}{0.149 + 0.0208} = 0.877$$

$$D.F. (b) = 1 - 0.877 = 0.123$$

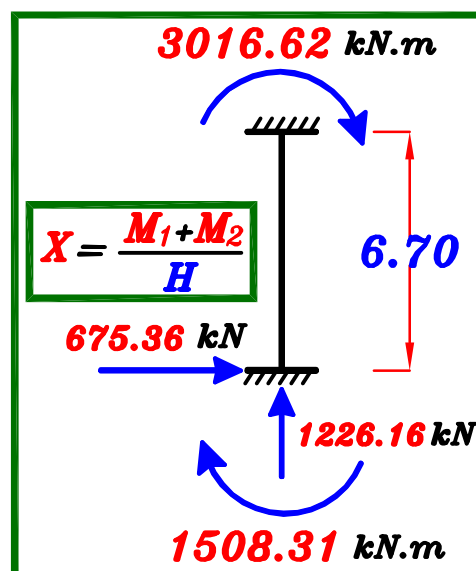


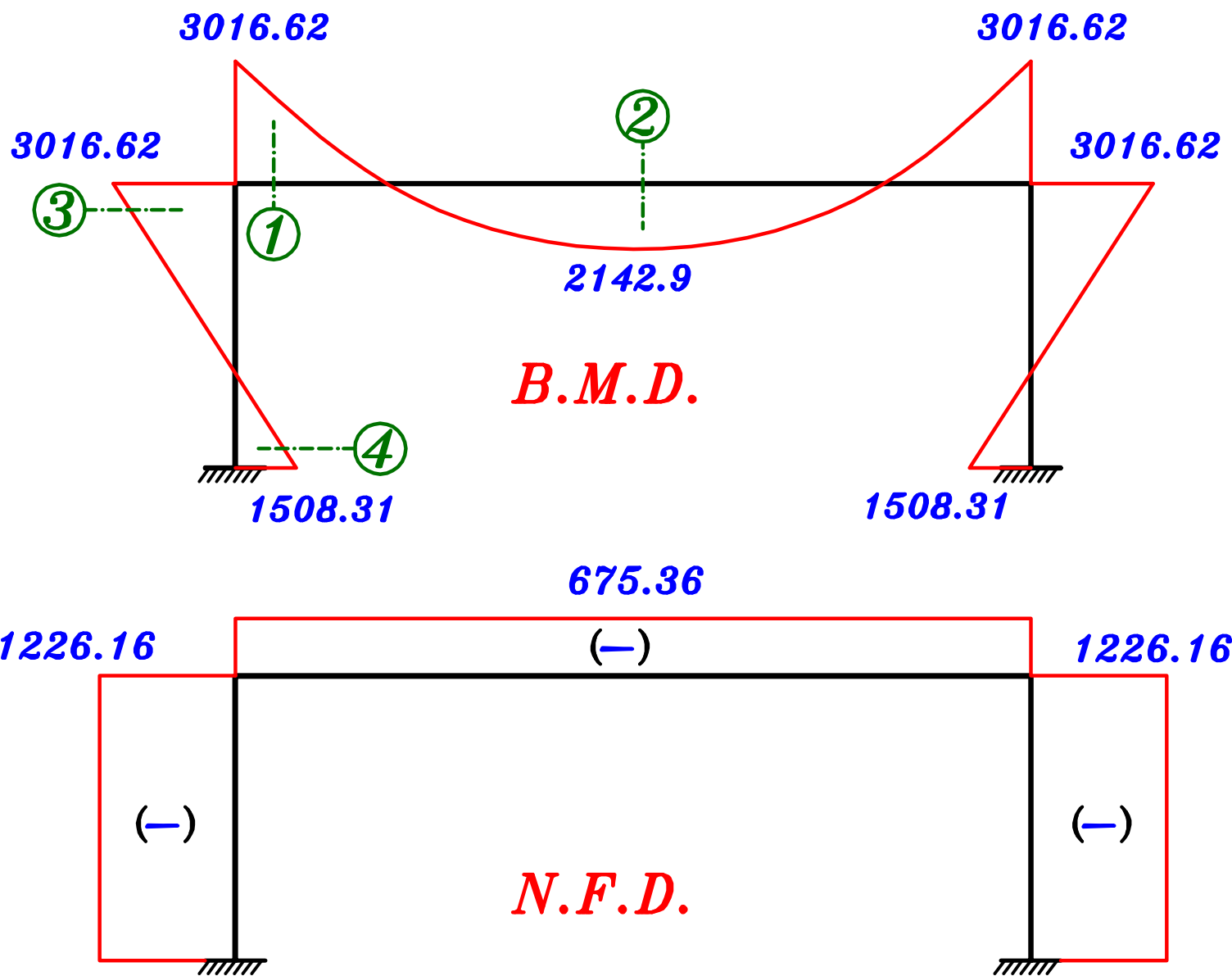
$$w = o.w. + \frac{\sum P}{span} = 22.4 + \frac{2(331.24) + 3(173.25)}{24.0} = 71.66 \text{ kN/m}$$

$$\frac{wL^2}{12} = \frac{71.66 * (24.0)^2}{12} = 3439.7 \text{ kN.m}$$



$$F.E.M. (Beam) * D.F. (Col.) = 3439.7 * 0.877 = 3016.62 \text{ kN.m}$$





Design of Sections.

Sec. ① R-Sec.

$$M = 3016.62 \text{ kN.m} , P = 675.36 \text{ kN} , b = 400 \text{ mm} , t = 1600 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{675.36 * 10^3}{30 * 400 * 1600} = 0.035 < 0.04 \text{ (neglect } P \text{)}$$

$$\therefore 1500 = C_1 \sqrt{\frac{3016.62 * 10^6}{30 * 400}} \rightarrow C_1 = 2.99 \rightarrow J = 0.742$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{3016.62 * 10^6}{0.742 * 400 * 1500} = 6775.9 \text{ mm}^2$$

Check $A_{s_{min}}$ $A_{s_{req.}} = 6775.9 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 400 * 1500 = 1848.6 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 6775.9 \text{ mm}^2$ $14 \Phi 25$

$$\therefore n = \frac{b - 25}{\phi + 25} = \frac{400 - 25}{25 + 25} = 7.50 = 7.5 \text{ bars}$$

Sec. ② R-Sec.

$M = 2142.9 \text{ kN.m}$, $P = 675.36 \text{ kN}$, $b = 400 \text{ mm}$, $t = 1600 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{675.36 * 10^3}{30 * 400 * 1600} = 0.035 < 0.04$ (neglect P)

$$\therefore 1500 = C_1 \sqrt{\frac{2142.9 * 10^6}{30 * 400}} \rightarrow C_1 = 3.55 \rightarrow J = 0.784$$

$$\therefore A_s = \frac{M_{U.L.}}{J F_y d} = \frac{2142.9 * 10^6}{0.784 * 400 * 1500} = 4555.5 \text{ mm}^2$$

Check $A_{s_{min}}$ $A_{s_{req.}} = 4555.5 \text{ mm}^2$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 400 * 1500 = 1848.6 \text{ mm}^2$$

$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 4555.5 \text{ mm}^2$ $10 \Phi 25$

Sec. ③ R-Sec.

Neglect Effect of Buckling.

$M = 3016.62 \text{ kN.m}$, $P = 1226.16 \text{ kN}$, $b = 400 \text{ mm}$, $t = 1600 \text{ mm}$

Check $\frac{P}{F_{cu} b t} = \frac{1226.16 * 10^3}{30 * 400 * 1600} = 0.064 > 0.04$ (Don't neglect P)

$$e_s = e + \frac{t}{2} - c = 2.46 + \frac{1.6}{2} - 0.1 = 3.16 \text{ m}$$

$$M_s = P * e_s = 1226.16 * 3.16 = 3874.67 \text{ kN.m}$$

$$\therefore d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} \therefore 1500 = c_1 \sqrt{\frac{3874.67 * 10^6}{30 * 400}} \rightarrow c_1 = 2.64 < 2.78$$

\therefore The section is over reinforced

\therefore Increase depth or use A_s From I.D.

\therefore Increase depth

To choose minimum depth that make the section under reinforced

Take $C_1 = 2.78$

$$\therefore d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} = 2.78 \sqrt{\frac{3874.67 * 10^6}{30 * 400}} = 1579.7 \text{ mm}$$

$$\therefore \text{Choose } d = 1600 \text{ mm} , t = 1700 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{1226.16 * 10^3}{30 * 400 * 1700} = 0.060 > 0.04 \text{ (Don't neglect } P \text{)}$$

$$e = \frac{M}{P} = \frac{3016.62}{1226.16} = 2.46 \text{ m} \therefore \frac{e}{t} = \frac{2.46}{1.70} = 1.447 > 0.5 \xrightarrow{\text{use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 2.46 + \frac{1.7}{2} - 0.1 = 3.21 \text{ m}$$

$$M_s = P * e_s = 1226.16 * 3.21 = 3935.97 \text{ kN.m}$$

$$\therefore d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} \therefore 1600 = c_1 \sqrt{\frac{3935.97 * 10^6}{30 * 400}} \rightarrow c_1 = 2.79 \rightarrow J = 0.718$$

$$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \delta_s)} = \frac{3935.97 * 10^6}{0.718 * 400 * 1600} - \frac{1226.16 * 10^3}{(400 \setminus 1.15)} = 5040.2 \text{ mm}^2$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 5040.2 \text{ mm}^2$$

$$\mu_{min.} b d = \left(0.225 * \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 * \frac{\sqrt{30}}{400} \right) 400 * 1600 = 1971.8 \text{ mm}^2$$

$$\therefore A_{s_{req.}} > \mu_{min.} b d \therefore \text{Take } A_s = A_{s_{req.}} = 5040.2 \text{ mm}^2 \quad (11 \phi 25)$$

Sec. ④ R-Sec.

Neglect Effect of Buckling.

$$M = 1508.31 \text{ kN.m} , P = 1226.16 \text{ kN} , b = 400 \text{ mm} , t = 1700 \text{ mm}$$

$$\text{Check } \frac{P}{F_{cu} b t} = \frac{1226.16 \cdot 10^3}{30 \cdot 400 \cdot 1700} = 0.060 > 0.04 \quad (\text{Don't neglect } P)$$

$$e = \frac{M}{P} = \frac{1508.31}{1226.16} = 1.23 \text{ m} \quad \therefore \frac{e}{t} = \frac{1.23}{1.70} = 0.72 > 0.5 \xrightarrow{\text{use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 1.23 + \frac{1.7}{2} - 0.1 = 1.98 \text{ m}$$

$$M_s = P \cdot e_s = 1226.16 \cdot 1.98 = 2427.80 \text{ kN.m}$$

$$\therefore d = c_1 \sqrt{\frac{M_s}{F_{cu} b}} \quad \therefore 1600 = c_1 \sqrt{\frac{2427.80 \cdot 10^6}{30 \cdot 400}} \rightarrow c_1 = 3.55 \rightarrow J = 0.784$$

$$\begin{aligned} \therefore A_s &= \frac{M_s}{J F_y d} - \frac{P_{U.L.}}{(F_y \setminus \delta_s)} = \frac{2427.80 \cdot 10^6}{0.784 \cdot 400 \cdot 1600} - \frac{1226.16 \cdot 10^3}{(400 \setminus 1.15)} \\ &= 1313.36 \text{ mm}^2 \end{aligned}$$

$$\text{Check } A_{s_{min.}} \quad A_{s_{req.}} = 1313.36 \text{ mm}^2$$

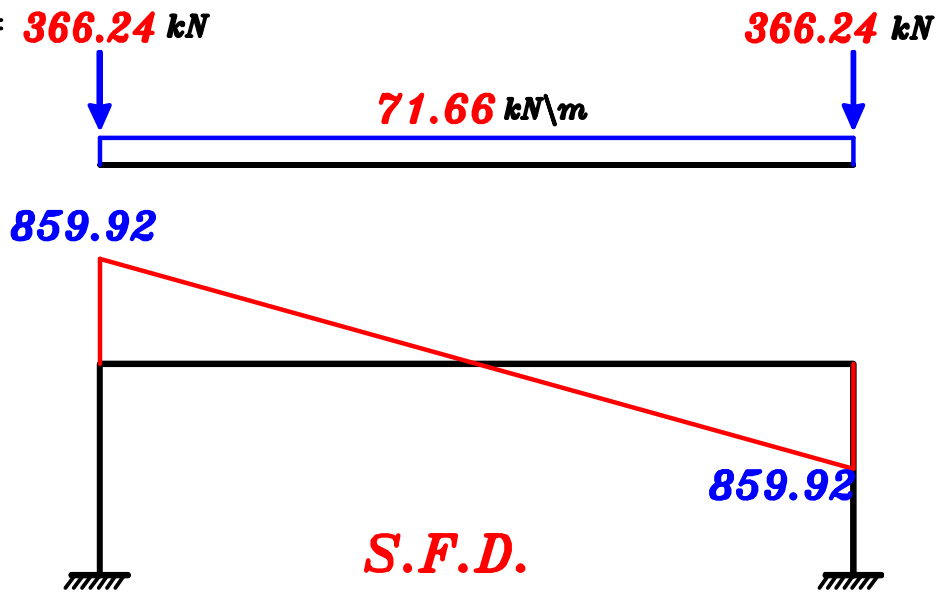
$$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{30}}{400} \right) 400 \cdot 1600 = 1971.8 \text{ mm}^2$$

$$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$$

$$\begin{aligned} A_{s_{min.}} &= 0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} b d = \left(0.225 \cdot \frac{\sqrt{30}}{400} \right) 400 \cdot 1600 = 1971.8 \\ 1.3 A_{s_{req.}} &= 1.3 \cdot 1313.36 = 1707.37 \\ \text{st. } 400/600 \quad \frac{0.15}{100} b d &= \frac{0.15}{100} \cdot 400 \cdot 1600 = 960 \end{aligned} \quad \left. \begin{array}{l} \text{الأقل} \\ \text{الأكثر} \end{array} \right\} = 1707.37 \text{ mm}^2$$

$4 \Phi 25$

Check Shear.



$$q_U = \frac{Q_{max}}{b d} = \frac{859.92 \times 10^3}{400 \times 1500} = 1.43 \text{ N/mm}^2$$

$$q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

$$q_{cu} = 0.70 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.70 \sqrt{\frac{30}{1.5}} = 3.13 \text{ N/mm}^2$$

$\therefore q_{cu} < q_U < q_{max}$. \therefore We need Stirrups more Than $5 \phi 8 \text{ m}$

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \delta_s)}{b S}$$

* Take $n = 2$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.43 - \frac{1.07}{2} = \frac{2 \times 50.3 (240 \times 1.15)}{400 \times S} \rightarrow S = 58.64 \text{ mm} < 100 \text{ mm}$$

* Take $n = 2$, $\phi 10 \rightarrow A_s = 78.5 \text{ mm}^2$

$$1.43 - \frac{1.07}{2} = \frac{2 \times 78.5 (240 \times 1.15)}{400 \times S} \rightarrow S = 91.5 \text{ mm} < 100 \text{ mm}$$

* Take $n = 4$, $\phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$

$$1.43 - \frac{1.07}{2} = \frac{4 \times 50.3 (240 \times 1.15)}{400 \times S} \rightarrow S = 117.29 \text{ mm} > 100 \text{ mm}$$

\therefore o.k.

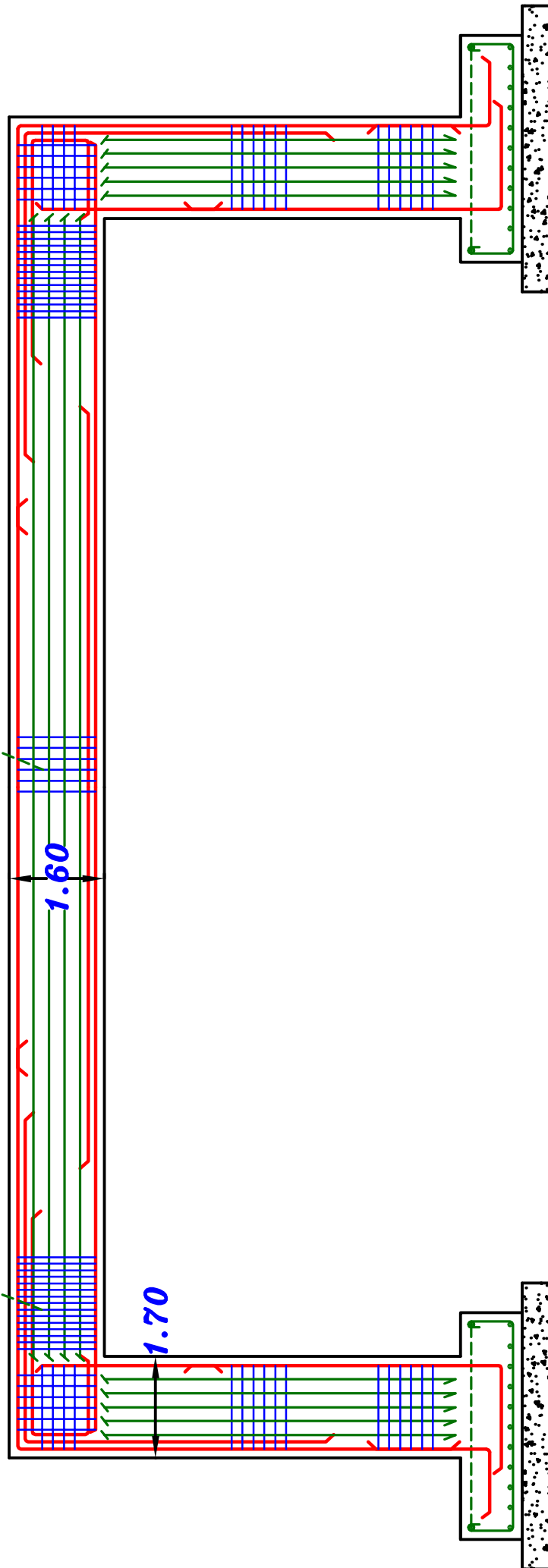
$$\therefore \text{No. of stirrups/m} = \frac{1000}{S} = \frac{1000}{117.29} = 8.52 = 9$$

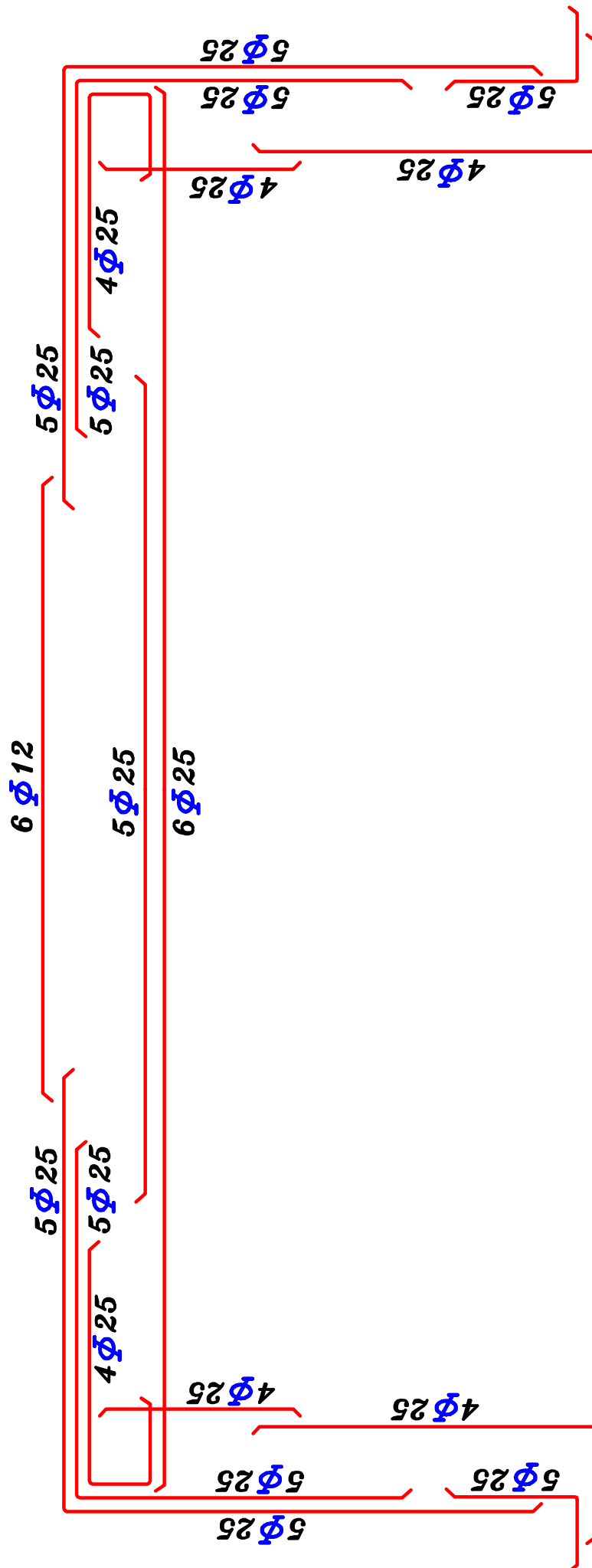
\therefore Use Stirrups **9 $\phi 8 \text{ m}$ 4 branches**

RFT. of Frame.

$5 \phi 8 \setminus m \hat{=}$ 2 branches

$9 \phi 8 \setminus m \hat{=}$ 4 branches

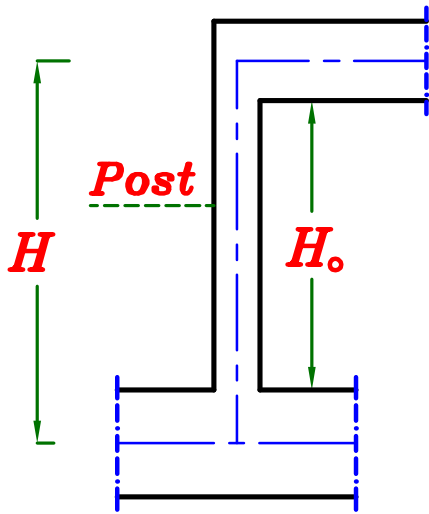




Note.



Posts.



إذا كان الارتفاع (H_o) لل *post*

أقل من أو يساوي ٢,٥٠ م

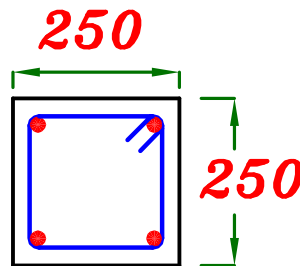
فعاده يكون *Short Column*

و عاده يؤخذ القطاع ($250 * 250$)

و التسليح $4 \phi 12$

Short Column

$4 \phi 12$



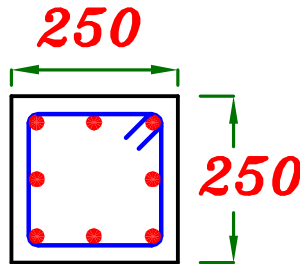
إذا كان الارتفاع (H_o) لل *post* يتراوح من ٢,٥٠ م إلى - ٤,٠ م

فسيتحول إلى *Long Column* و لكن يظل القطاع ($250 * 250$)

و سنأخذ التسليح $8 \phi 12$

Long Column

$8 \phi 12$



إذا كان الارتفاع (H_o) لل *post* أكبر من - ٤,٠ م

فهذا حل غير مفضل و إذا اضطررنا له سنجعل القطاع ($b * b$)

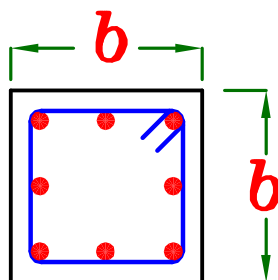
حيث b عرض ال *system* الذي يحمل ال *post*

و يعتبر *Long Column*

و سنأخذ التسليح $8 \phi 12$

Long Column

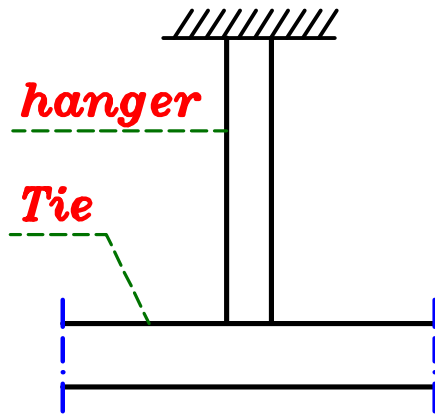
$8 \phi 12$



Hangers.

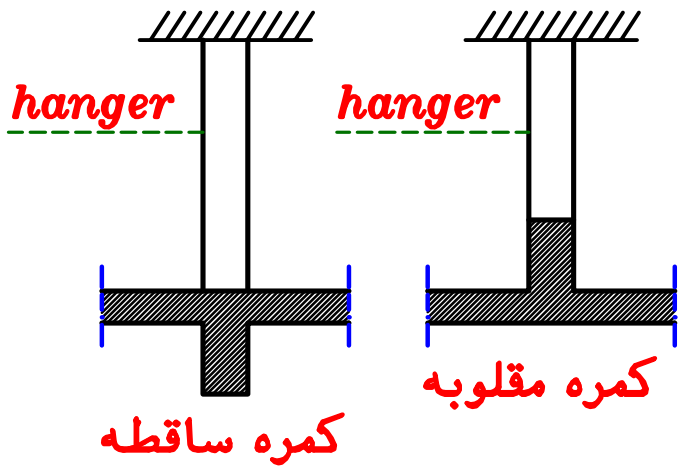
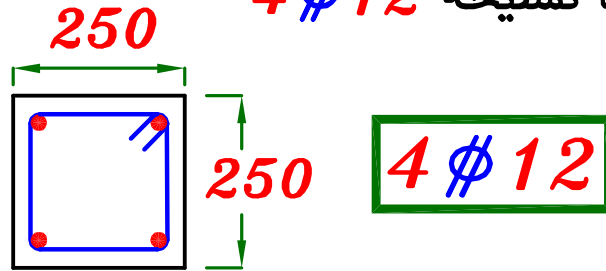
ال **Hangers** يؤثر عليها **tension** لذا الارتفاع لن يؤثر عليها

لانه لا يوجد عليها **buckling** لذا عاده نأخذ ابعاد القطاع (250 * 250) مهما كان الارتفاع .



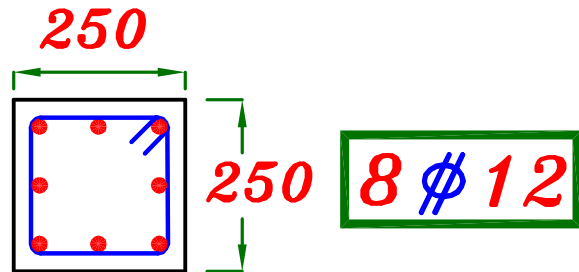
اذا كان ال **Hanger** يحمل وزن ال **Tie** فقط

فعاده نأخذ تسليحه 4 # 12



اذا كان ال **Hanger** يحمل وزن كمره

فعاده نأخذ تسليحه 8 # 12



لن يفرق اذا كانت الكمره ساقطه او مقلوبه لانه في الحالتين

سيدخل تسليح ال **Hanger** داخل الكمره .

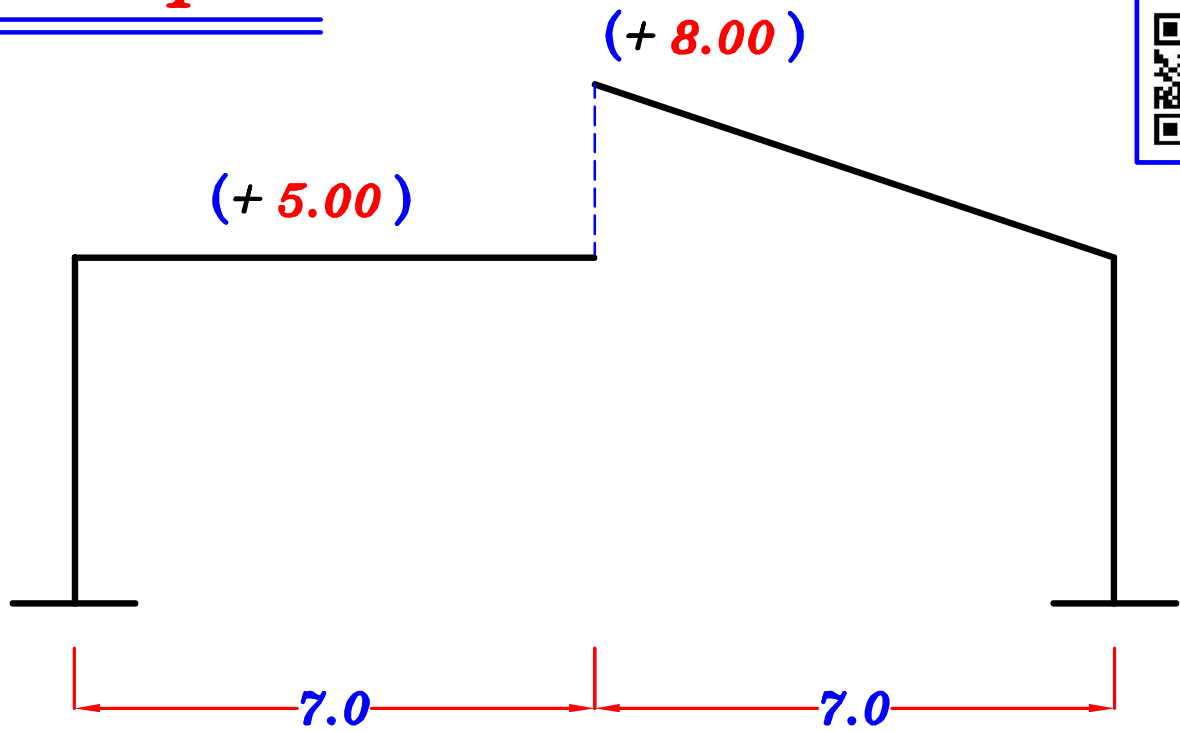
ملحوظه .

اذا كان هناك خيارين ان نحمل الكمرات على **Hanger** او **Post**

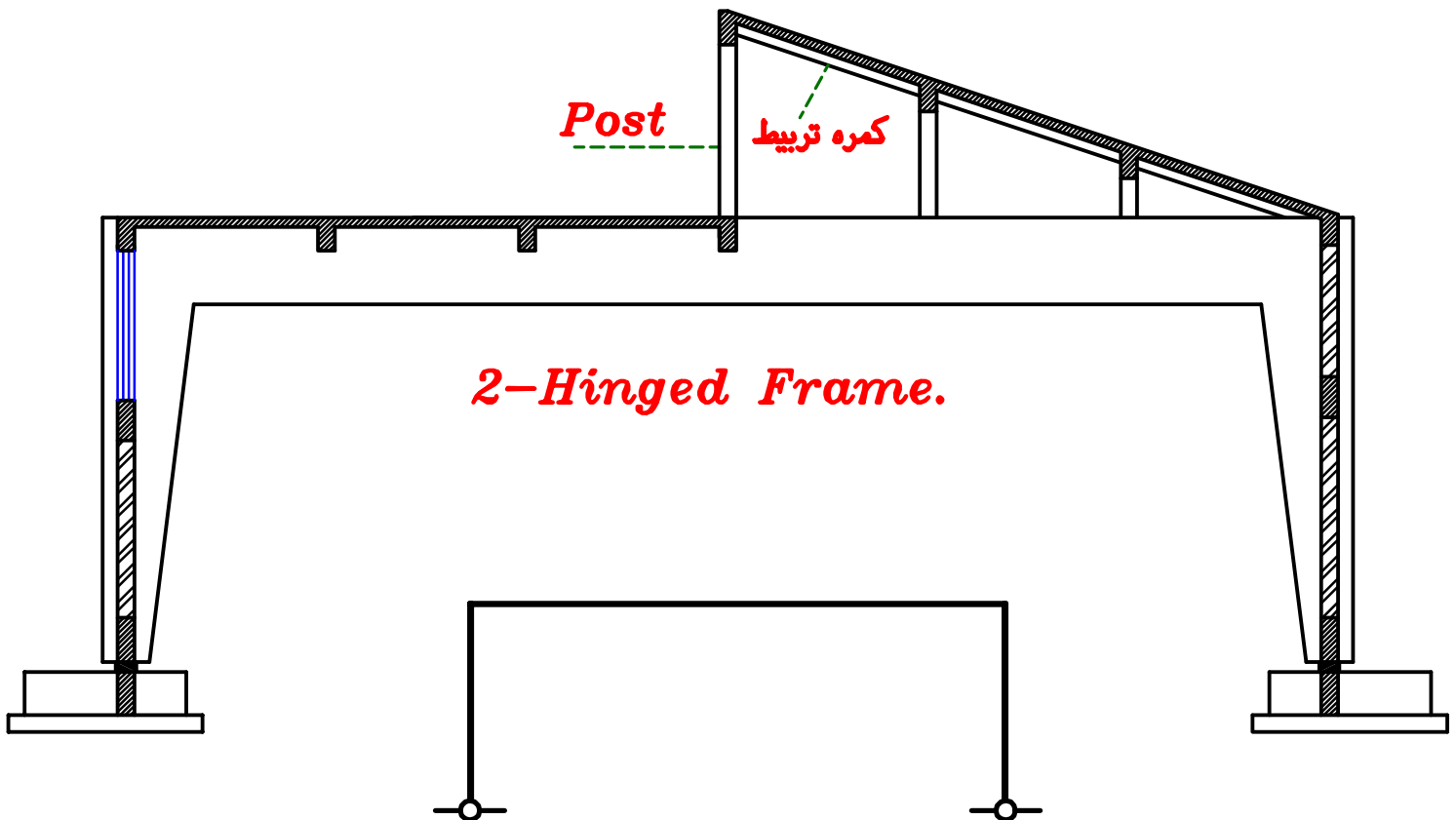
فعاده نفضل استخدام ال **Post** الا اذا زاد ارتفاع ال **Post** عن ٤م

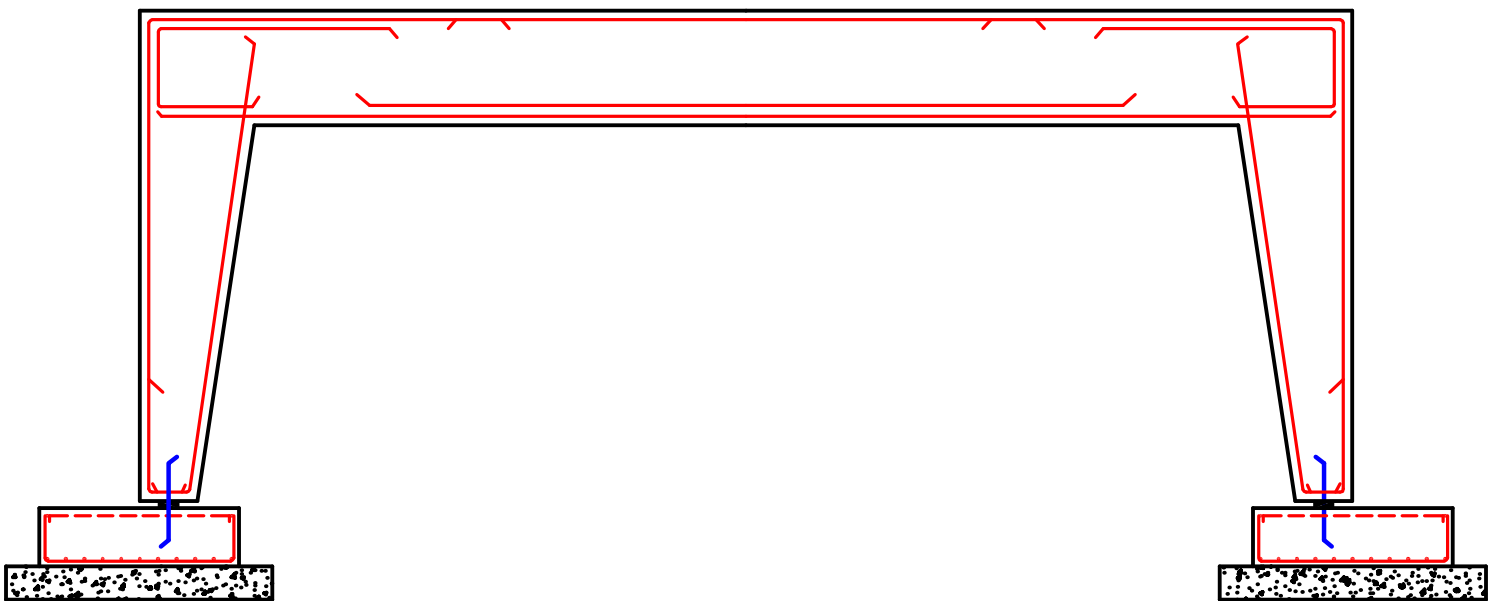
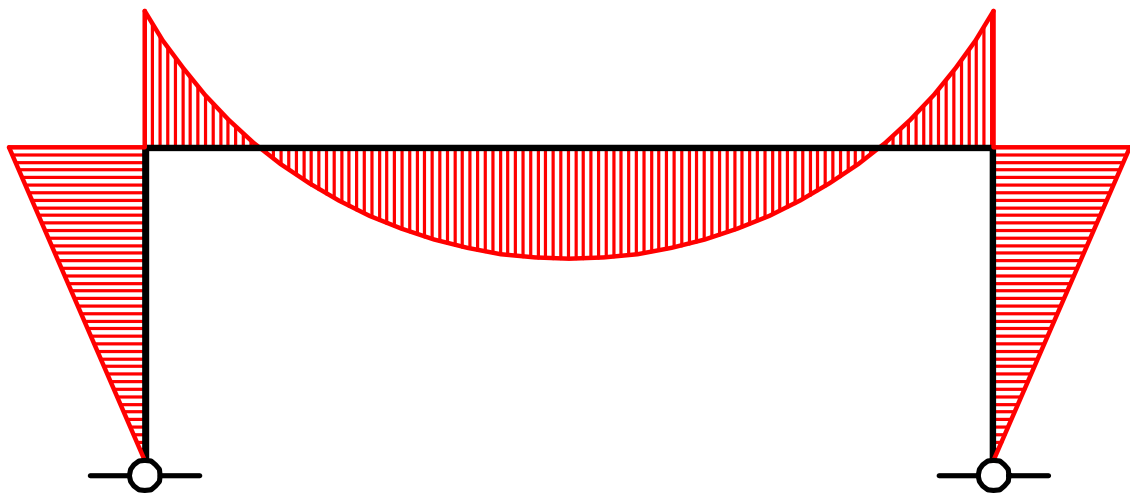
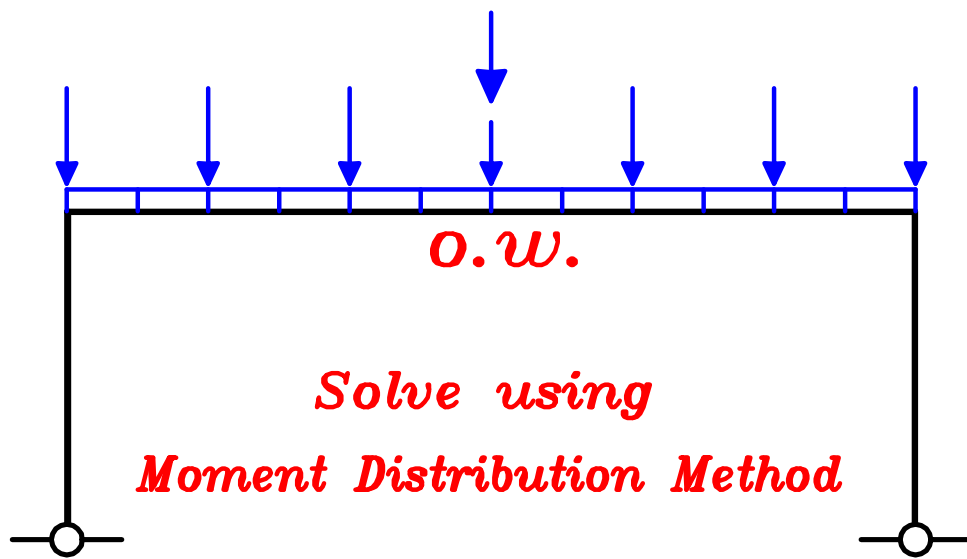
فسيكون استخدام ال **Hanger** افضل .

Example.

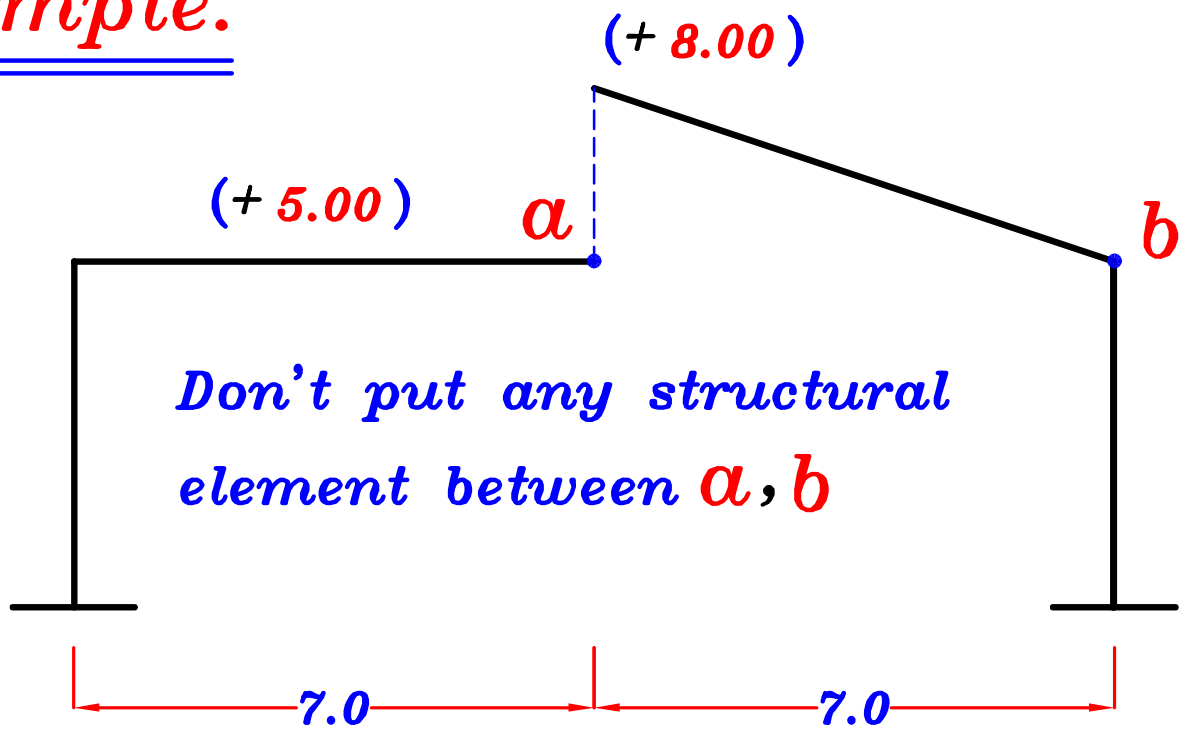


Choose a convenient Statical System and draw a sketch
For an elevation Showing Concrete Dimensions & RFT.



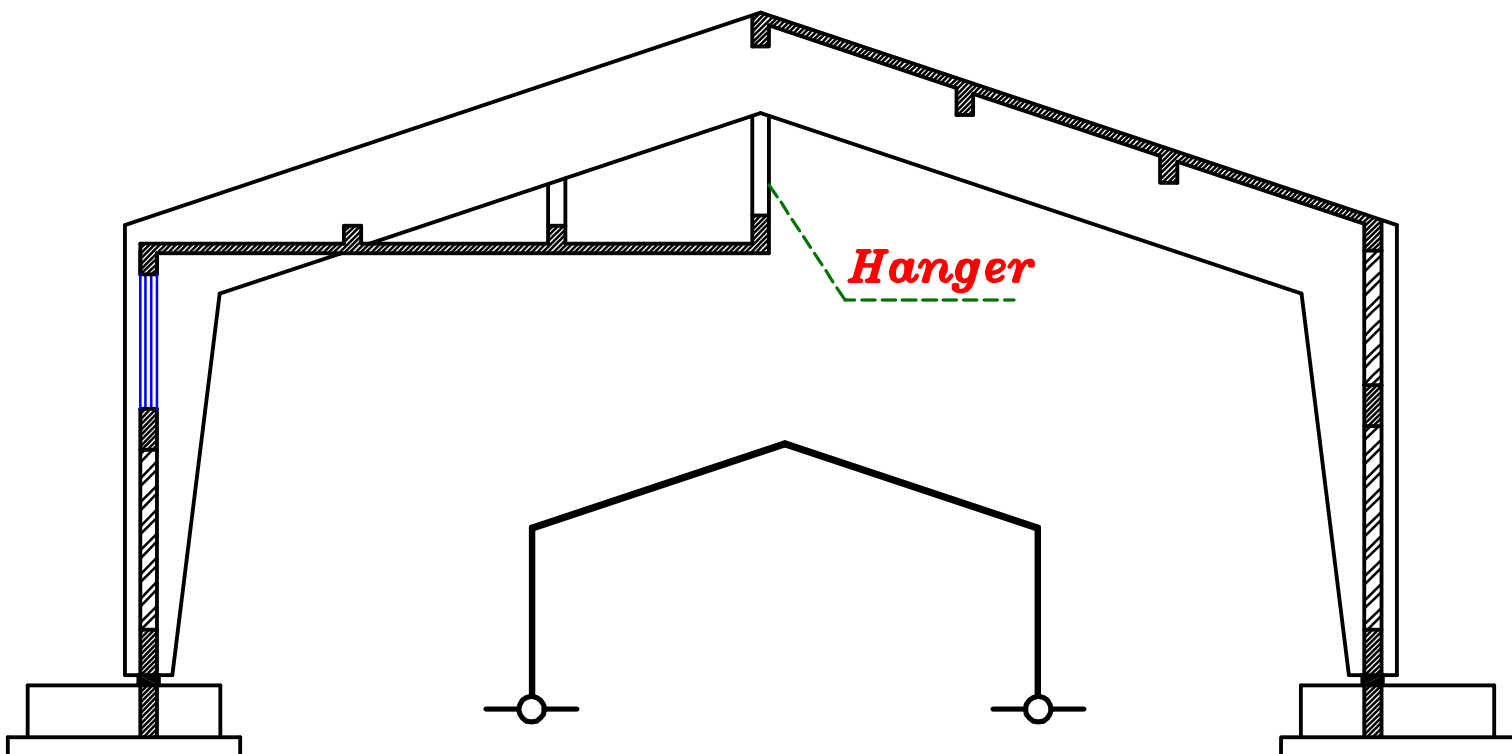


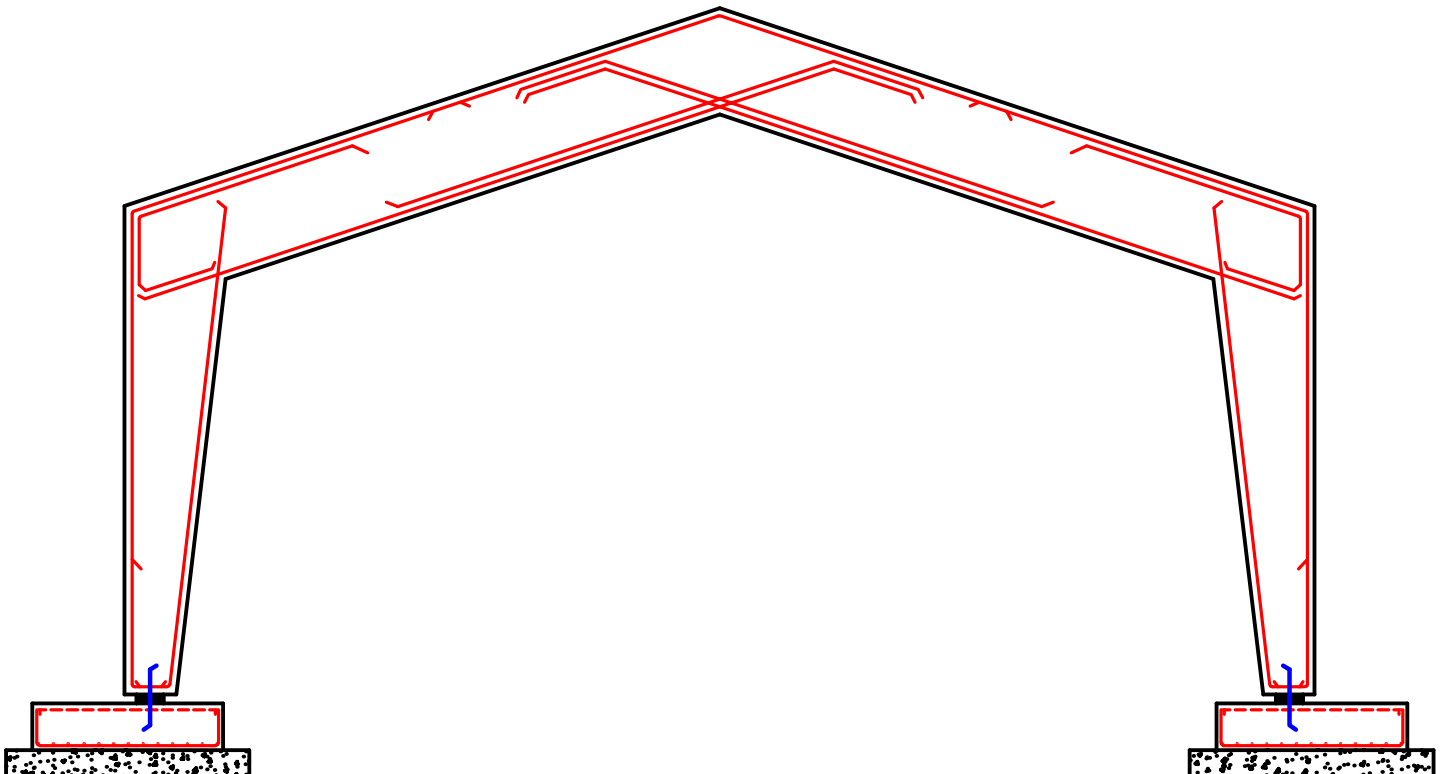
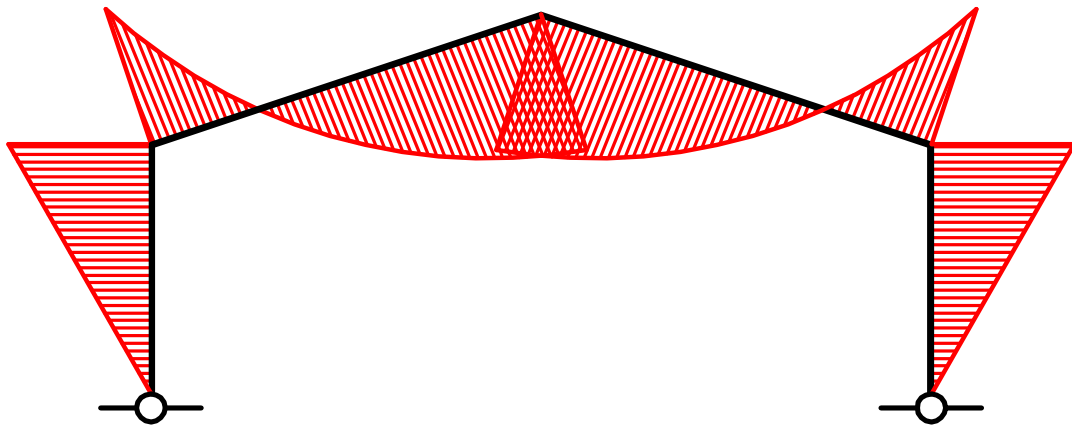
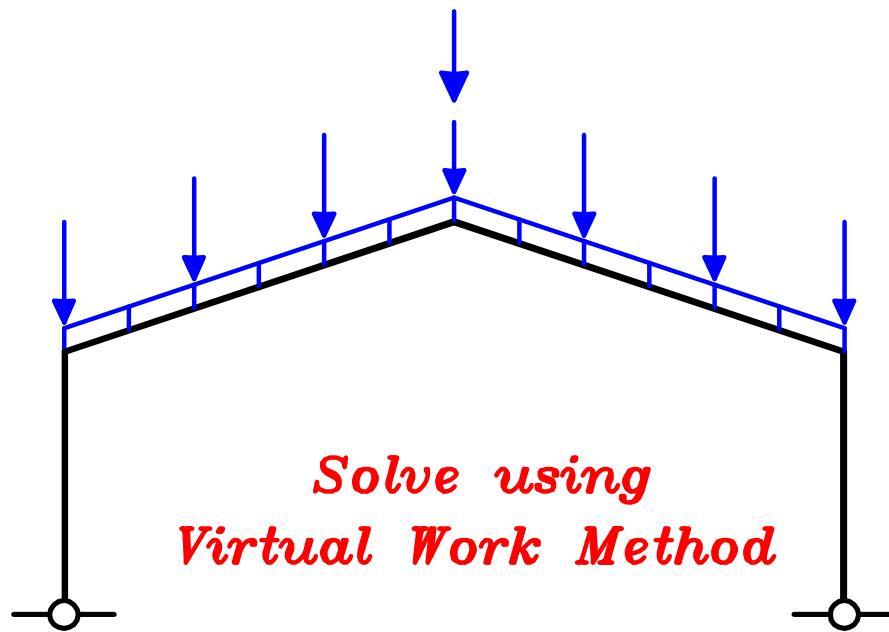
Example.



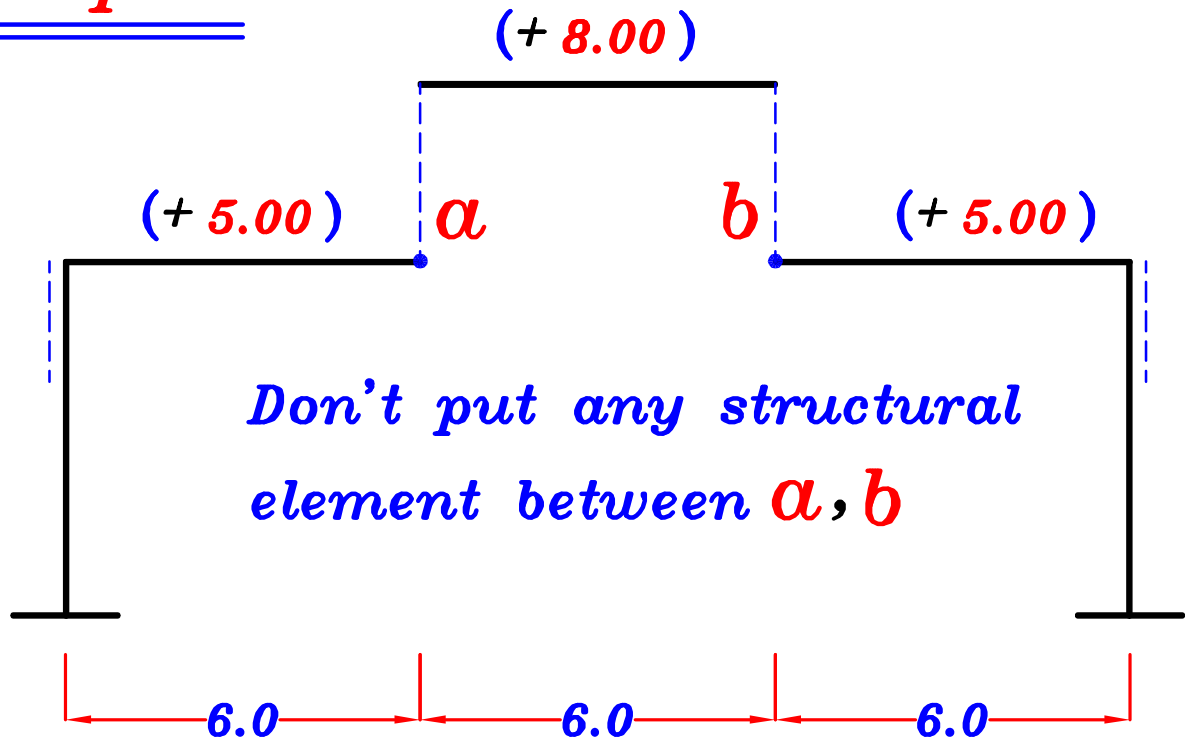
Choose a convenient Statical System and draw a sketch For an elevation Showing Concrete Dimensions & RFT.

2-Hinged Inclined Frame.



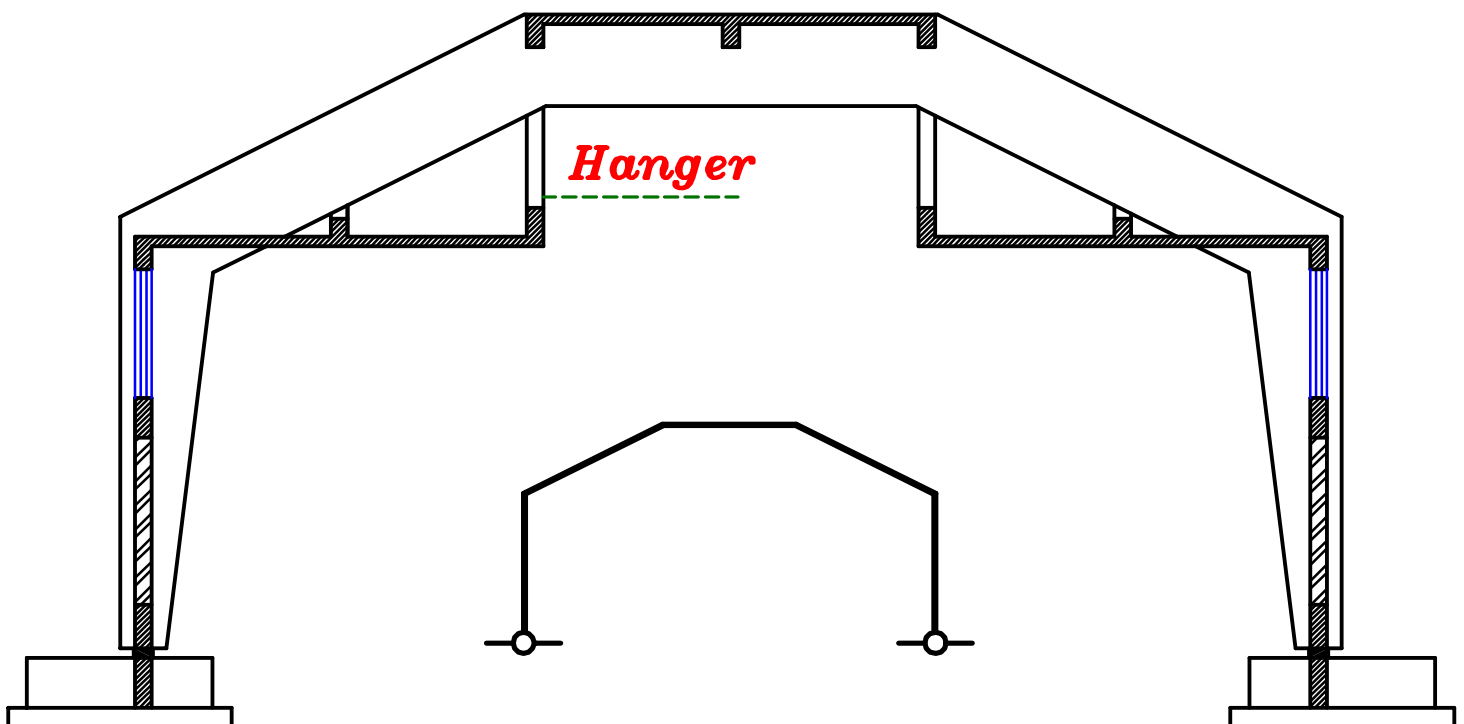


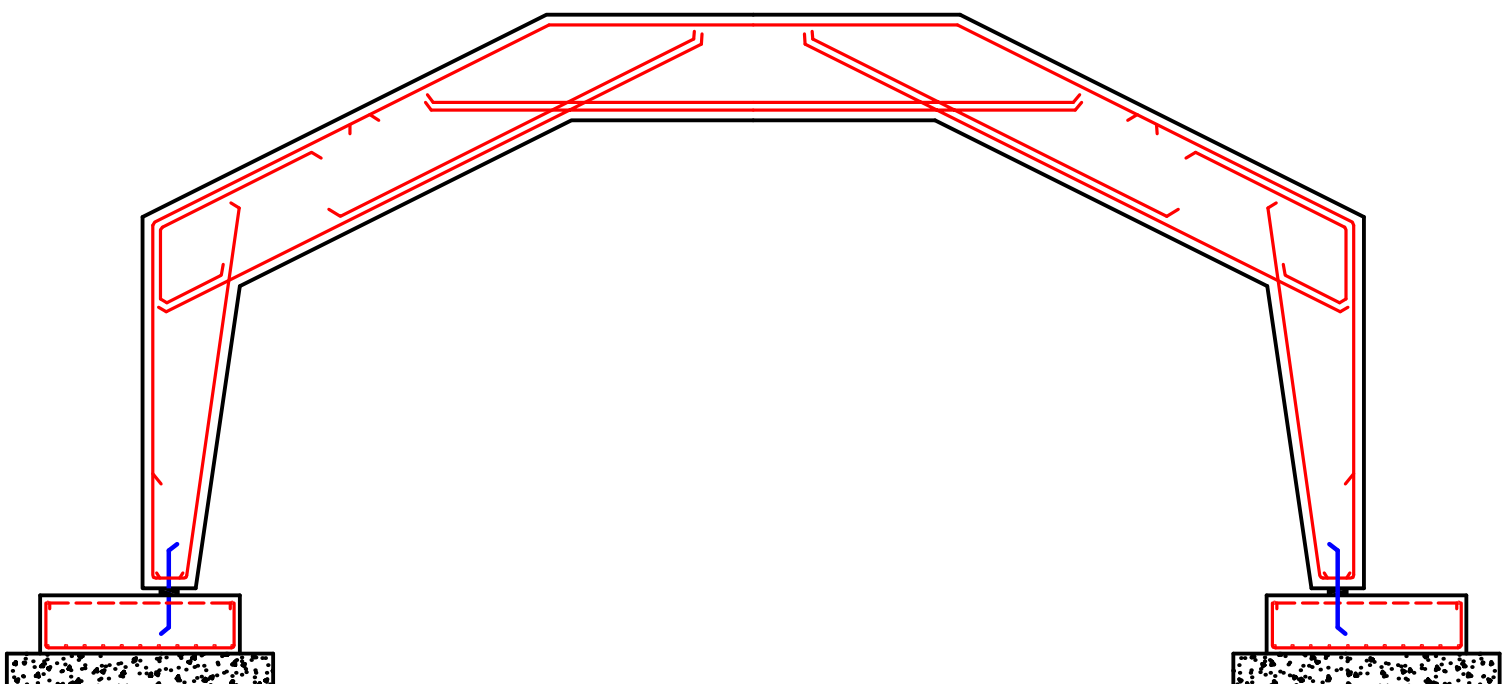
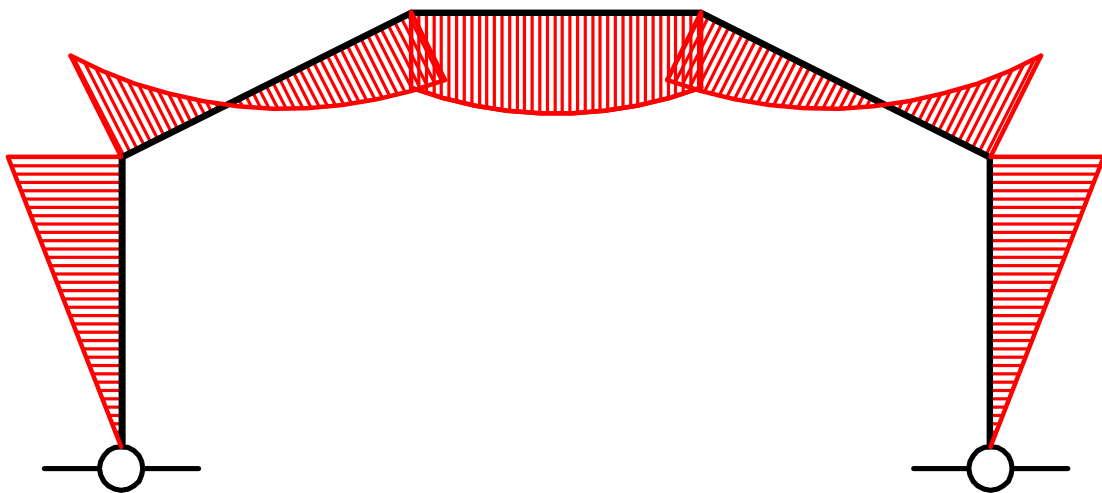
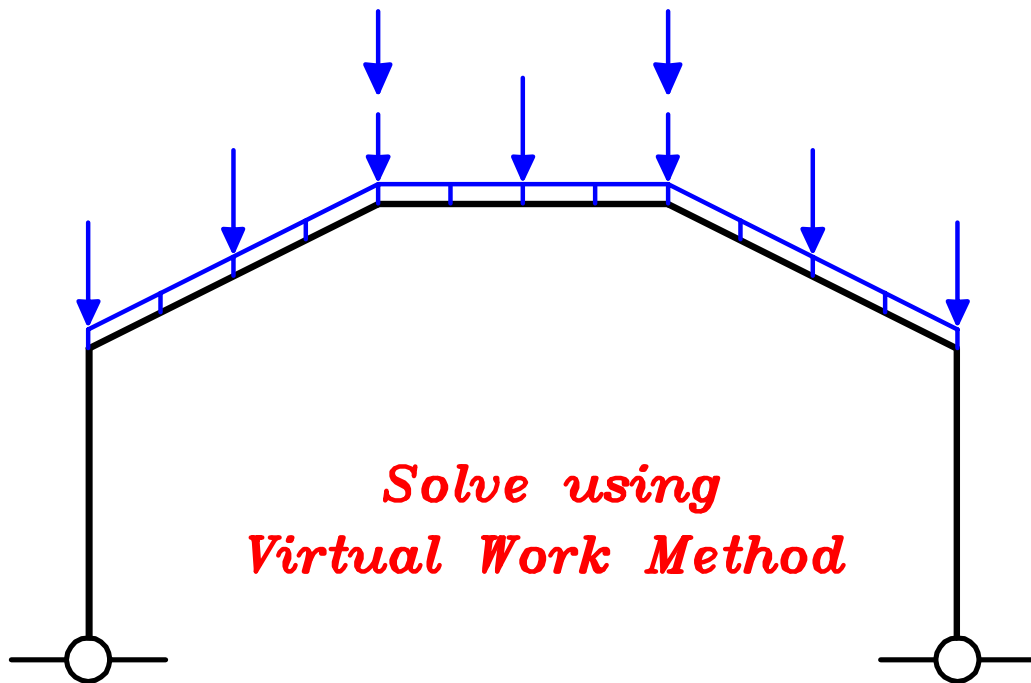
Example.



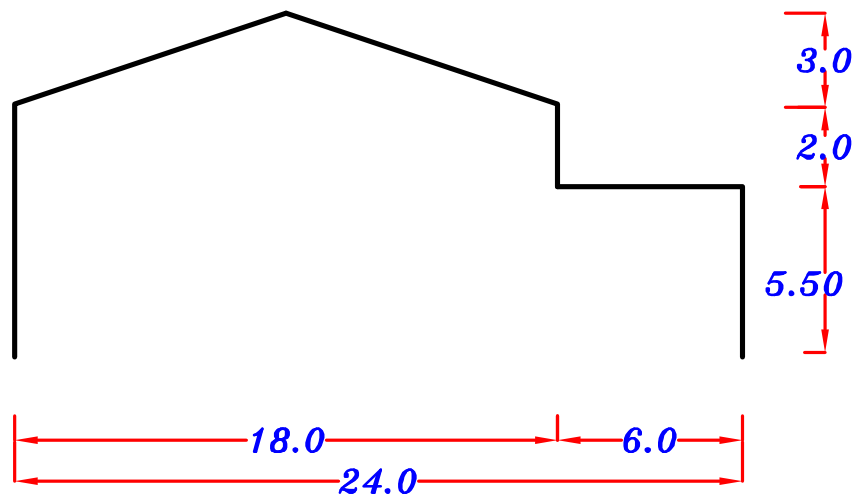
Choose a convenient Statical System and draw a sketch For an elevation Showing Concrete Dimensions & RFT.

2-Hinged Inclined Frame.

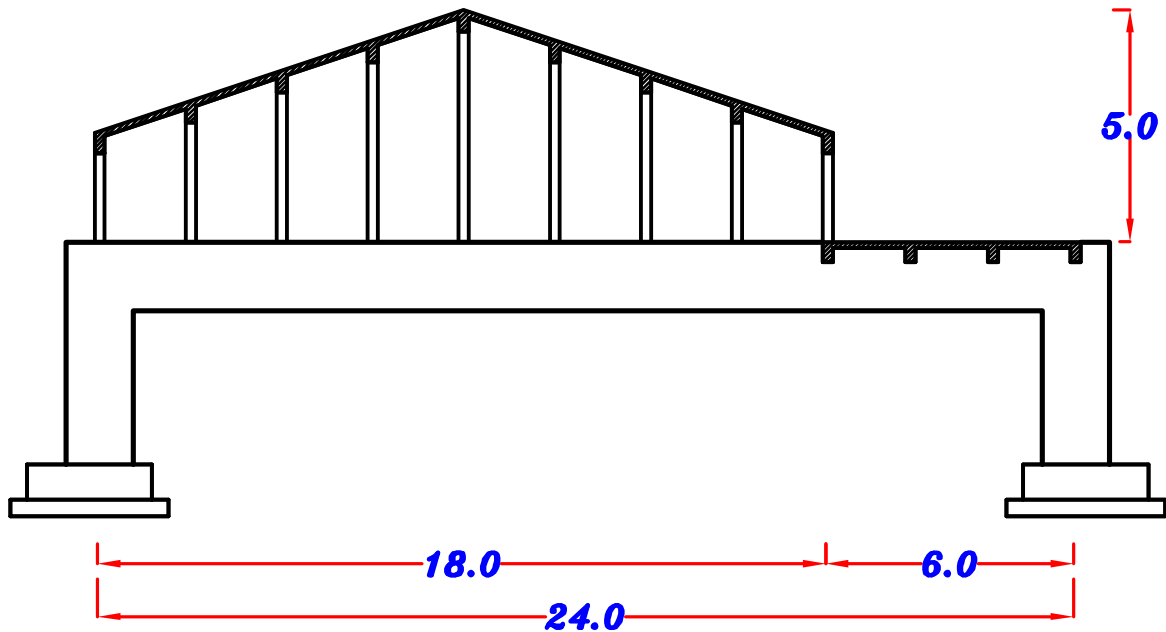




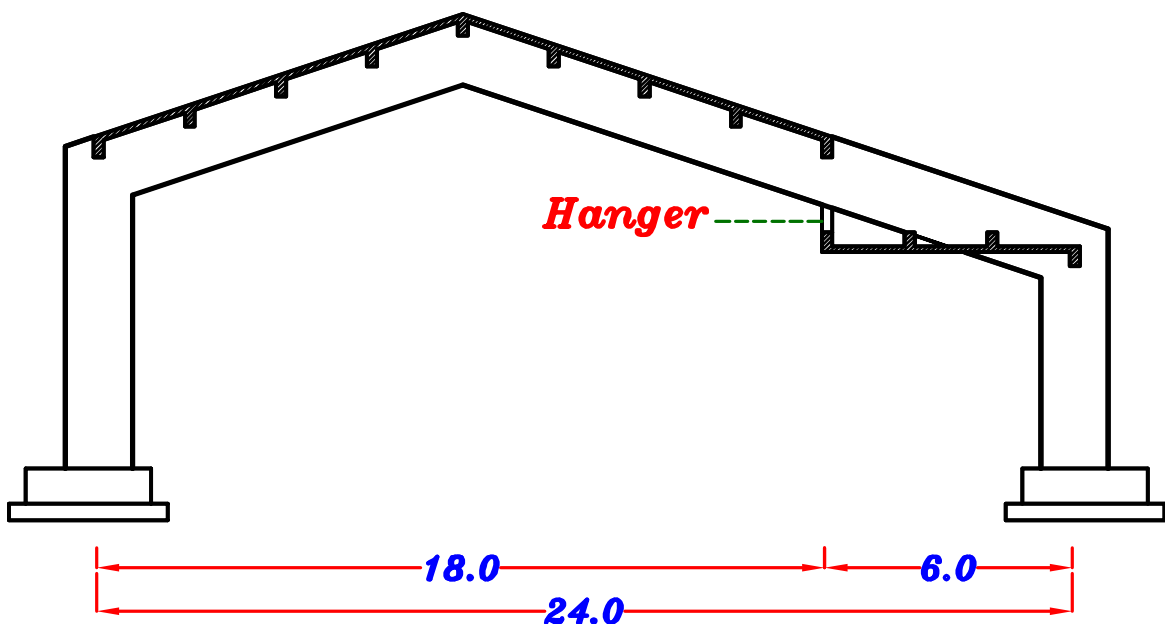
Note.



إذا اخترنا البلاطة محمولة على **post** و ال **post** محمول على **Frame** أفقي في هذه الحالة سيوجد **post** ارتفاعه 5.0 و هذا بالطبع حل سيئ و لكن ليس خطأ .

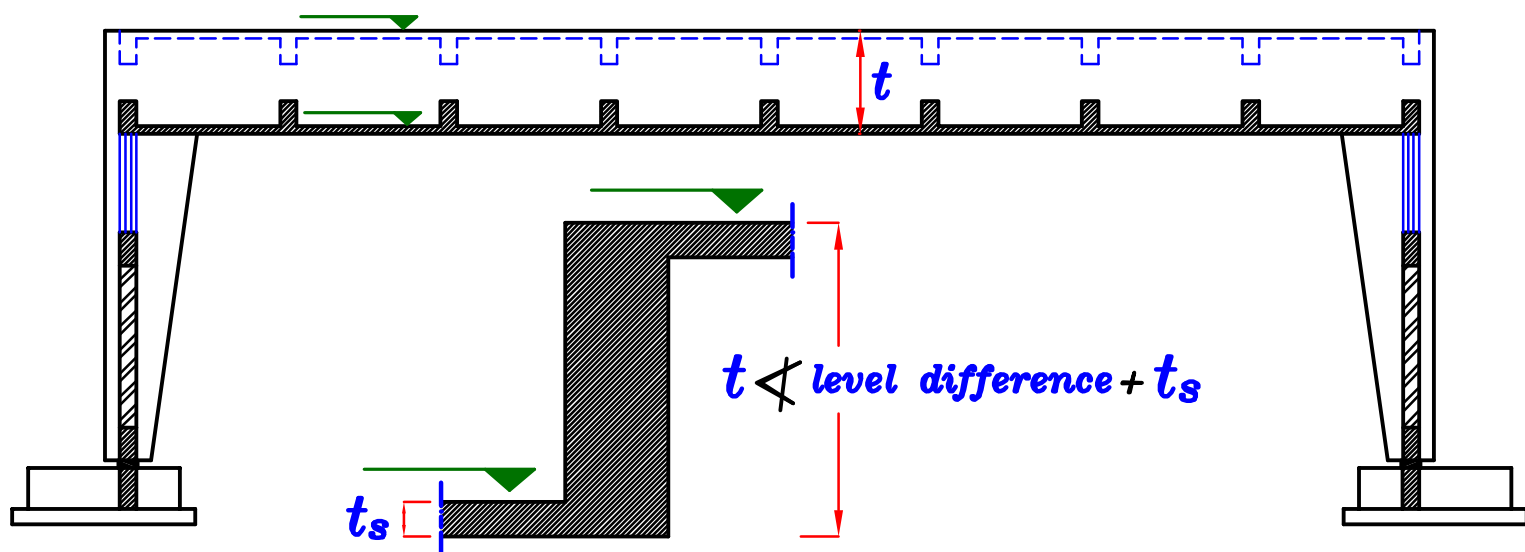
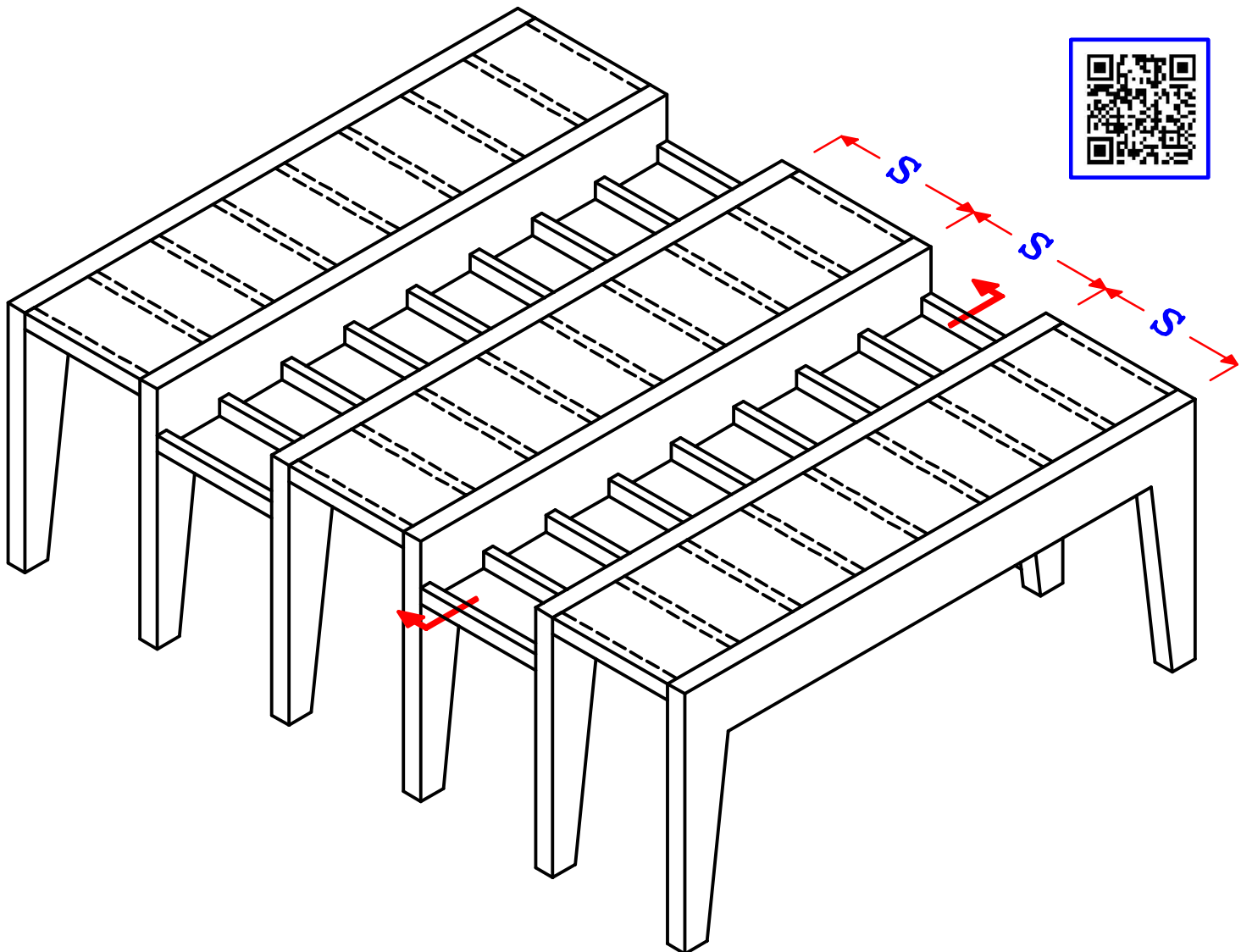


يفضل جعل البلاطة الأفقية محمولة على **Hanger**



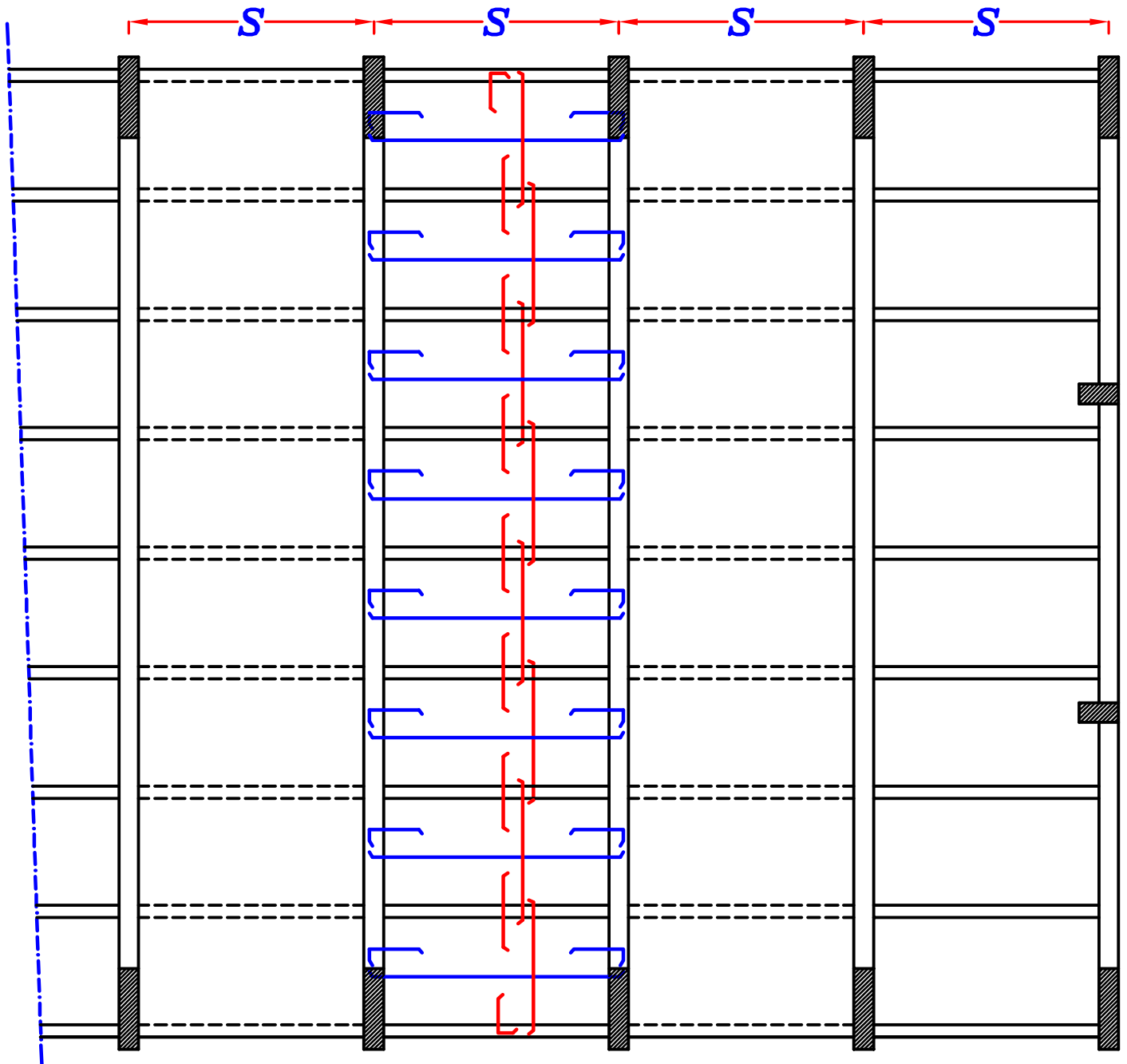
Note.

إذا كان ال **Frame** يحمل مباشرة بلاطات فى منسوبين مختلفين
فيفضل الا يزيد فق المنسوب بينهم عن - ٢٠ سم حتى لا يضطر لعمل عمق كبير جدا لل **Frame**
مما يعمل على زياده التكلفة .
فى بلاطات المنسوب الاقل يفضل أن تؤخذ كميات مقلوبه حتى لا نعمل على زياده عمق ال **Frame**

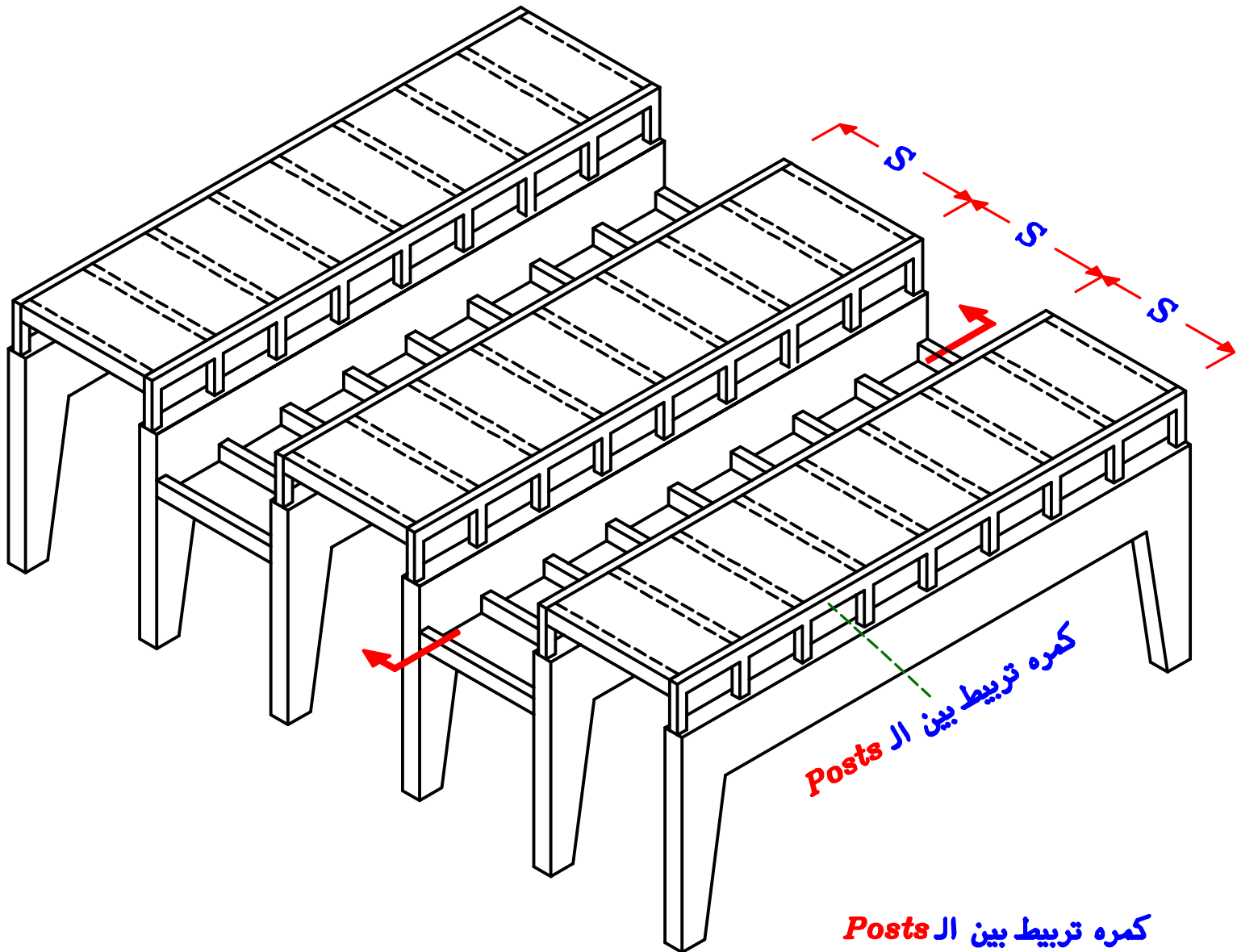


عمق ال **Frame** لا يقل عن فرق المنسوب بين البلاطتين مضاف اليه تخانه البلاطه السفليه .

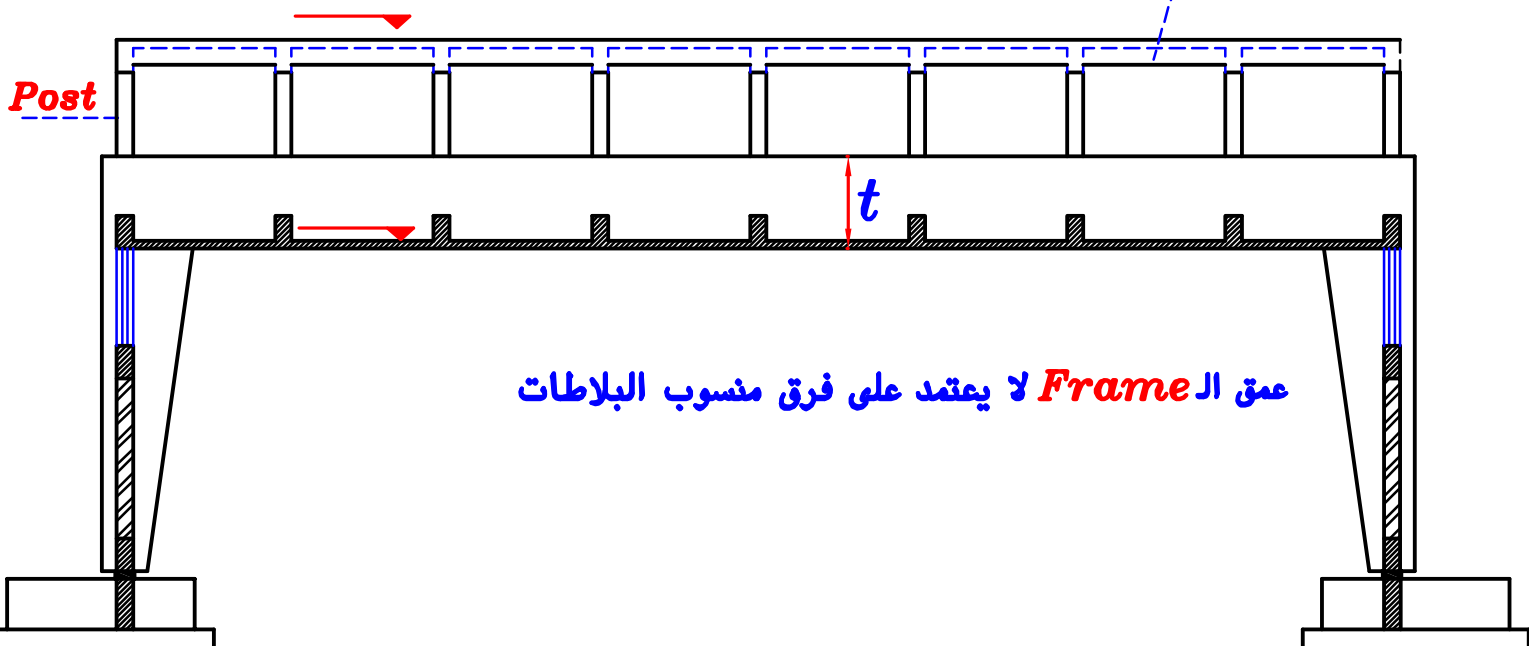
RFT. of the slab.



اما اذا زاد الفرق فى المنسوب بين البلاطتين عن - ٢,٣ م
 فيفضل ان يحمل ال **Frame** بلاطه منهم مباشرة و الاخرى
 تحمل اما على **Posts** أو على **Hangers**

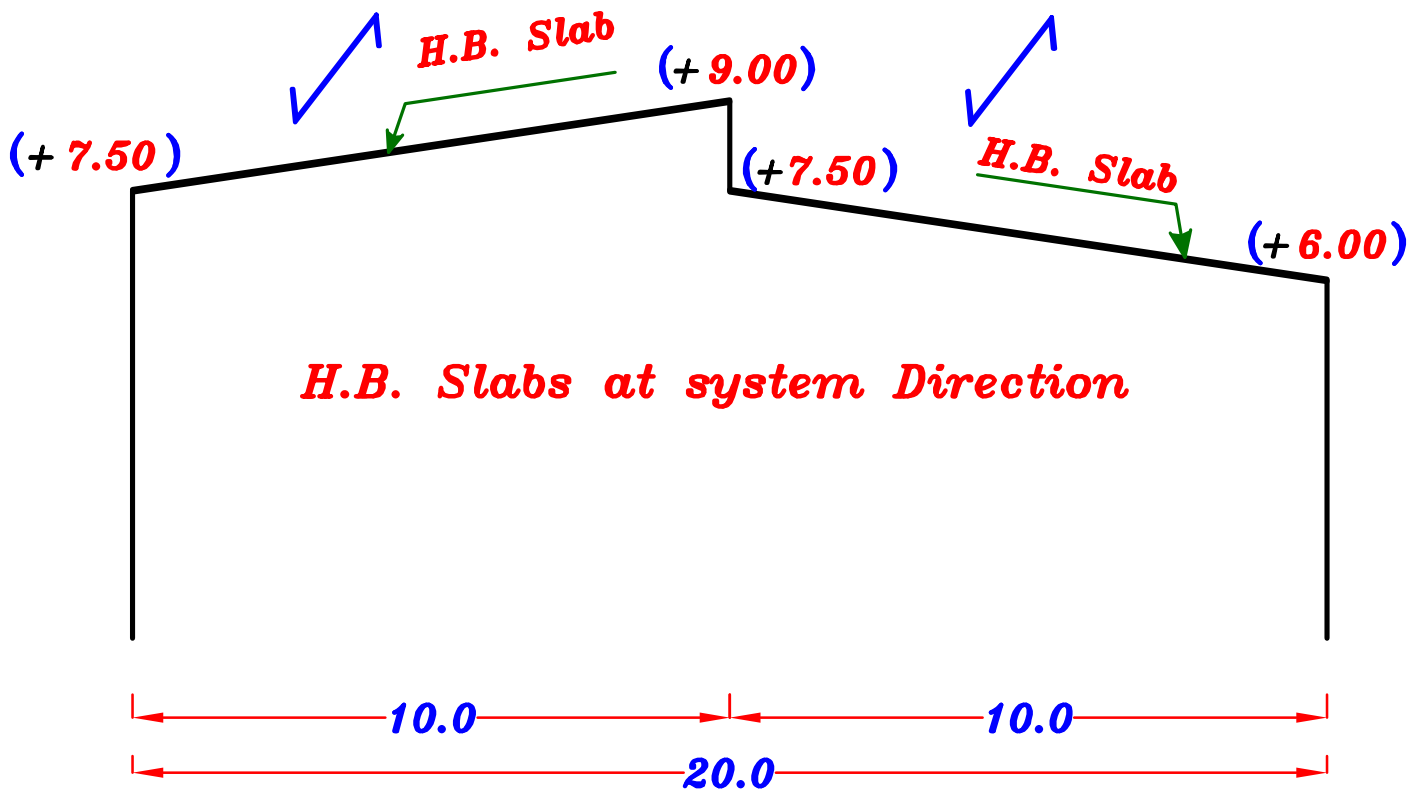


كمره تريبط بين ال **Posts**

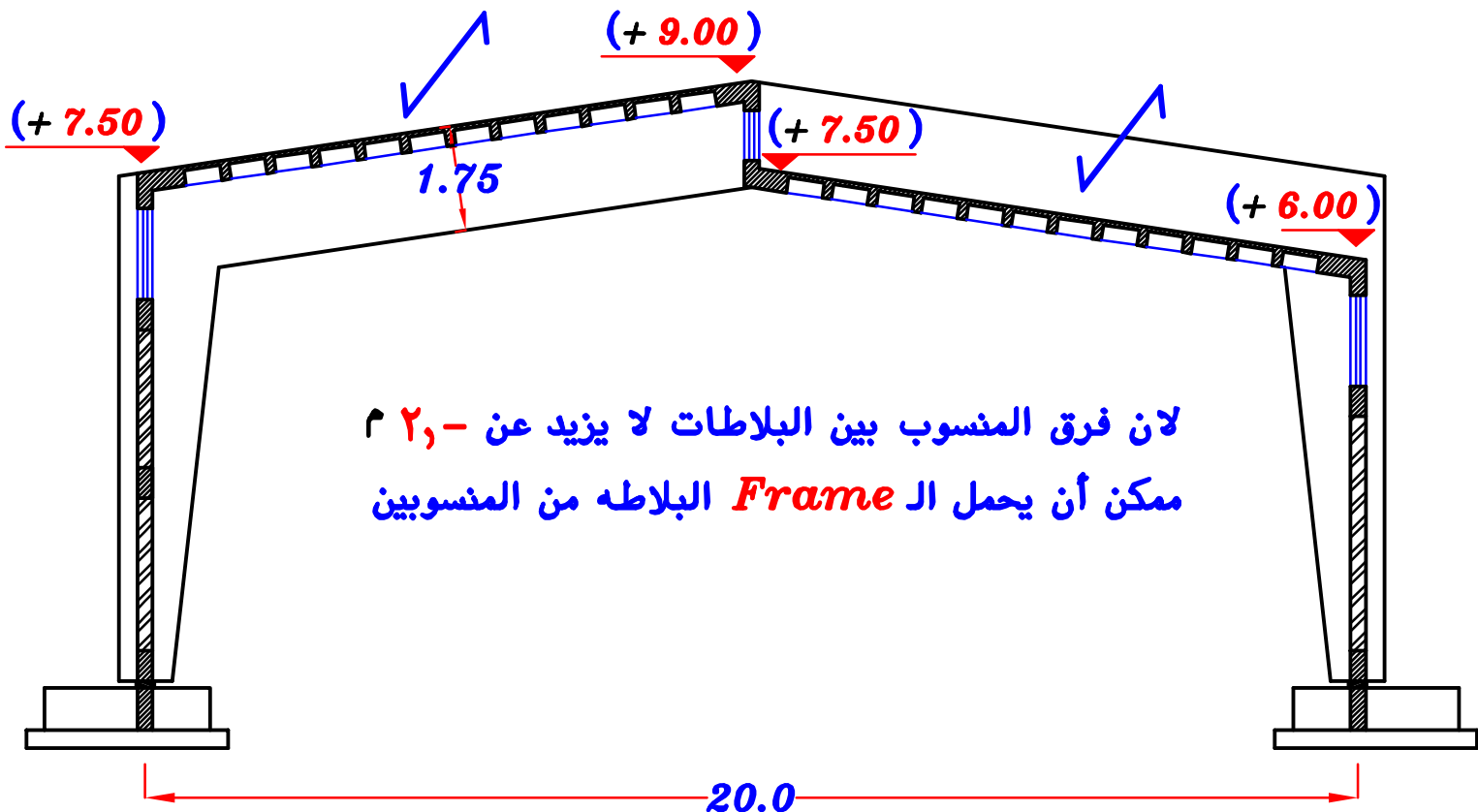


عمق ال **Frame** لا يعتمد على فرق منسوب البلاطات

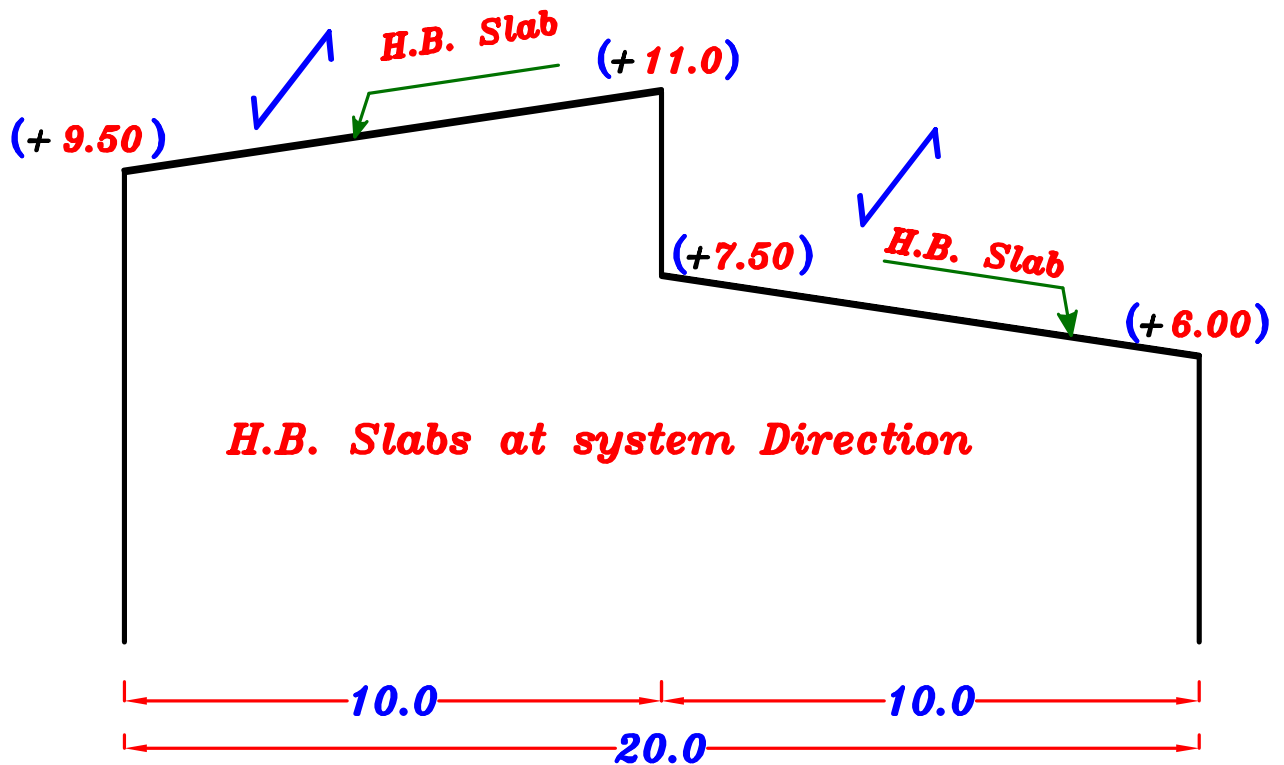
Example.



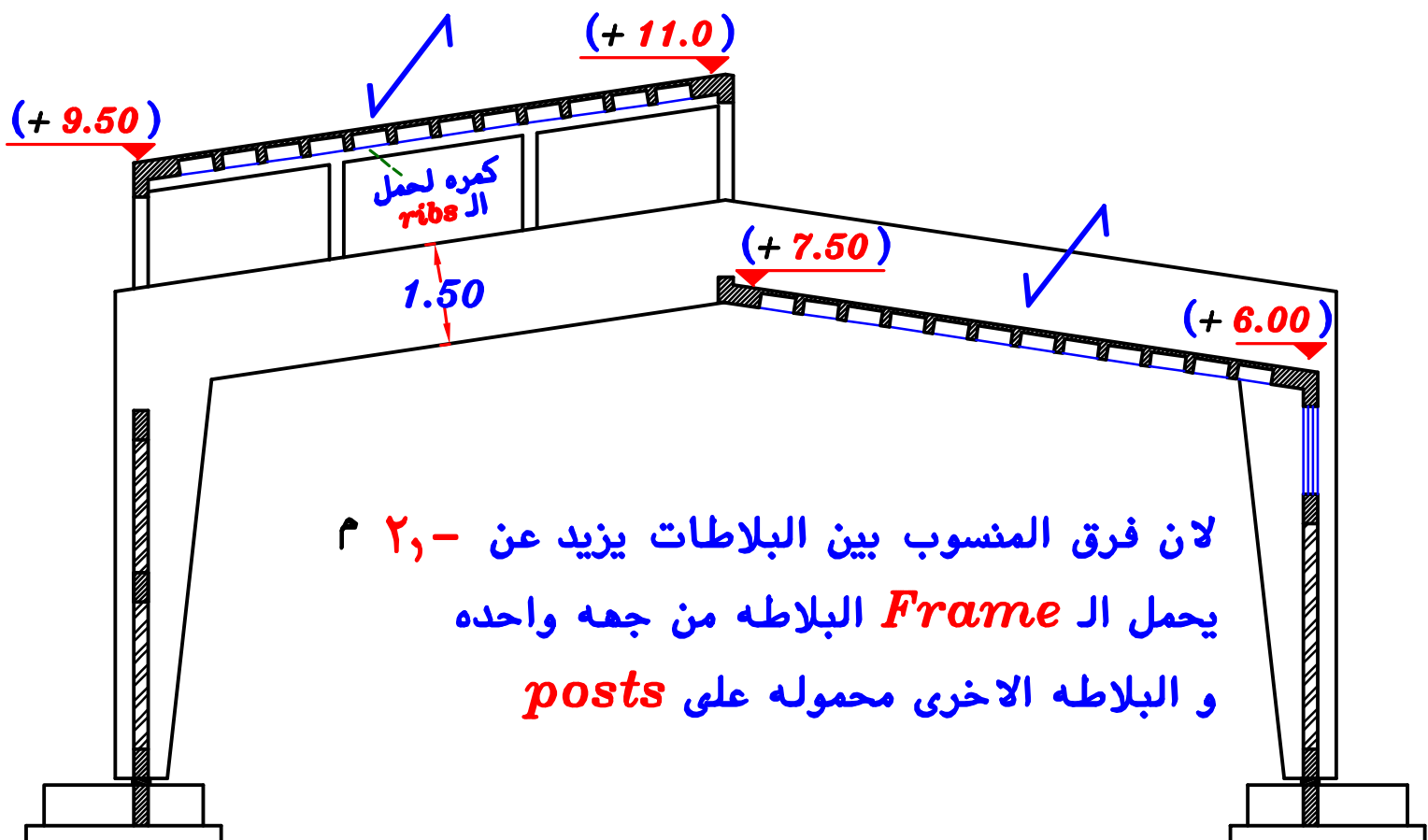
Choose a convenient Statical System and draw a sketch For an elevation Showing Concrete Dimensions.



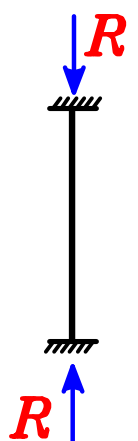
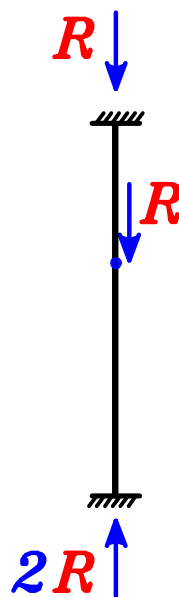
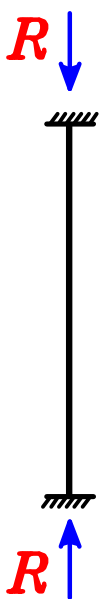
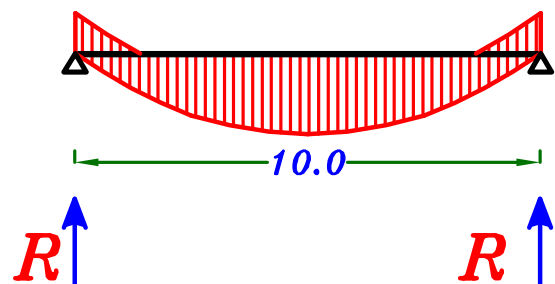
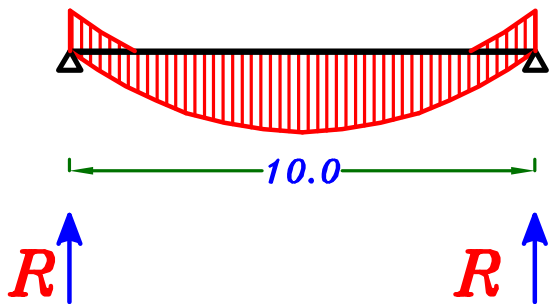
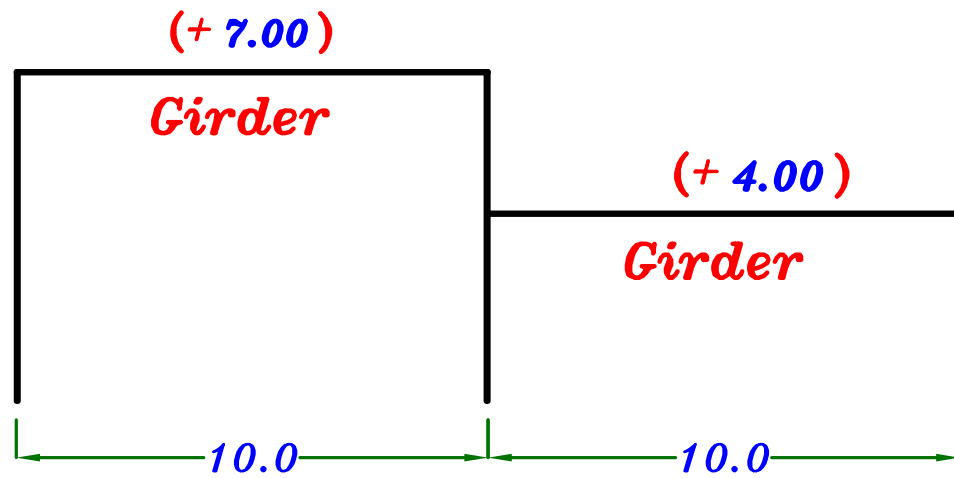
Example.

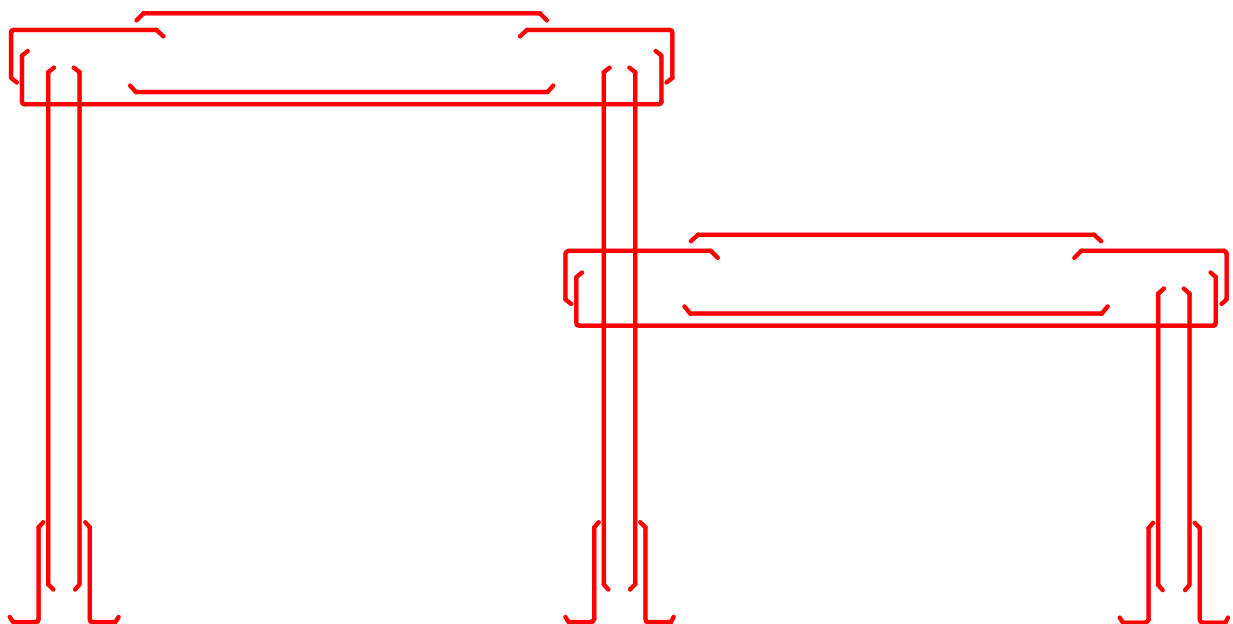
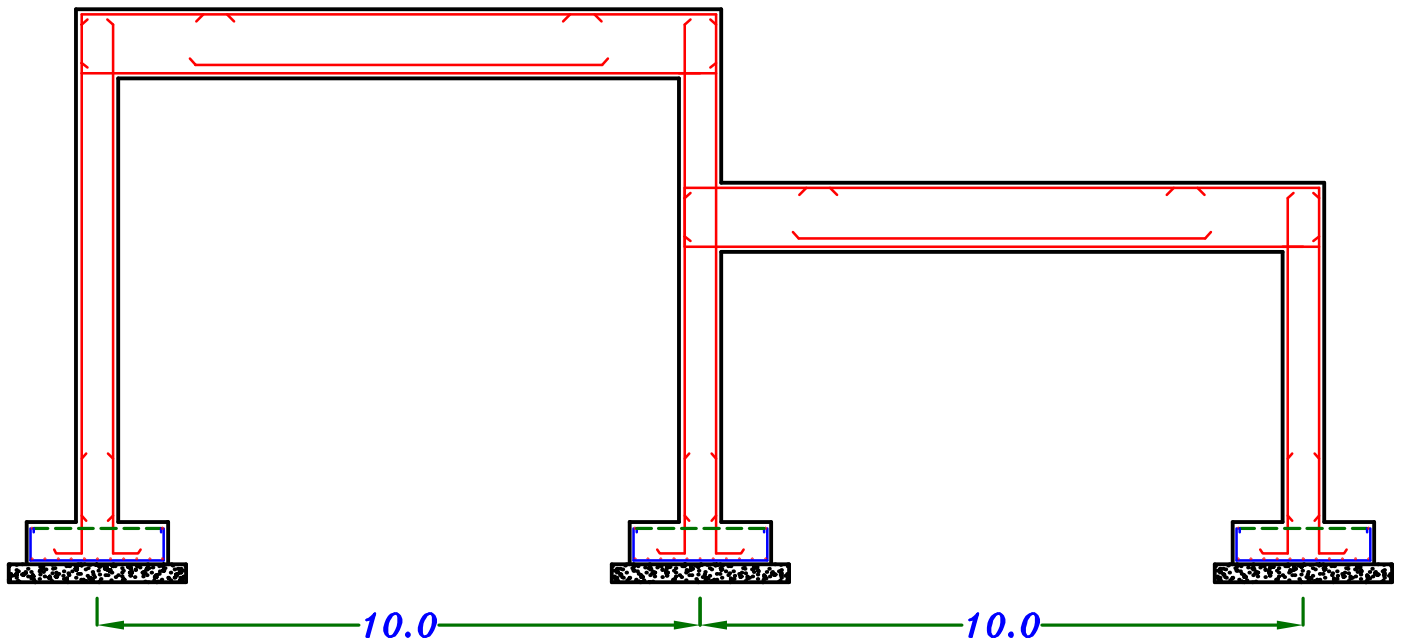
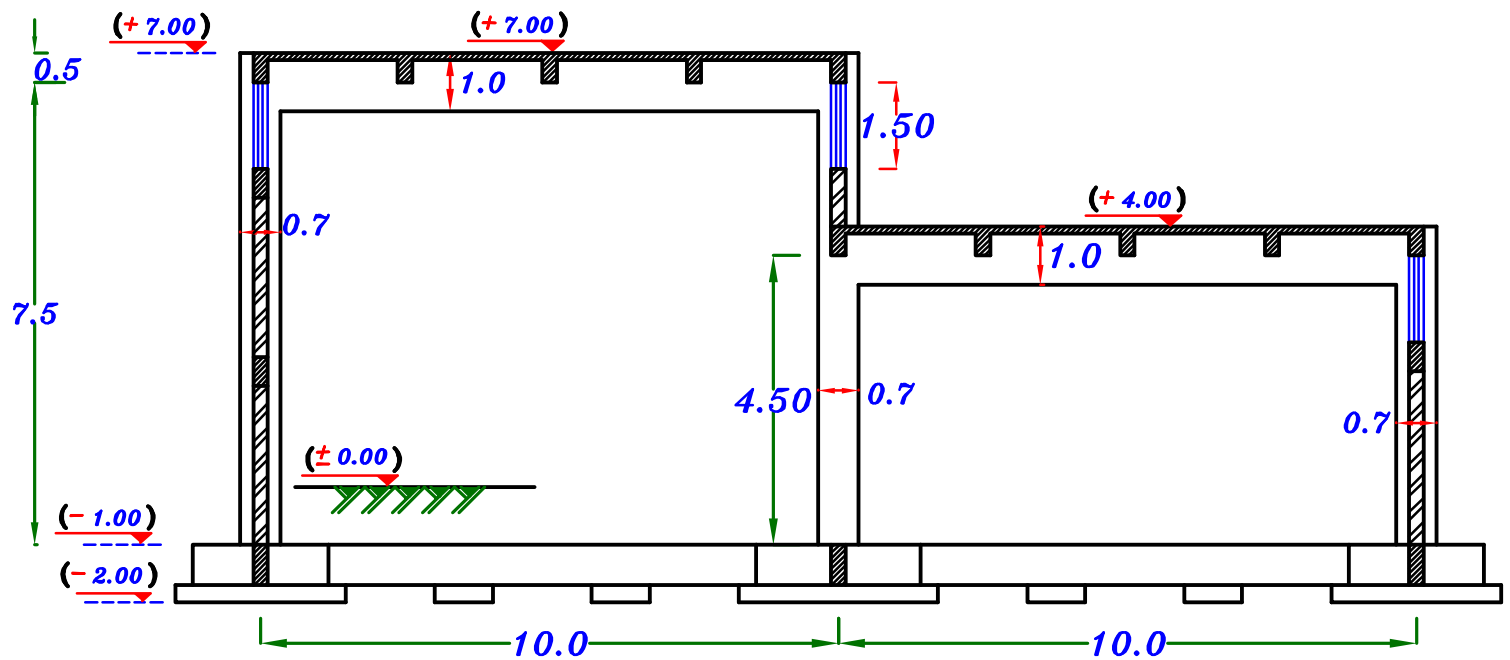


Choose a convenient Statical System and draw a sketch For an elevation Showing Concrete Dimensions.

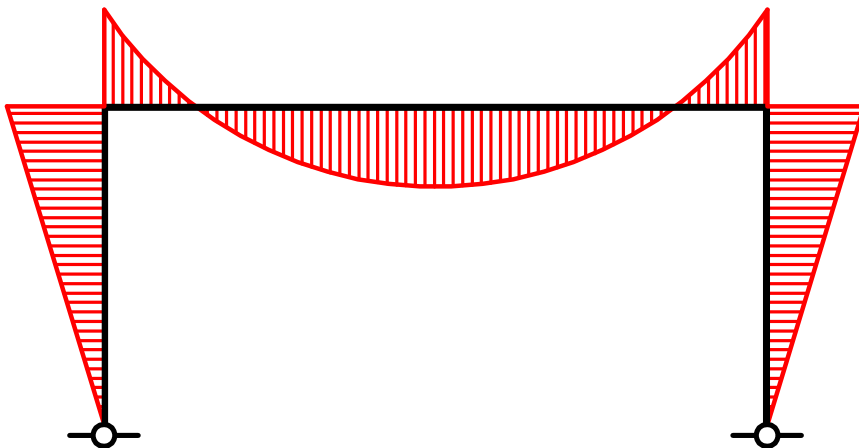
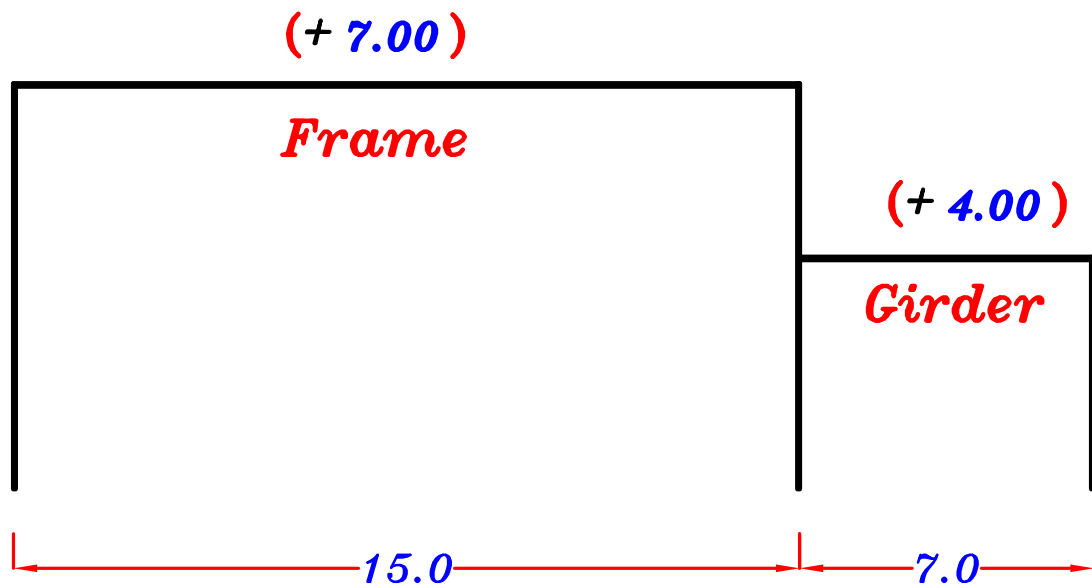


Connection between two Girders.

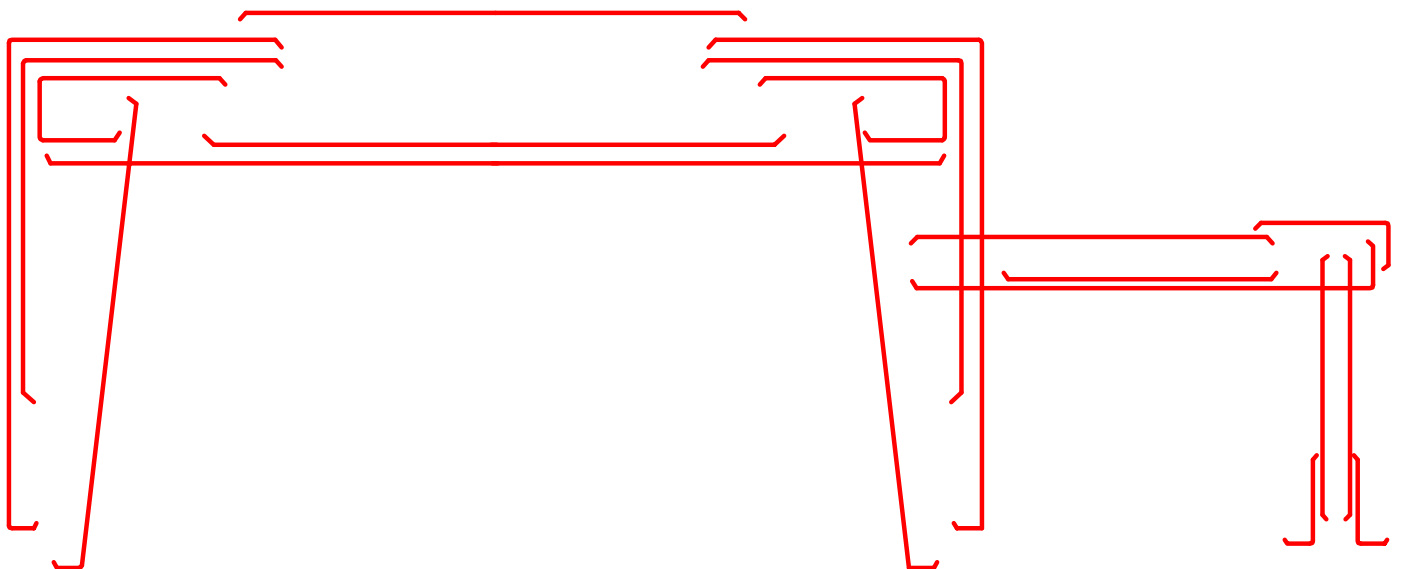
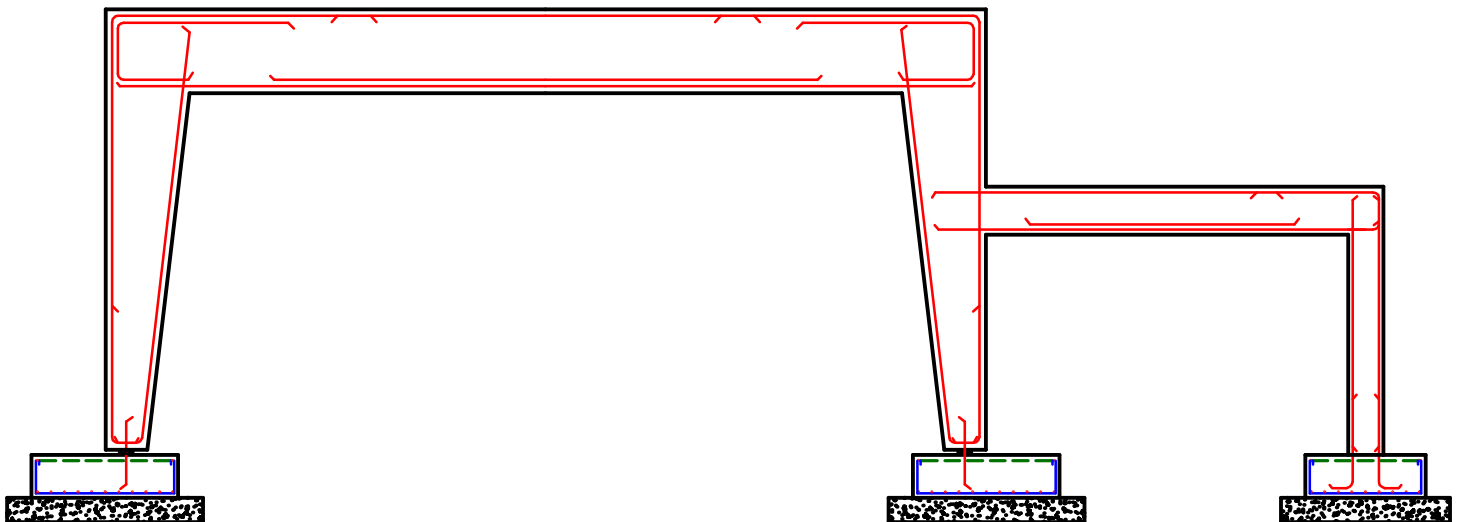
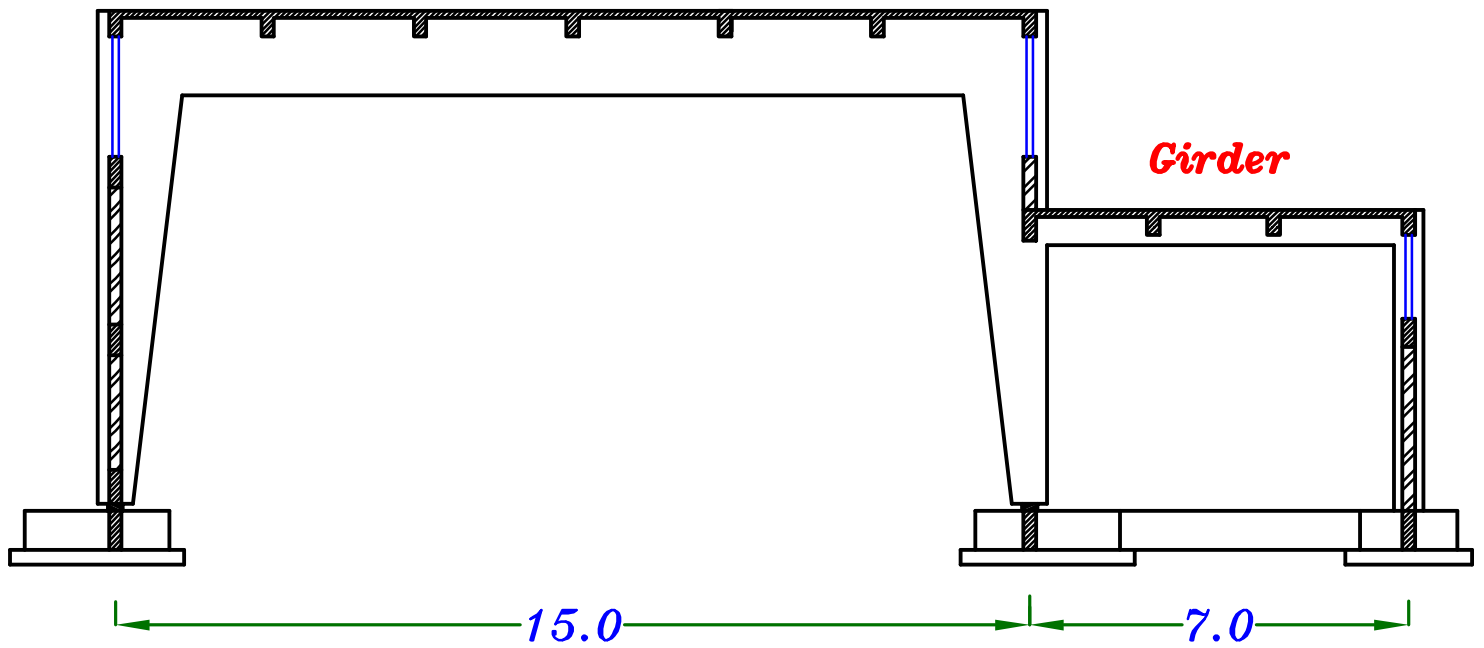




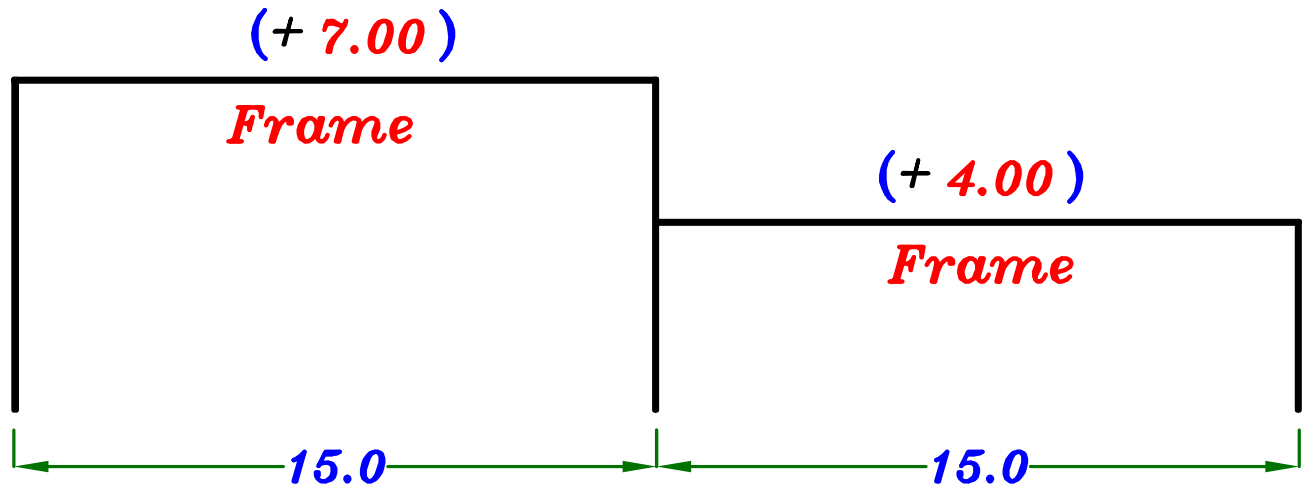
Connection between Girder & Frame.



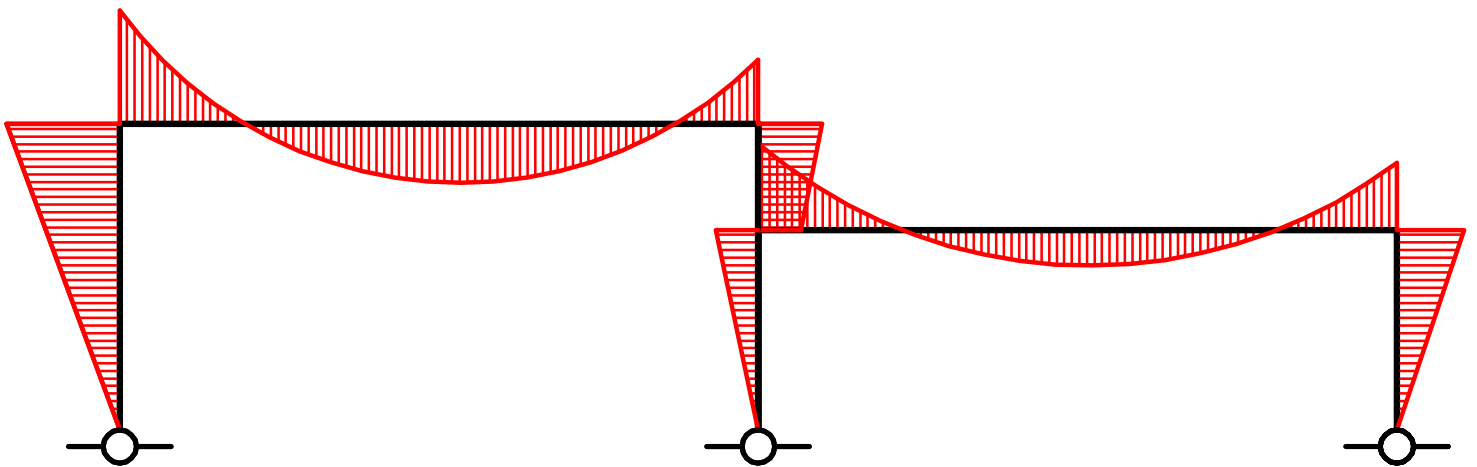
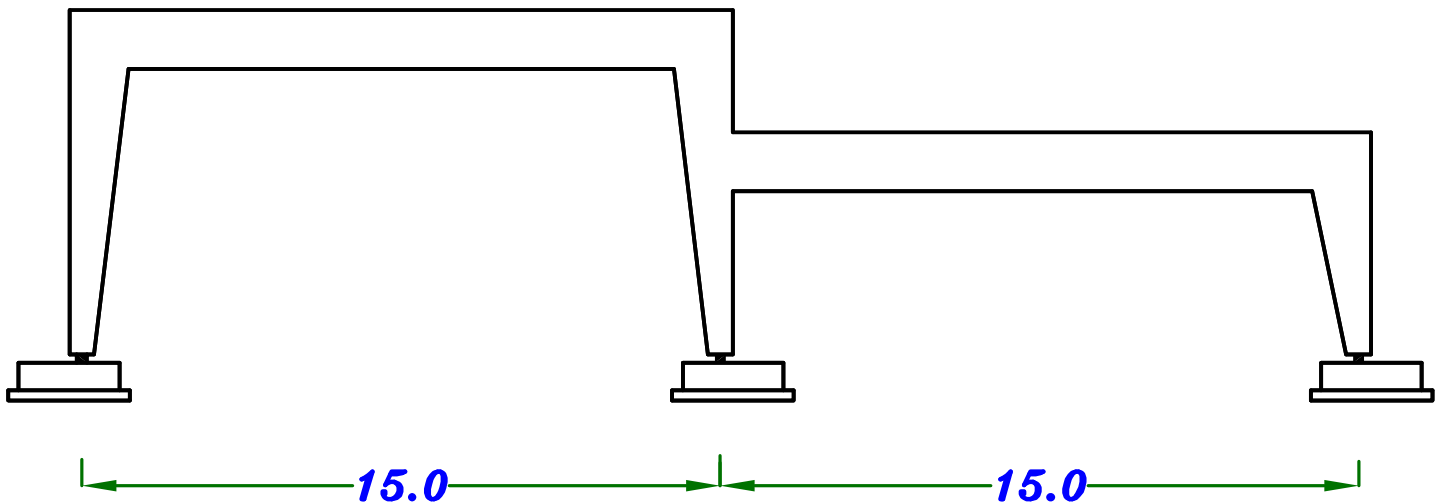
Two-Hinged Frame



Connection between two Frames.

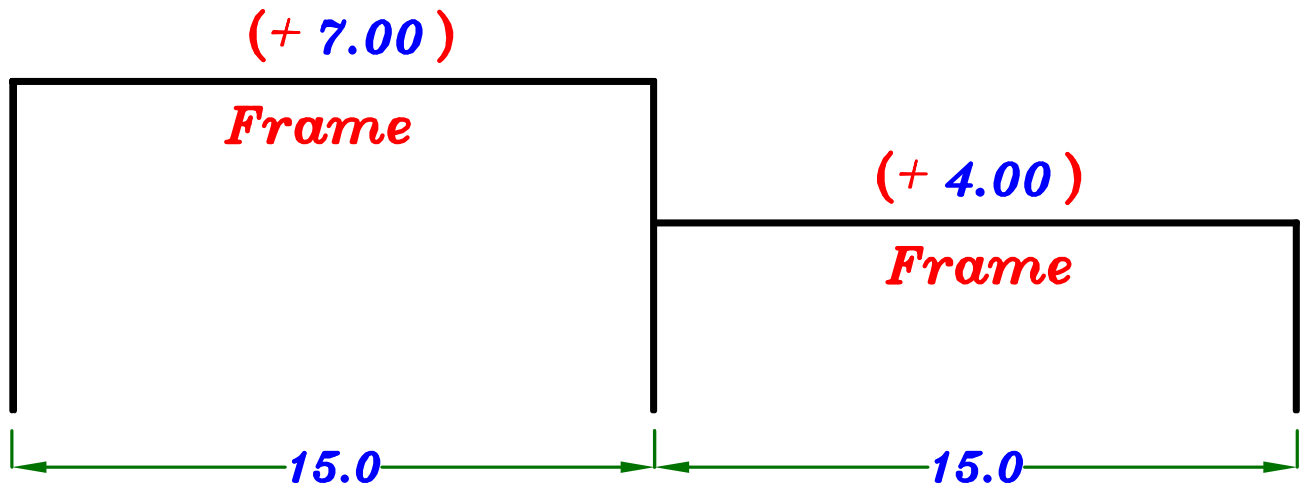


عاده في العمل يحل هذا ال **system** على انه **Continuous Frame**



لكن حله يدويا سيكون صعب جدا
لذا يفضل في الدراسة ان تفصل بينهم و تحل كل **system** بمفرده .

يفضل في الدراسة ان تفصل بينهم و نحل كل **system** بمفرده .



يفضل أن تفصل بين ال **2 Frames**

Two Hinged Frame

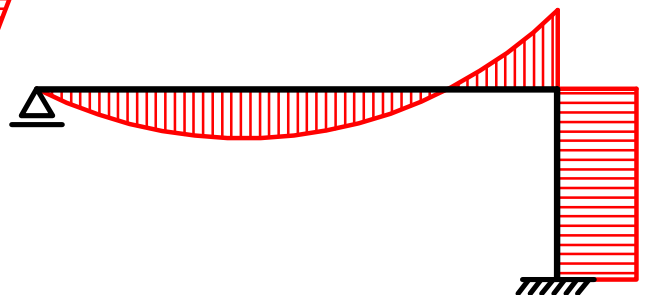
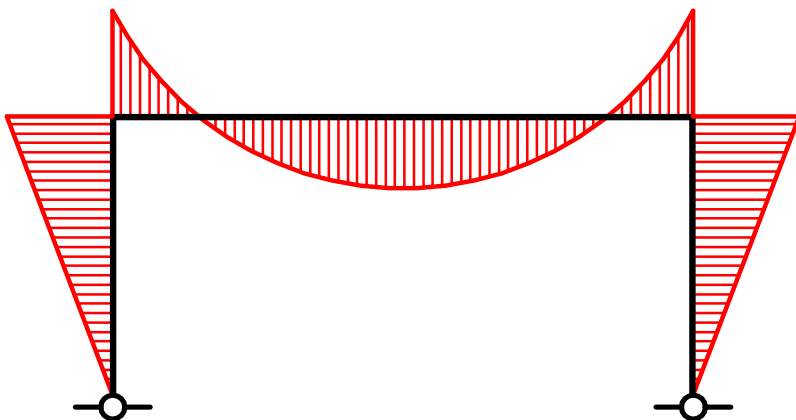


Solve using
Moment Distribution Method

Roller Fixed Frame

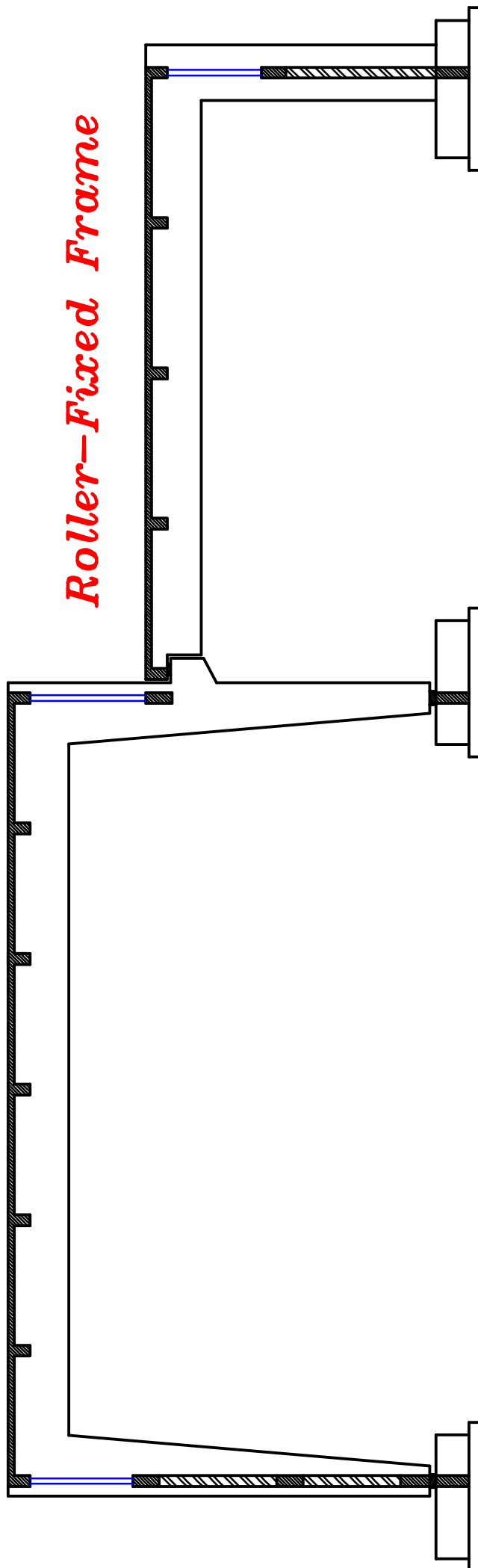


Solve using
Virtual Work Method

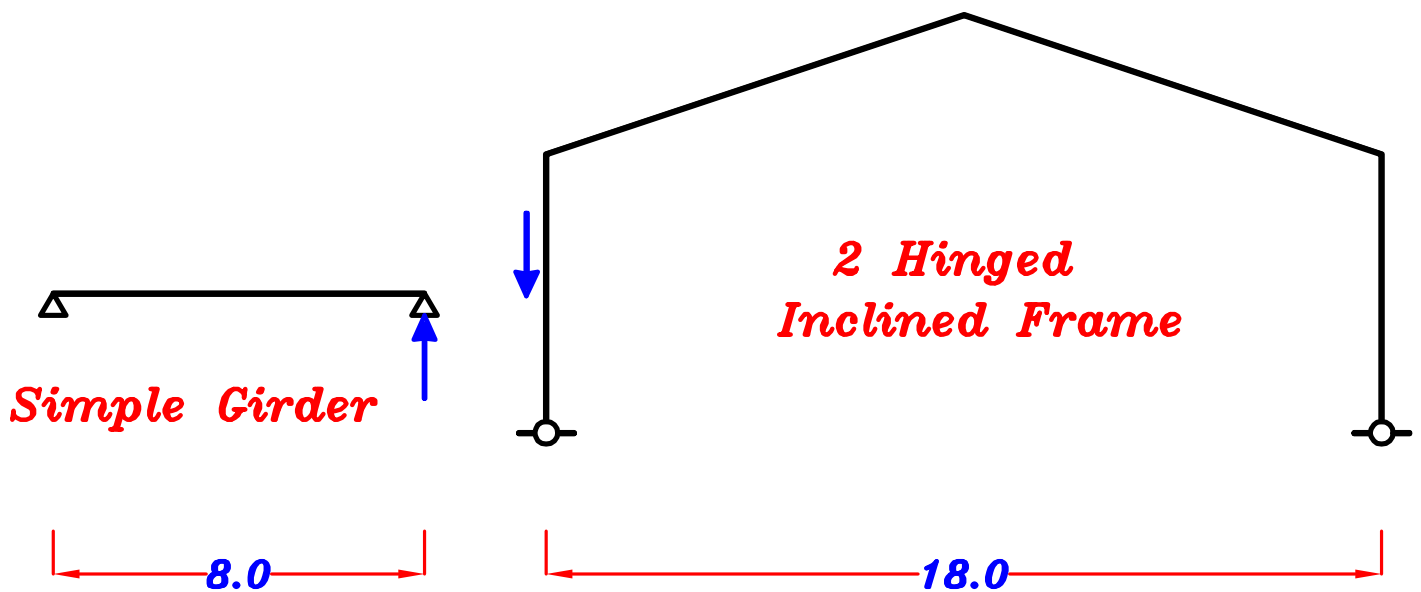
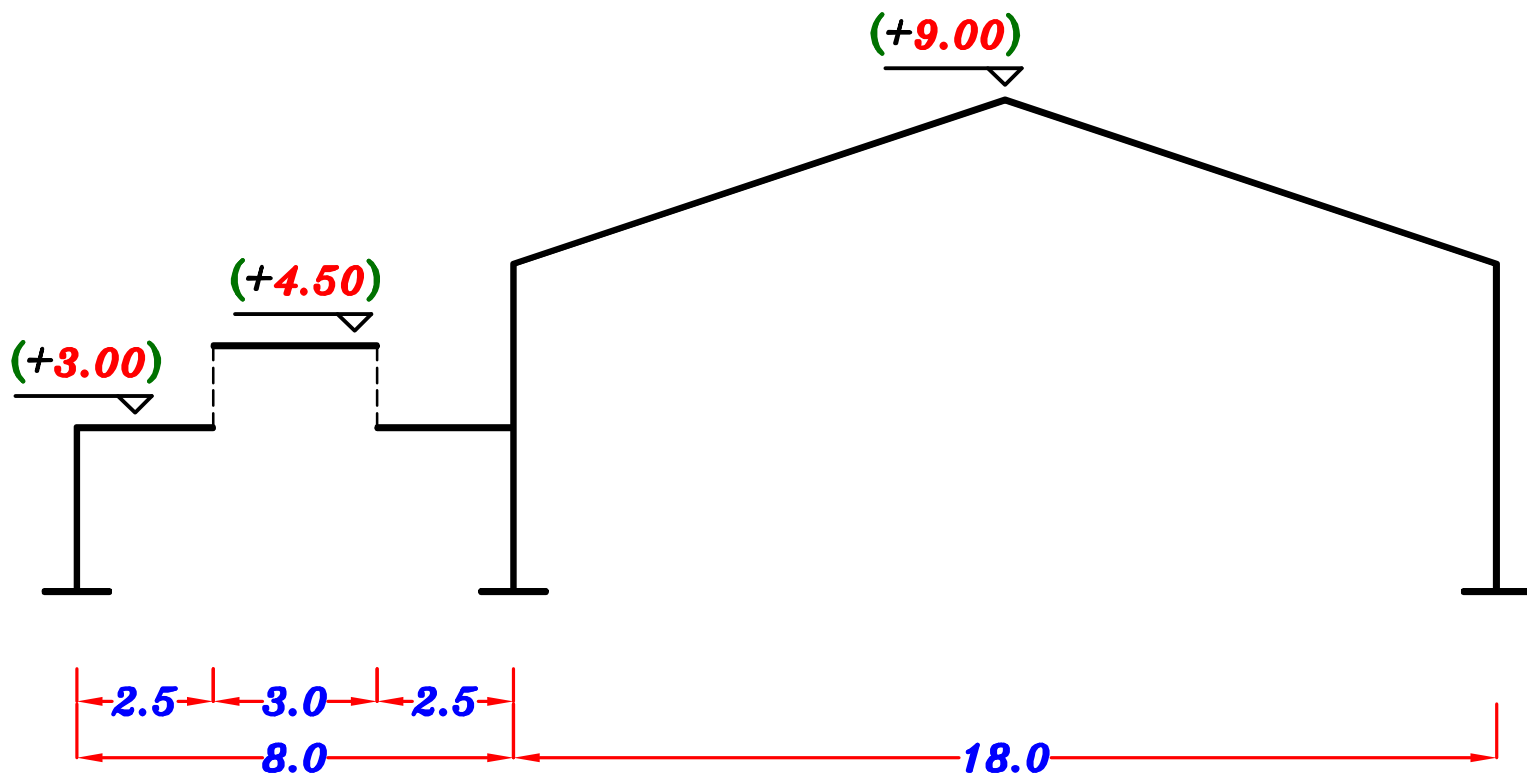


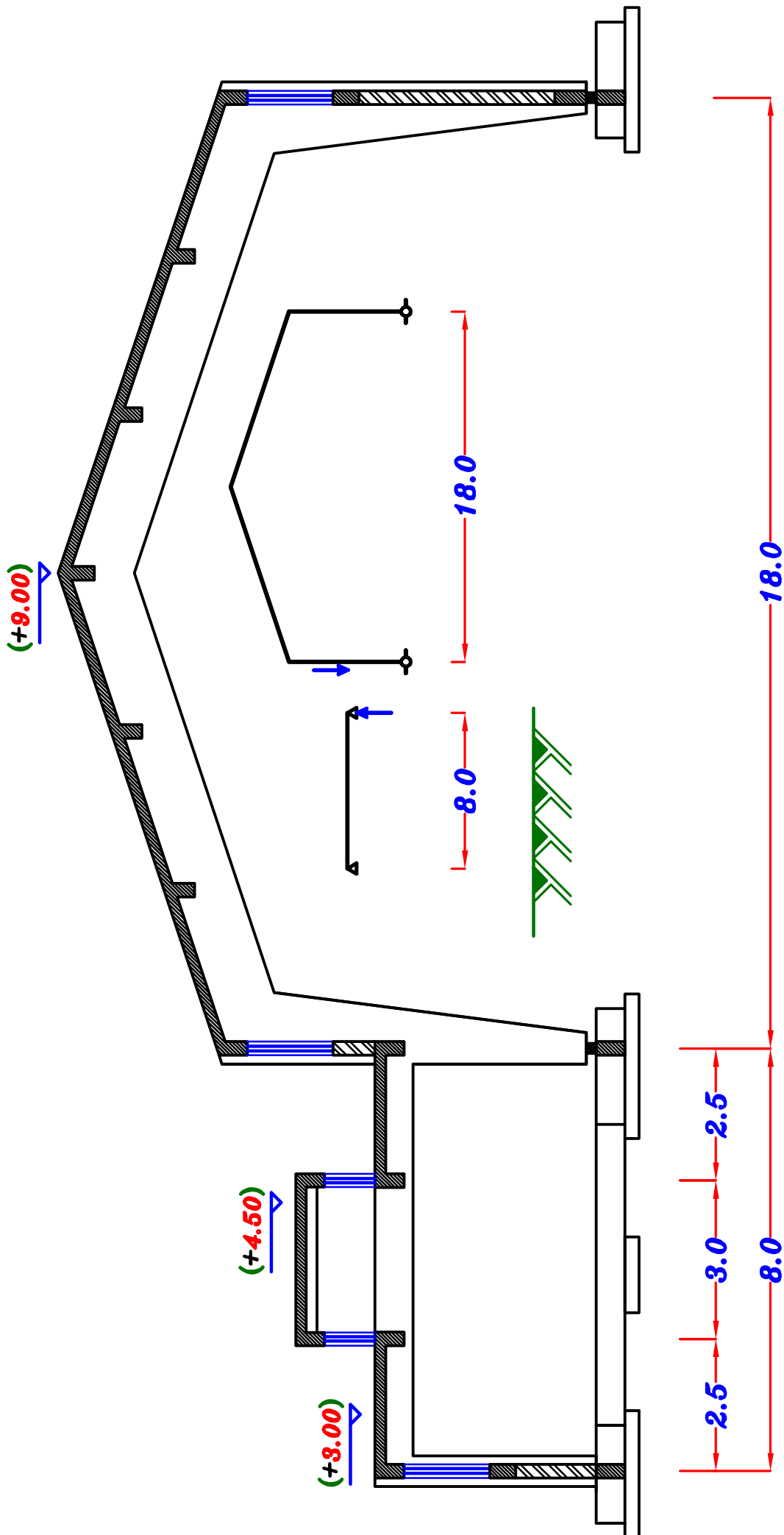
Two-Hinged Frame

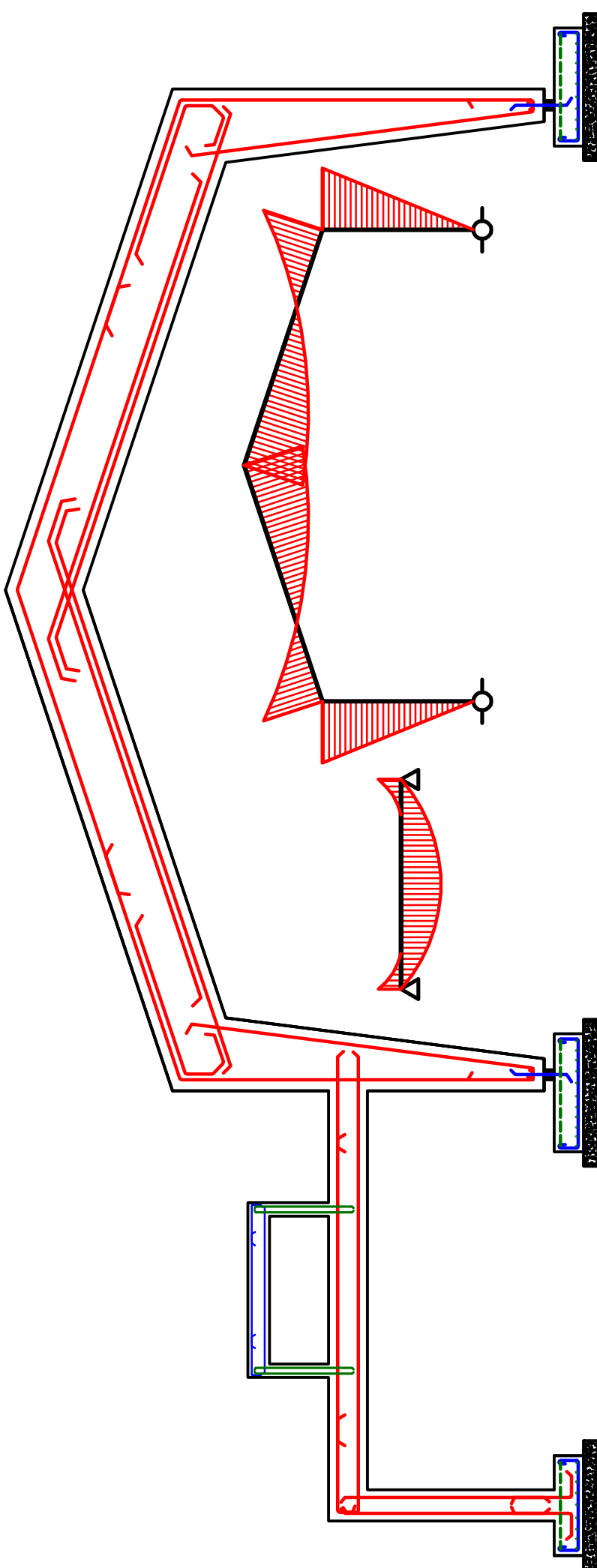
Roller-Fixed Frame



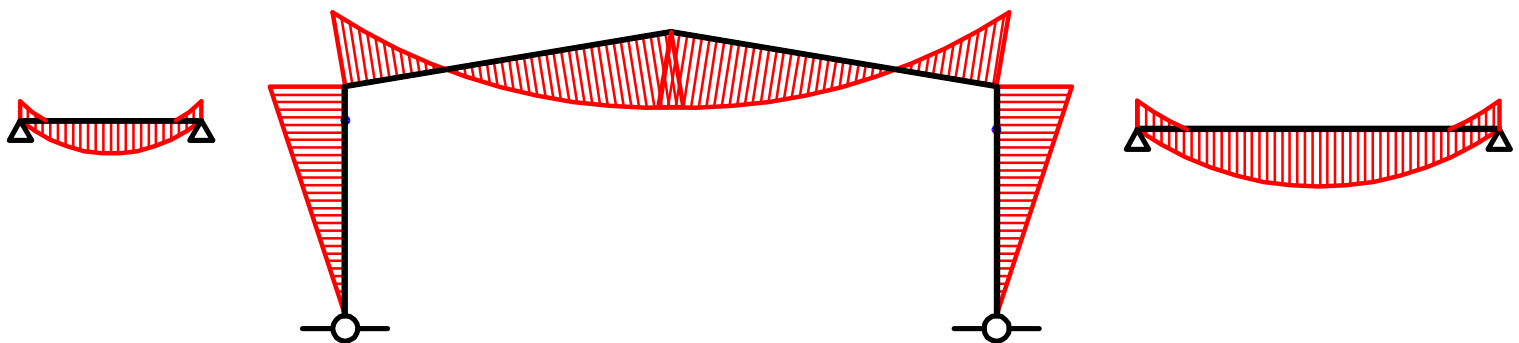
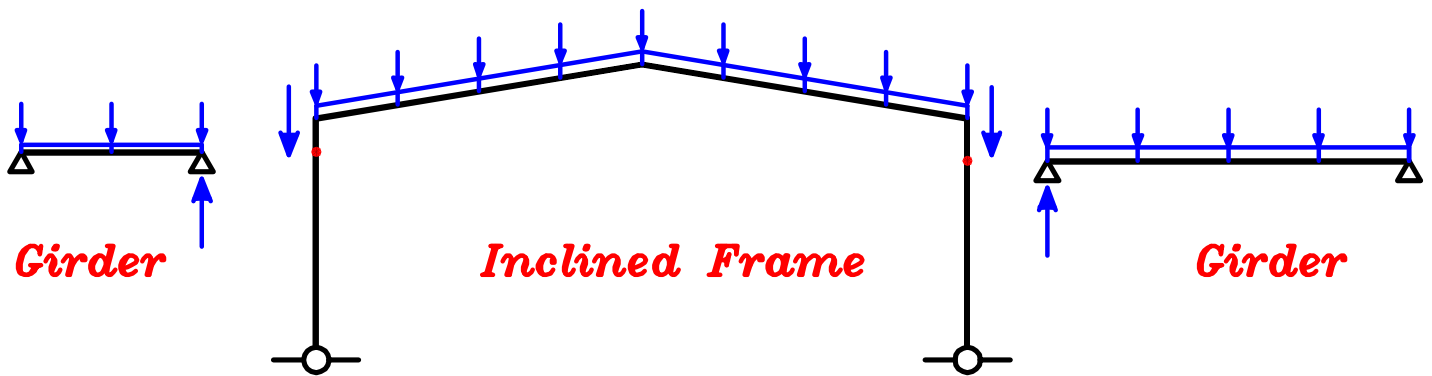
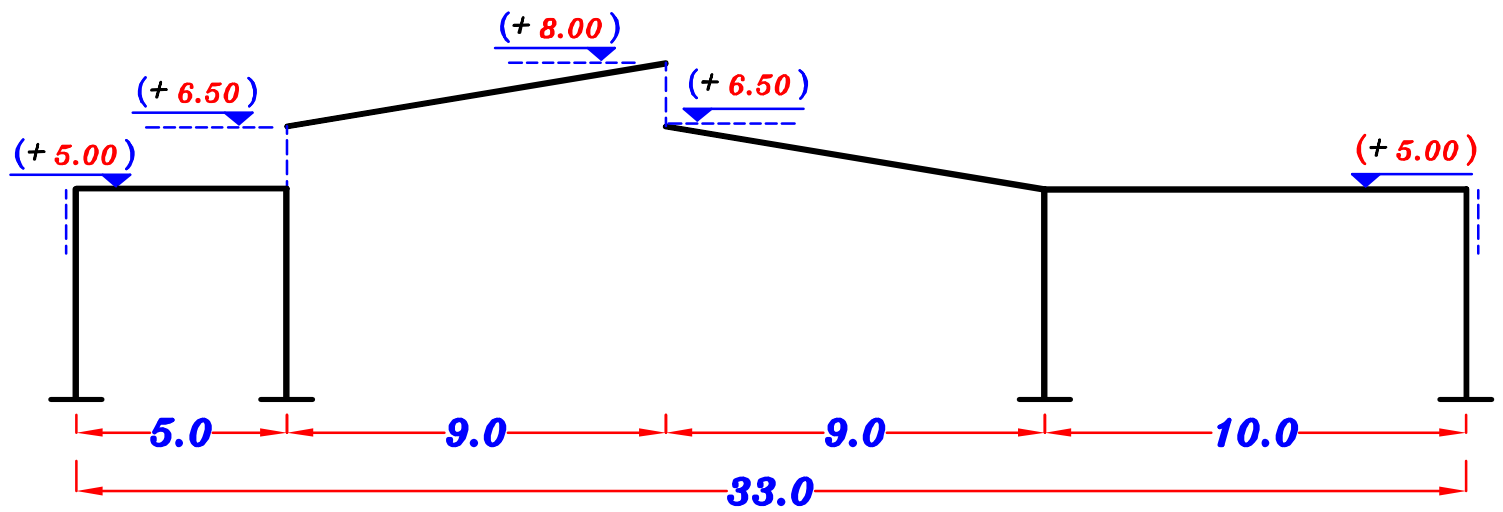
Example.

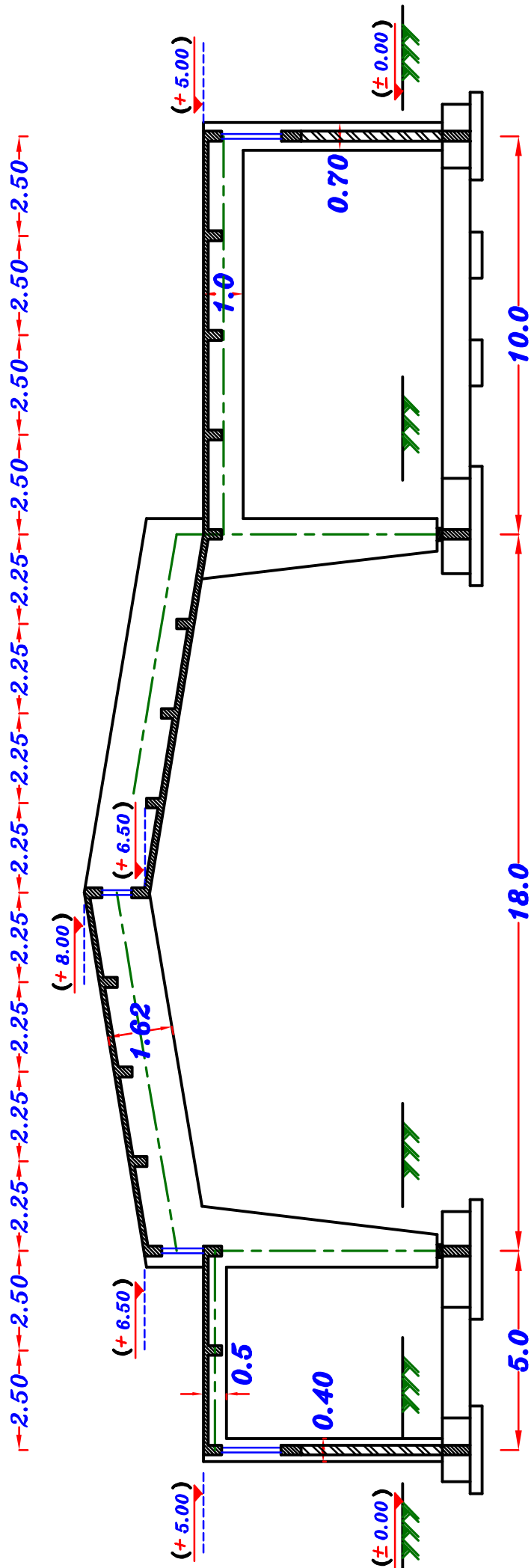


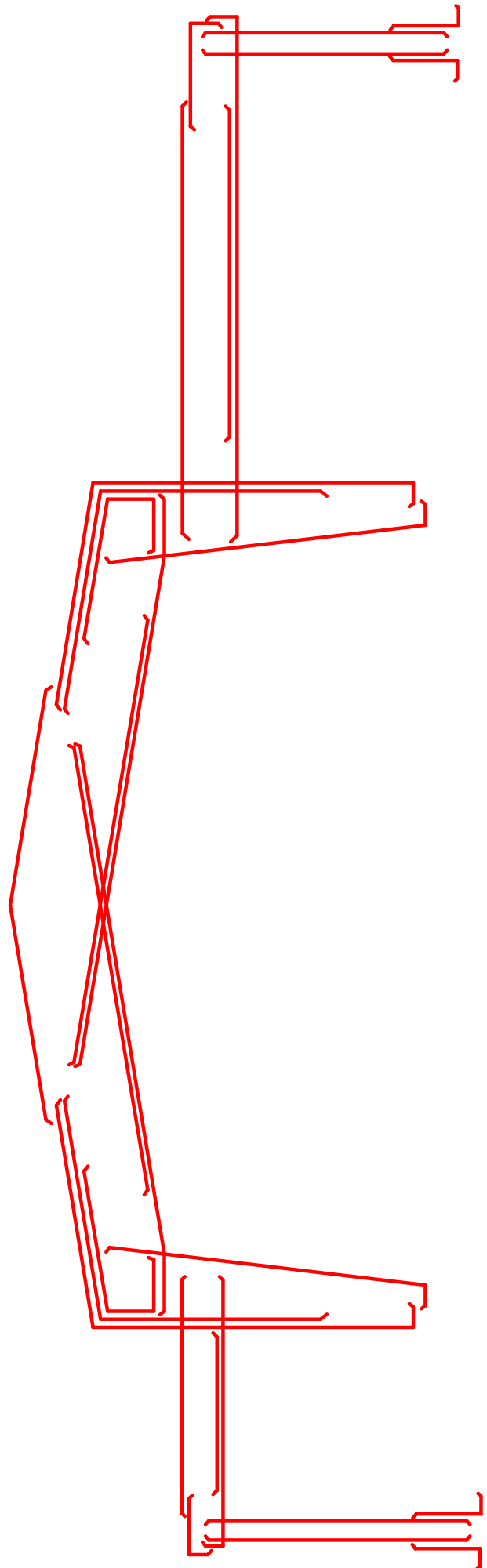
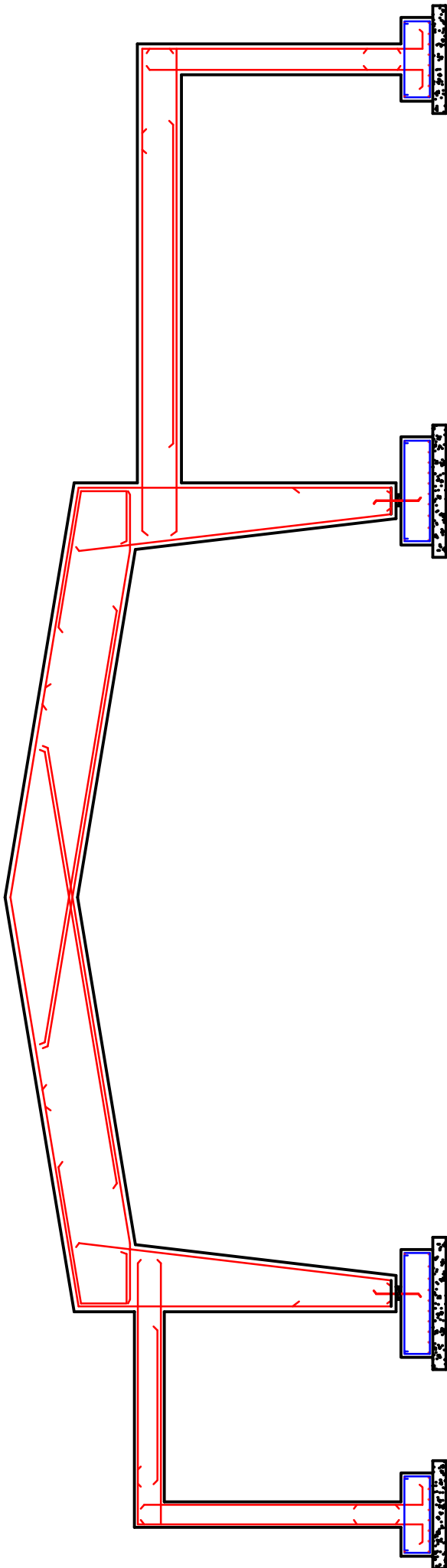




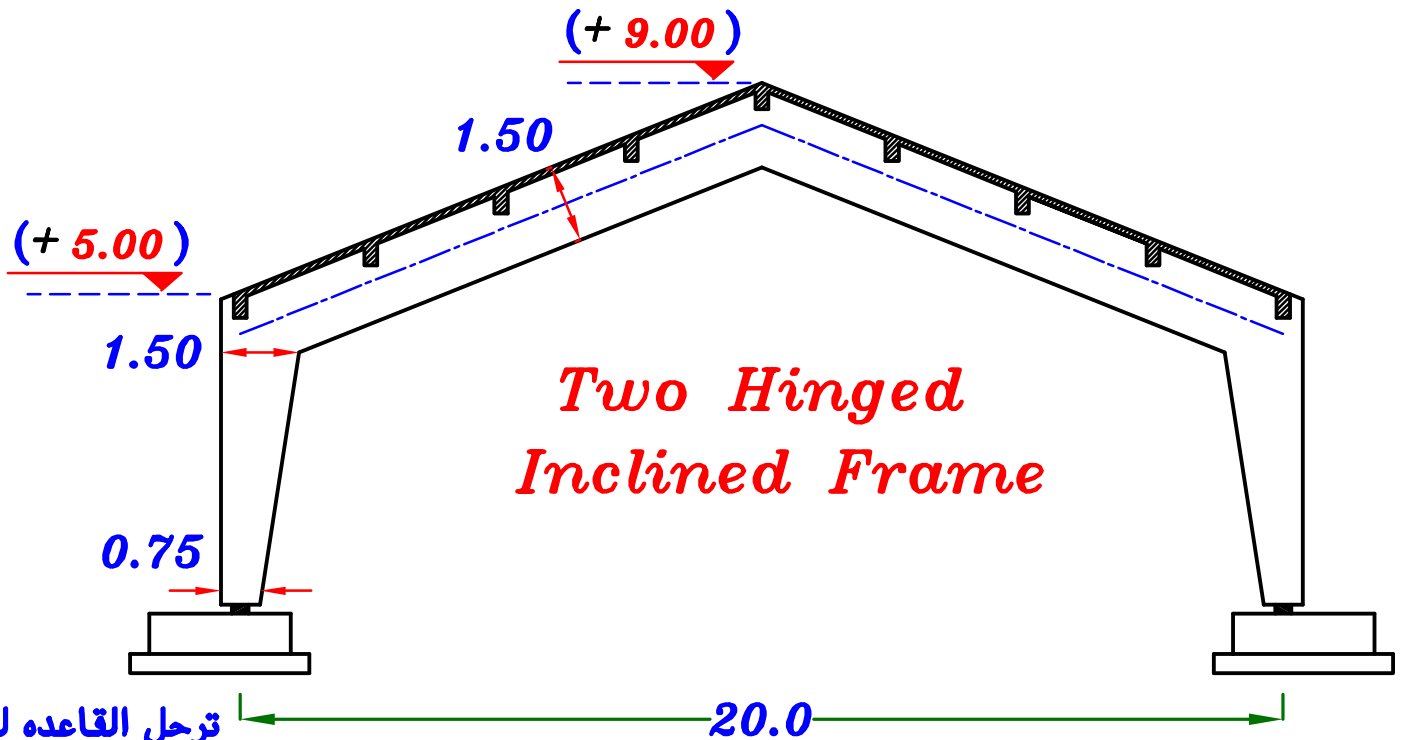
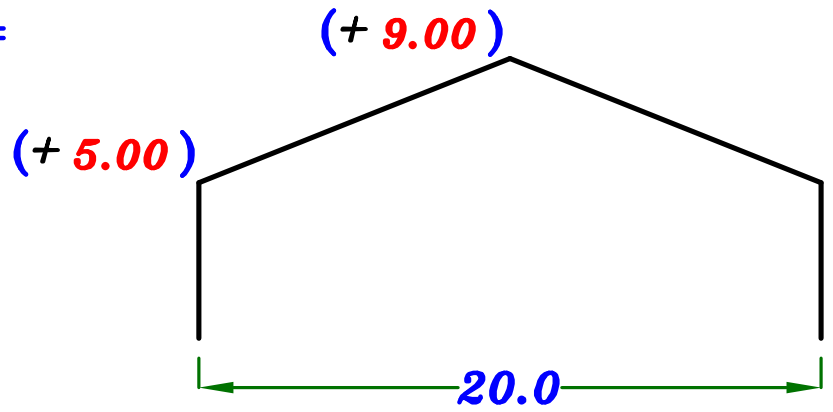
Example.



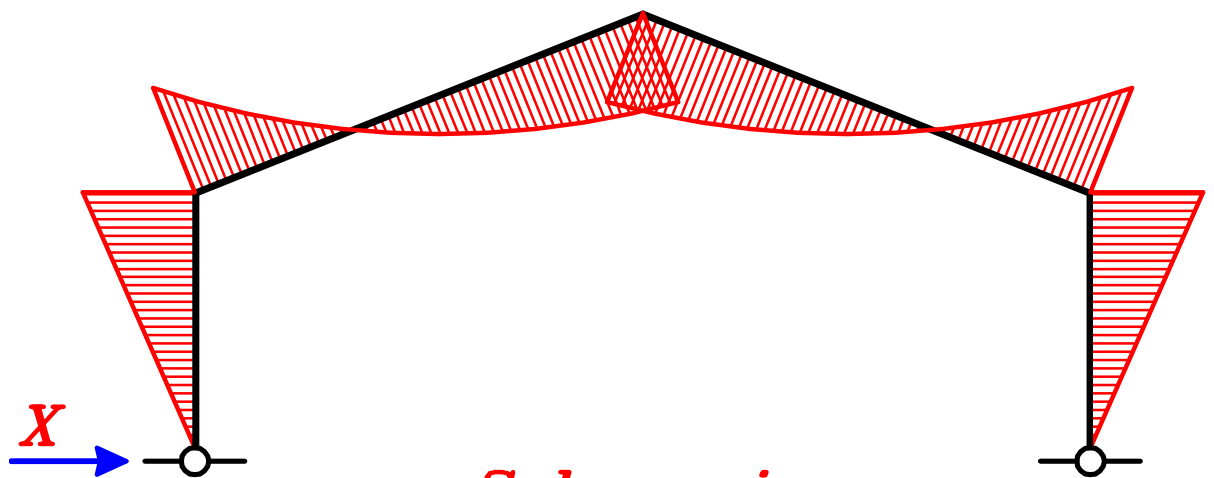




Example.

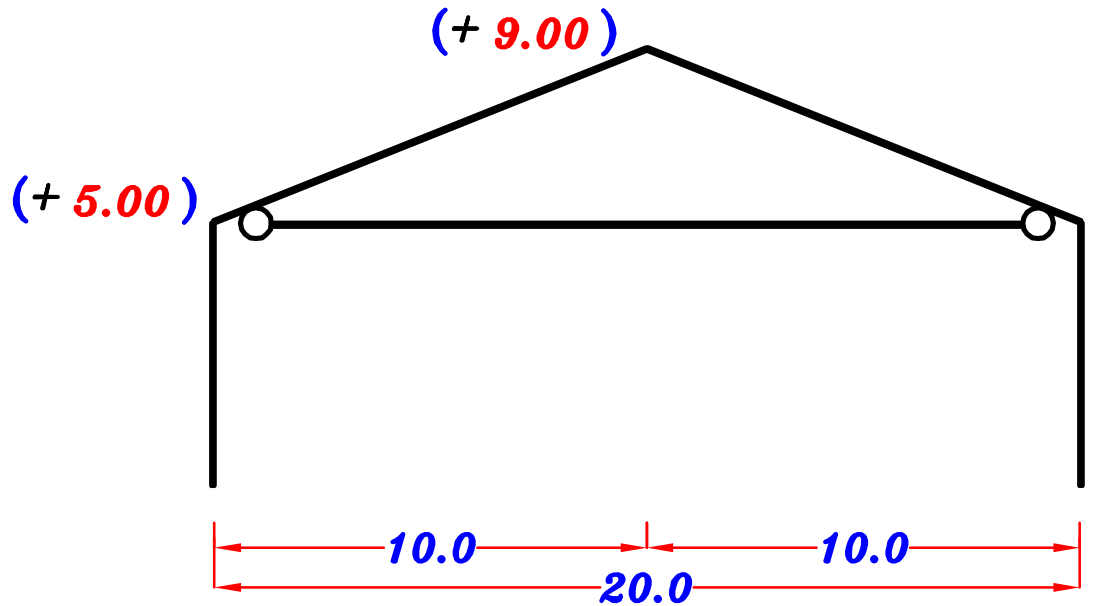


ترحل القاعده للخارج
عكس اتجاه X



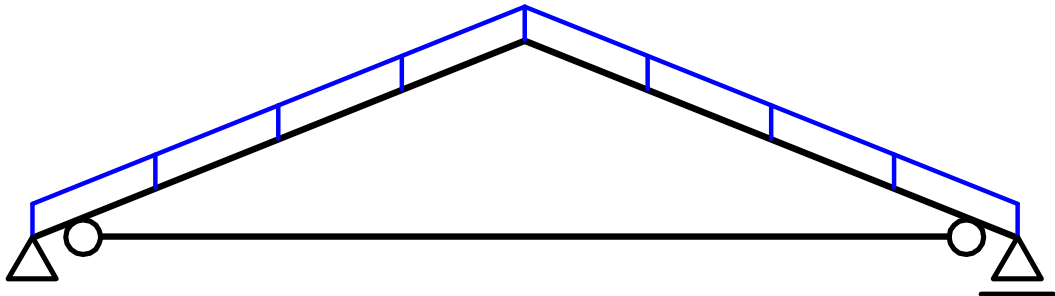
*Solve using
Virtual Work Method*

Note.

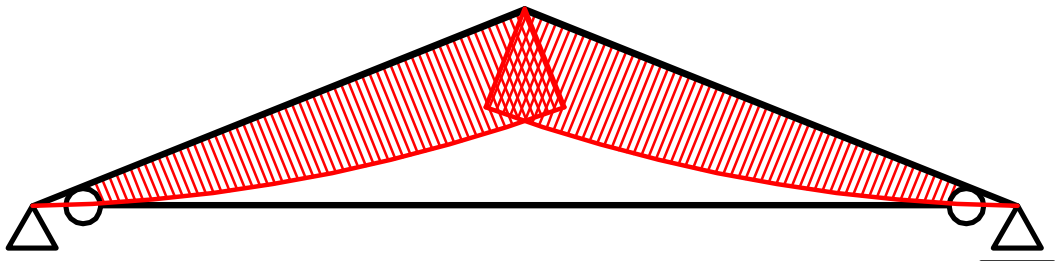


Choose a convenient Statical System and draw a sketch For an elevation Showing Concrete Dimensions.

نظرا لوجود **tie** فان ال **tie** تعمل على سحب القوى الافقيه من على الاعمده
و بالتالى لا يوجد عزوم على الاعمده فيكون ال **system** عبارة عن **Girder**

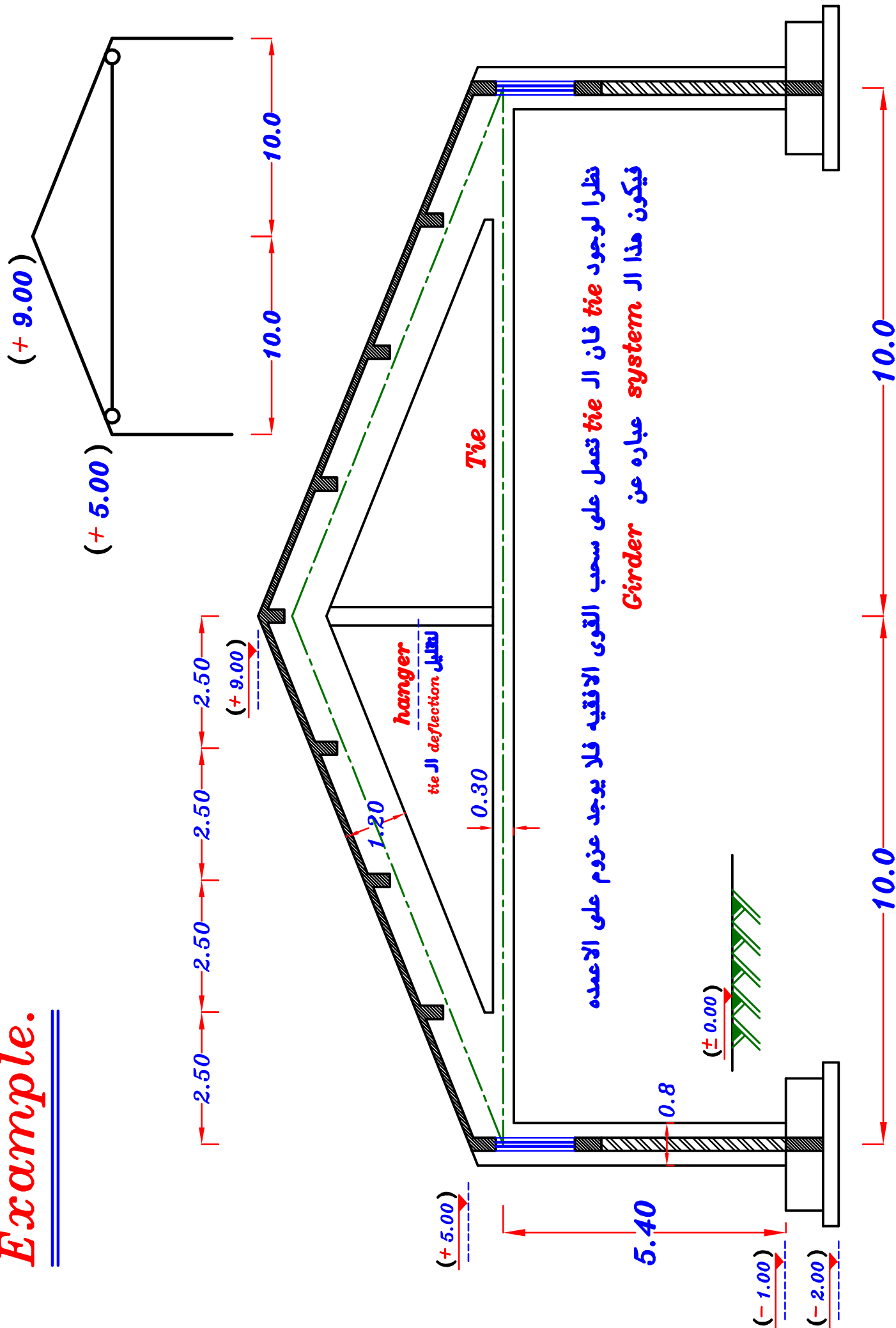


Solve using Virtual Work Method

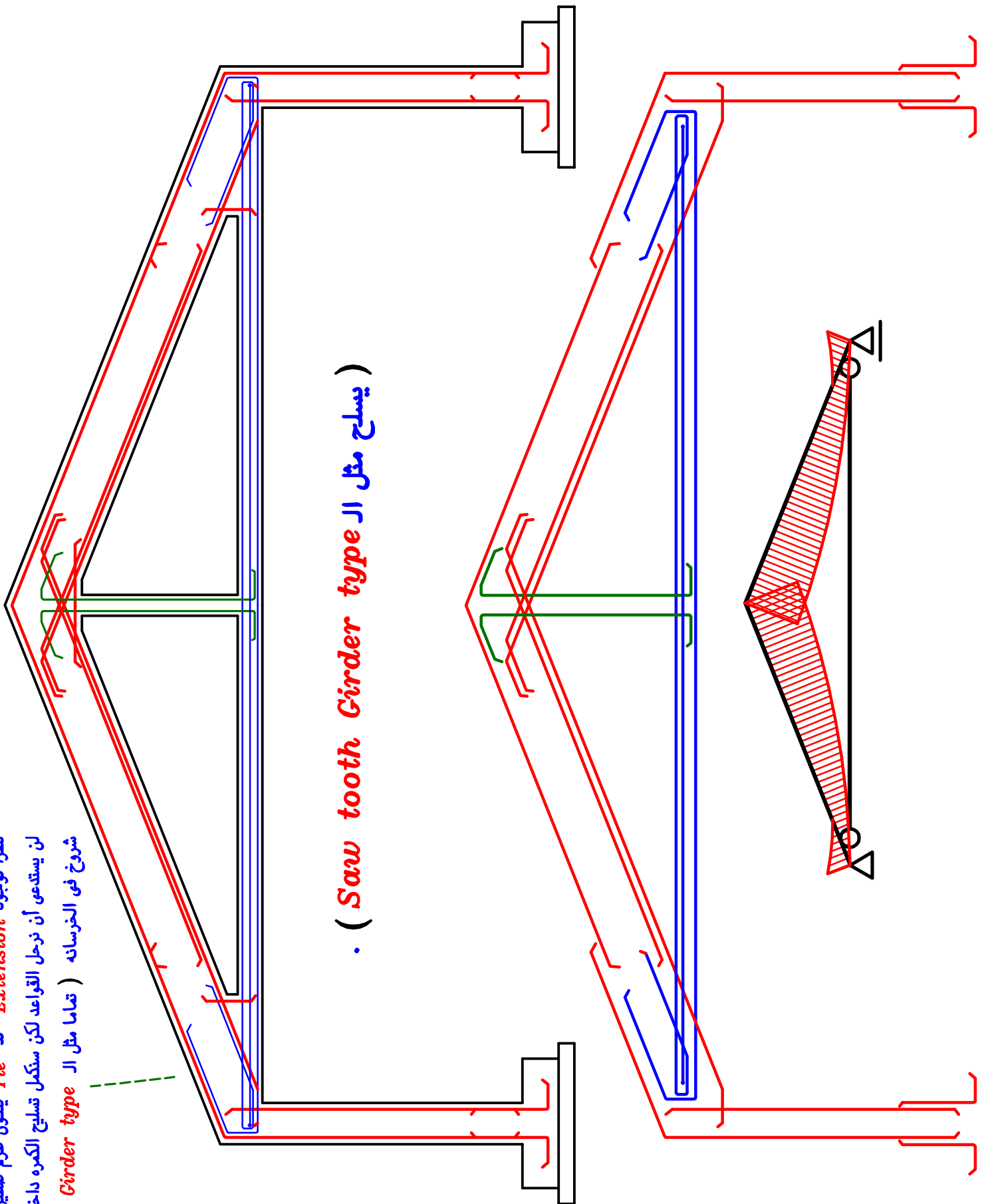


لكن نظرا لوجود **Extension** لل **Tie** فيتكون عزم صغير على الاعمده
لن يستدعى أن نرحل القواعد لكن سنكمل تسليح الكمره داخل العمود حتى لا تحدث
شروخ في الخرسانه (تماما مثل ال **Saw tooth Girder type**) .

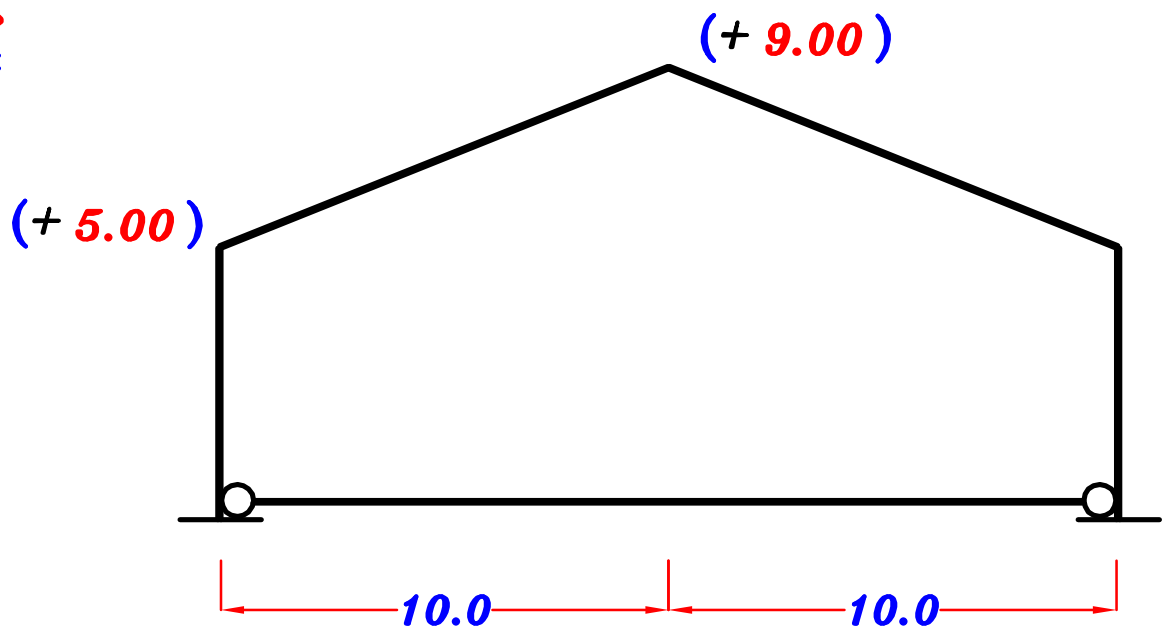
Example.



نظرا لوجود *Extension* لا *Tie* يتكون عزم صغير على الاعده
لن يستدعى أن نرحل القواعد لكن سنكمل تسليح الكمره داخل العمود حتى لا تحدث
شروخ في الخرسانه (تماما مثل ال *Saw tooth Girder type*) .

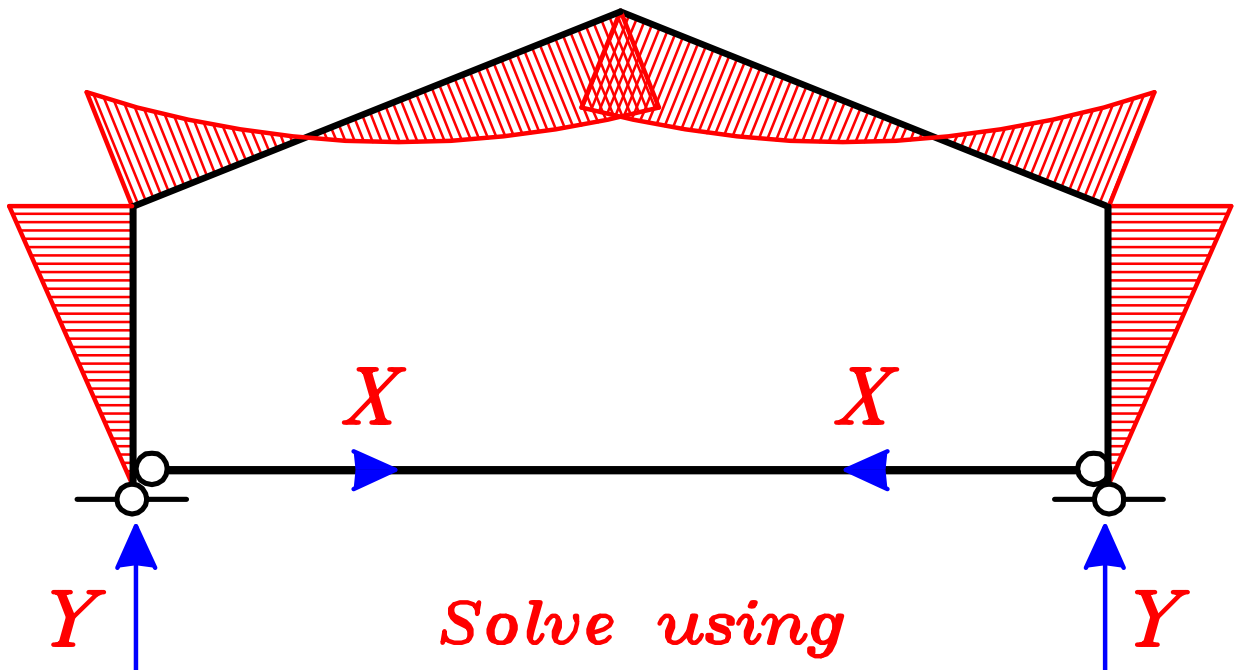


Note.



Choose a convenient Statical System and draw a sketch For an elevation Showing Concrete Dimensions.

نظرا لوجود **tie** فان ال **tie** تعمل على سحب القوى الافقيه من على القواعد
و بالتالى لا يوجد ترحيل للقواعد



*Solve using
Virtual Work Method
or Approximate*

